

IISER Kolkata – Mid-Semester Examinations

CH-3103- Quantum Chemistry II

Total marks = 20

Duration: 1 hour

Note: Answer all questions. Each question contains 5 marks.

1. Calculate the most probable value of r in 1s state. Wave function for 1s state is given

$$\text{by } \psi_{100} = \frac{1}{\sqrt{\pi}} \left(\frac{1}{a_0} \right)^{3/2} \exp\left(-\frac{r}{a_0}\right).$$

2. Calculate the probability that a hydrogen 1s electron will be found within a distance

$$a_0 \text{ from the nucleus. [Given: } \int x^2 e^{bx} dx = e^{bx} \left(\frac{x^2}{b} - \frac{2x}{b^2} + \frac{2}{b^3} \right)]$$

3. Prove that $[\hat{L}_z, \hat{L}_+] = \hat{L}_+$

4. If $[\hat{A}, \hat{B}] = c\hat{B}$, where c is a constant and $\hat{A}\psi = a\psi$, then prove that

$$\hat{A}(\hat{B}\psi) = (a+c)(\hat{B}\psi).$$

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