



Experiments on Bell's theorem: past, present, and future



Everyday Loophole-free

Florian Fertig
Pooja Malik
Chengfeng Xu
Yiru Zhou

Wei Zhang
Tim van Leent
Robert Garthof
Kai Redeker
Weniamin Rosenfeld

Daniel Burchardt
Sebastian Eppelt
Norbert Ortegel
Markus Rau
Mathias Seubert
Derya Taray

René Schwonnek
Valerio Scarani
Charles C.-W. Lim



Jake Covey
Hannes Bernien

U Illinois
U Chicago

Funding by IMPRS, CSC, BMBF, DFG



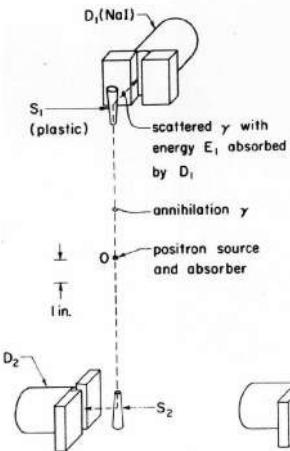
- the early days
- Aspect
- SPDC: new tools and long distances
- towards closing loopholes
- new strategies and detectors
- loophole free
- future: more users – networks – closing more loopholes?



Chien-Shiung Wu

- Wu-Shaknov
First observation of quantum correlations using electron-positron annihilation with parallel analyzers ('50)

- L. Kasday
 - angle dependent Compton scattering violation of Bell-inequality (70)



L. Kasday, Proc.
School Enrico Fermi IV (71)

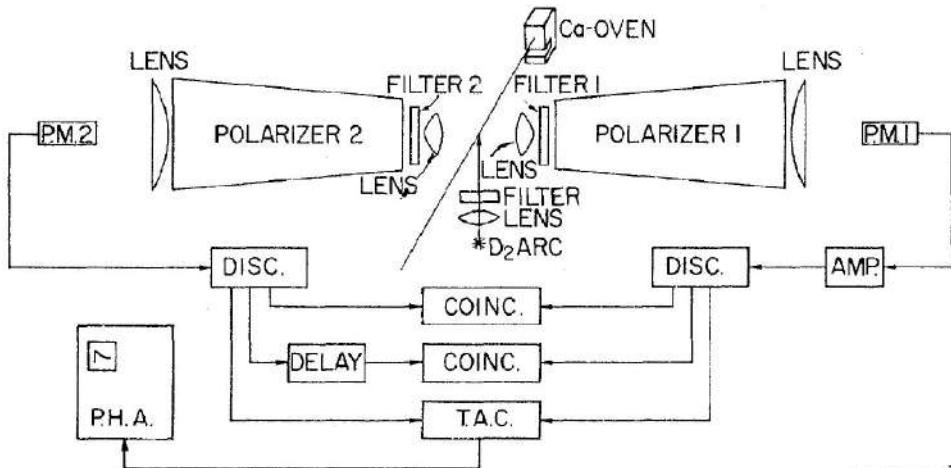


Photon Cascades



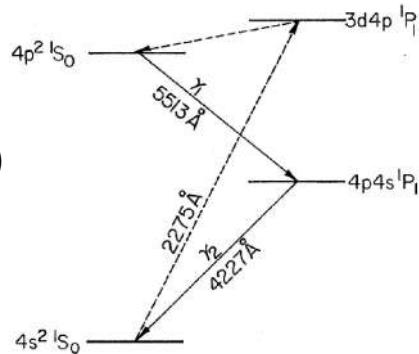
S.J. Freedman, J.F. Clauser, PRL 28, 938 (1972)

