

IISER Kolkata – Mid-Semester Examinations

CH-3103- Quantum Chemistry II

Total marks = 20

Duration: 1 hour

**Note: Answer all questions. Each question contains 5 marks.**

1. Calculate the most probable value of  $r$  in 1s state. Wave function for 1s state is given

$$\text{by } \psi_{100} = \frac{1}{\sqrt{\pi}} \left( \frac{1}{a_0} \right)^{3/2} \exp\left(-\frac{r}{a_0}\right).$$

2. Calculate the probability that a hydrogen 1s electron will be found within a distance

$$a_0 \text{ from the nucleus. [ Given: } \int x^2 e^{bx} dx = e^{bx} \left( \frac{x^2}{b} - \frac{2x}{b^2} + \frac{2}{b^3} \right) ]$$

3. Prove that  $[\hat{L}_z, \hat{L}_+] = \hat{L}_+$

4. If  $[\hat{A}, \hat{B}] = c\hat{B}$ , where  $c$  is a constant and  $\hat{A}\psi = a\psi$ , then prove that

$$\hat{A}(\hat{B}\psi) = (a+c)(\hat{B}\psi).$$

*Amwari*