Freedman, Clauser 1972

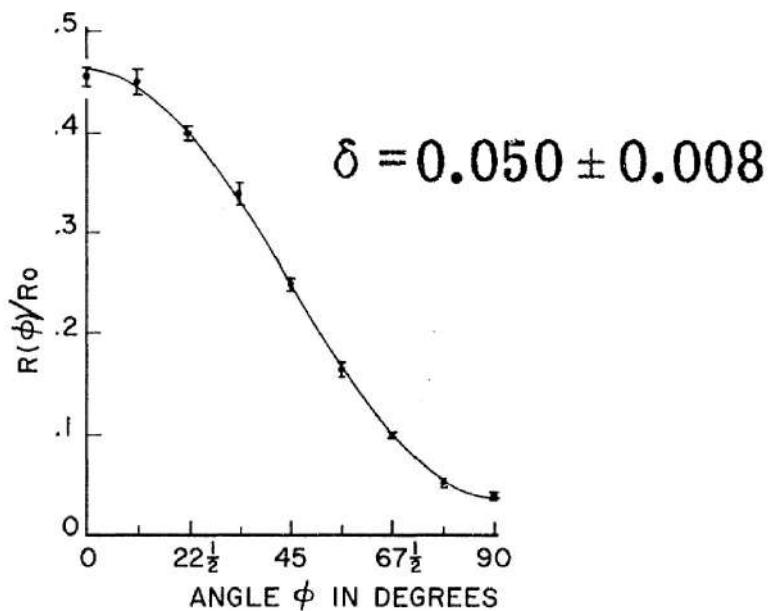


$$\delta = |R(22\frac{1}{2}^\circ)/R_0 - R(67\frac{1}{2}^\circ)/R_0| - \frac{1}{4} \leq 0$$

- experimental design by Kocher Commins (|| orient.)
- Ca excited by D₂-lamp
- ~0.2 coincidence counts/s
- 200 h measurement time



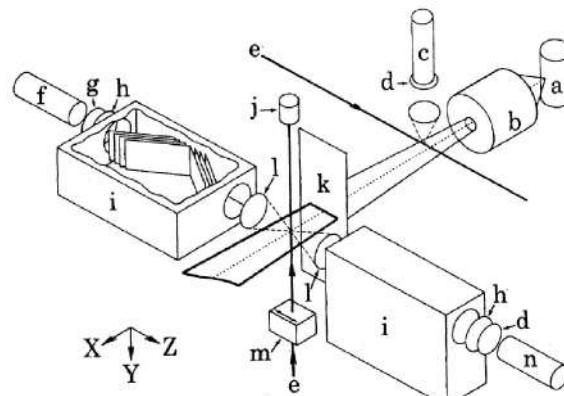
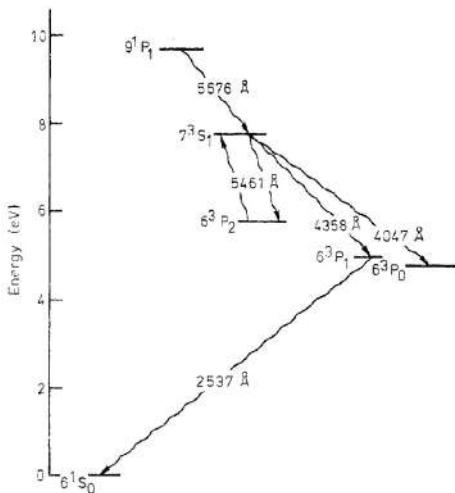
We consider
these results to be strong evidence against local
hidden-variable theories.





Holt, Pipkin (unpublished)

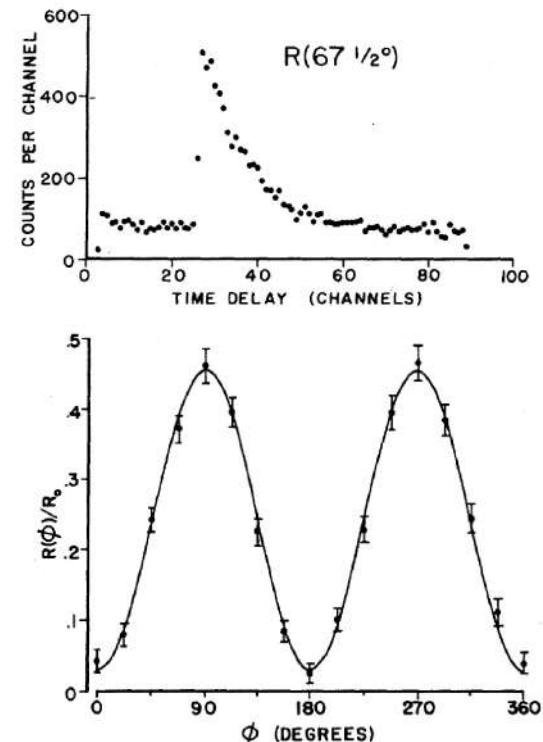
- cascade in Hg – 567.6 nm & 404.7 nm
- use $|R(\pi/8) - R(3\pi/8)| / R_0 \leq \frac{1}{4}$ but **don't observe violation**
- stress in bulb, in lens
- Clauser repeats experiment with violation



$$\delta_{\text{exp}} = 0.046 \pm 0.014$$

Fry, Thomson

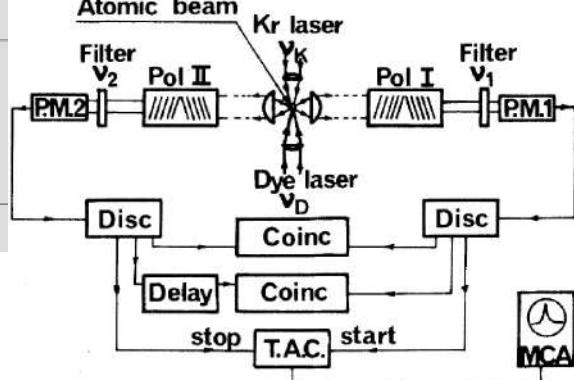
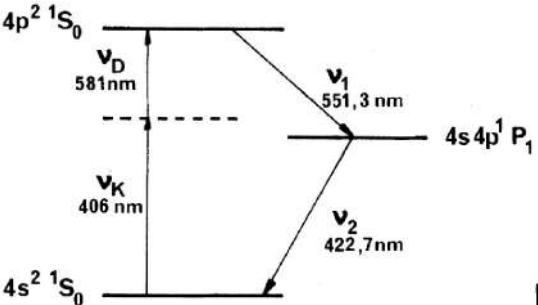
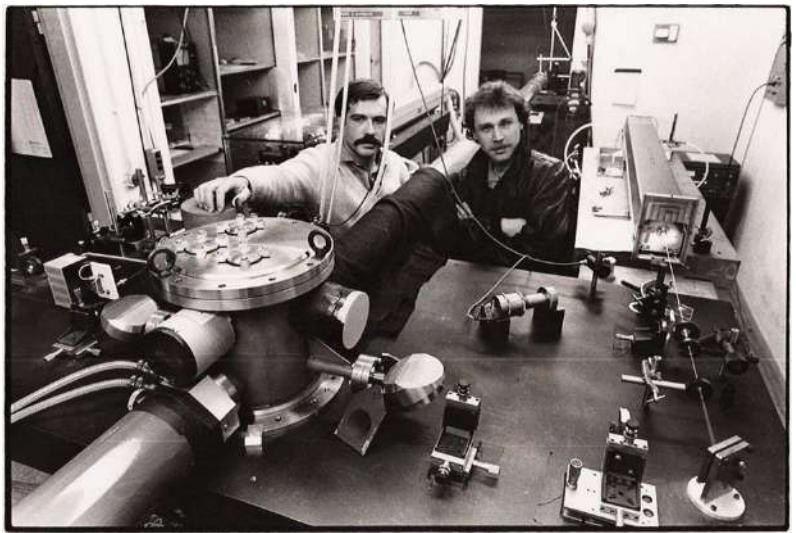
- Hg – 435.8 nm and 253.7 nm
- e- + dye-laser, improved optics
- 80 min collection/point



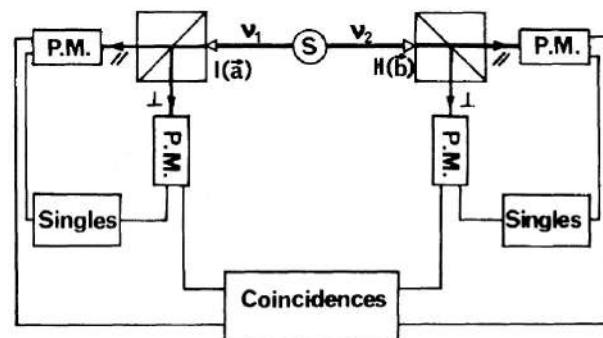
Aspect's (et al.) experiments

Alain Aspect

- pushed for improved experiments
- together with P. Grangier, J. Dalibard, G. Roger
- Ca-cascade, resonant excitation by lasers
- small volume, high efficiency** (singles 40000/s
120000/s, coinc 240/s, minus 90/s accidental)
- two-way polarizer
- time-dependent analyzers

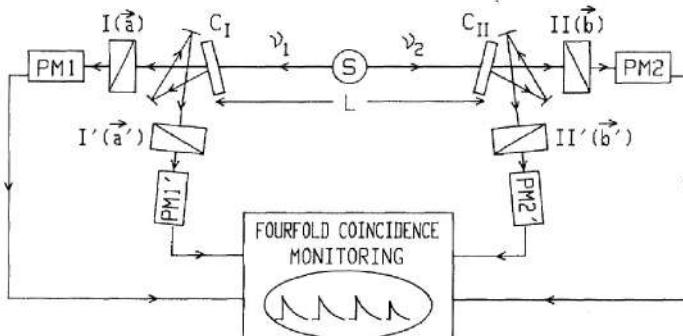
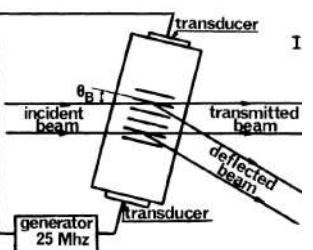


$$\delta_{\text{exp}} = 5.72 \times 10^{-2} \pm 0.43 \times 10^{-2}$$



$$S_{\text{expt}} = 2.697 \pm 0.015$$

change the settings of the polarizers, at a rate greater than c/L .



- A. Aspect, P. Grangier, G. Roger, PRL **47**, 460 (1981)
 A. Aspect, P. Grangier, G. Roger, PRL **49**, 91 (1982)
 A. Aspect, J. Dalibard, G. Roger, PRL **49**, 1804 (1982)

SPDC sources

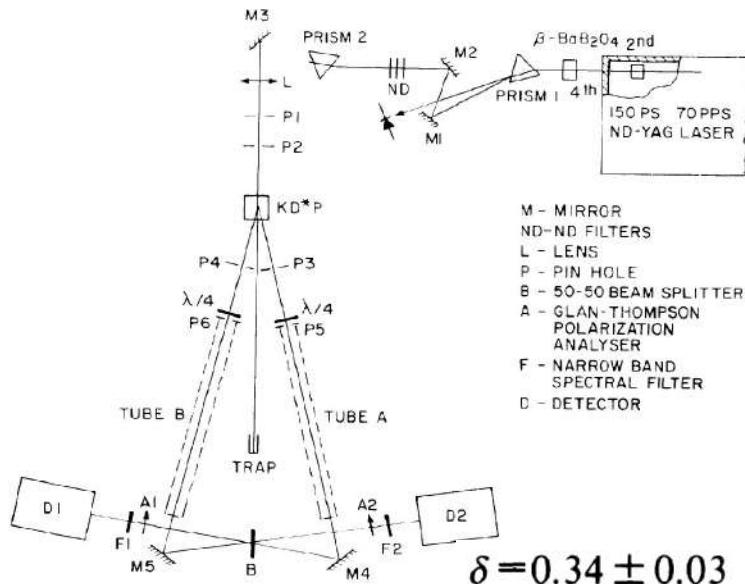


spontaneous parametric downconversion

- directed emission
- different degrees of freedom

Shih, Alley

- L & R polarised photons overlapped at a beamsplitter
- selection for coincidences



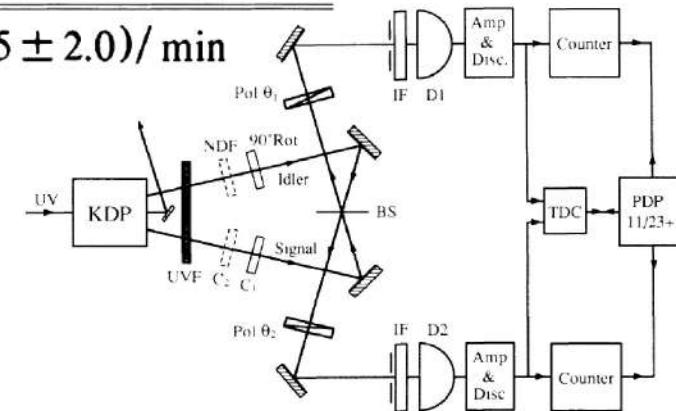
Y.H. Shih, C.O. Alley, PRL **61**, 2921 (1988)
Z.Y. Ou, L. Mandel, PRL **61**, 50 (1988)

Ou, Mandel

- orthogonal polarisation at a beamsplitter + selection
- CH-inequality (with coincidences)

θ_1	θ_2	Coincidence rate per minute \mathcal{R}
67.5°	45°	28.3 ± 0.8
22.5°	45°	29.8 ± 0.8
67.5°	0°	29.9 ± 0.8
22.5°	0°	5.6 ± 0.7
67.5°	No polarizer	34.7 ± 0.9
No polarizer	45°	36.2 ± 0.9

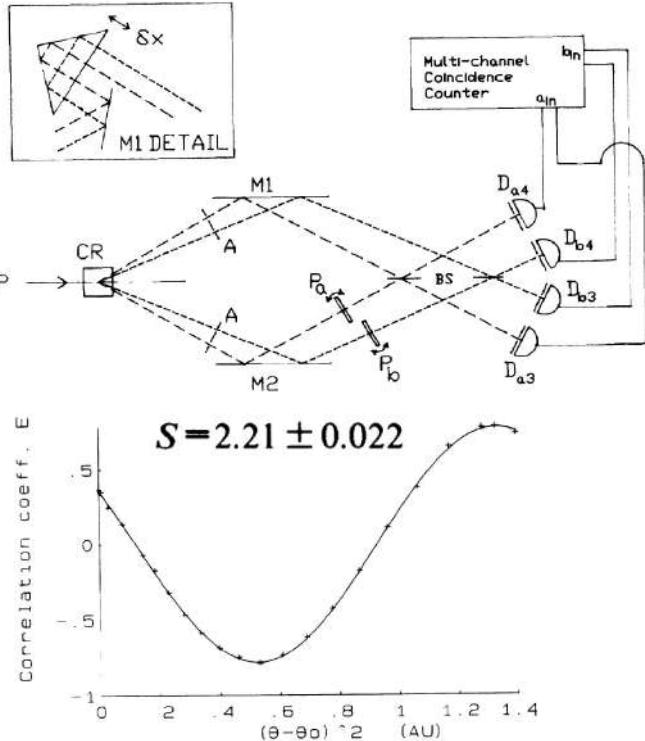
$$\tilde{S} = (11.5 \pm 2.0) / \text{min}$$



other degrees of freedom

Rarity, Tapster

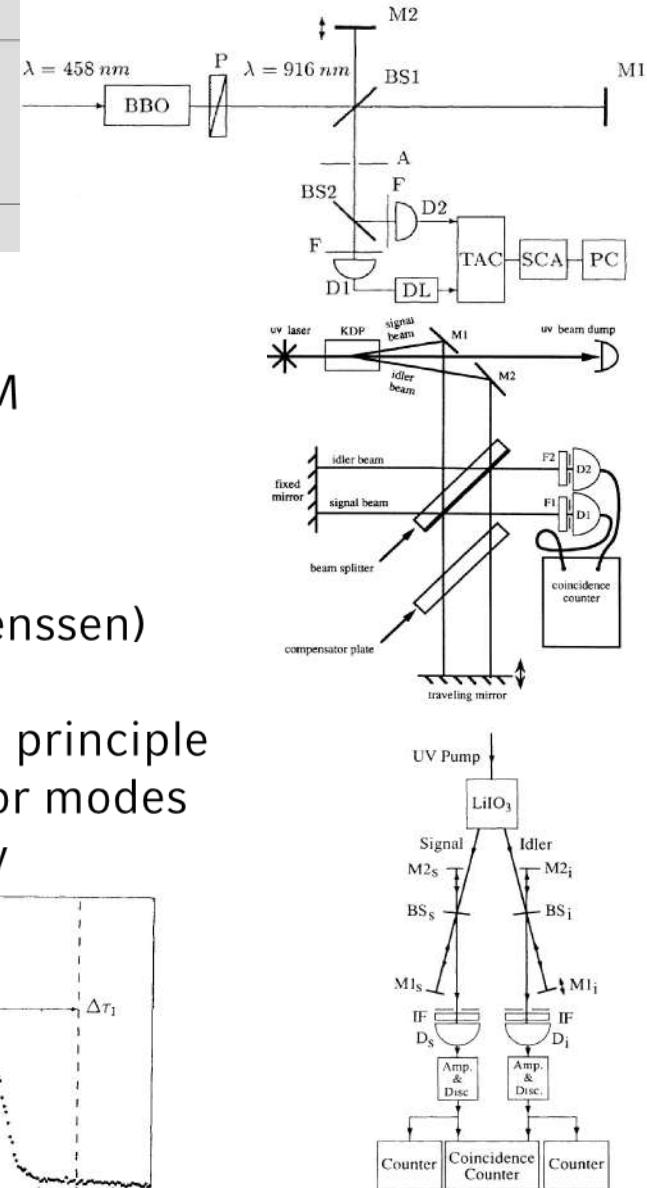
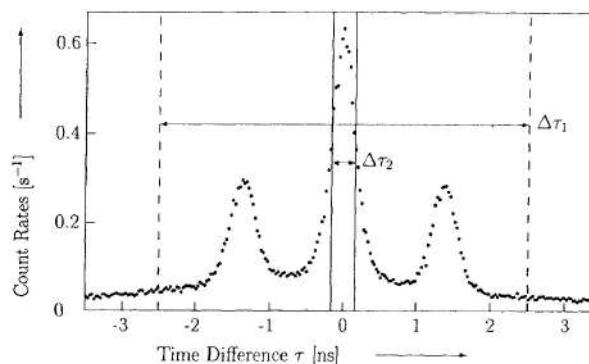
- entanglement in \vec{k} - momentum of the photons
- dual Mach-Zehnder IFM



- entanglement in ω
- dual Michelson-IFM

Kwiat et al. (Chiao)
Ou et al. (Mandel)
Brendel et al. (Martienssen)

- Bell test possible in principle
- separation in time or modes would be necessary



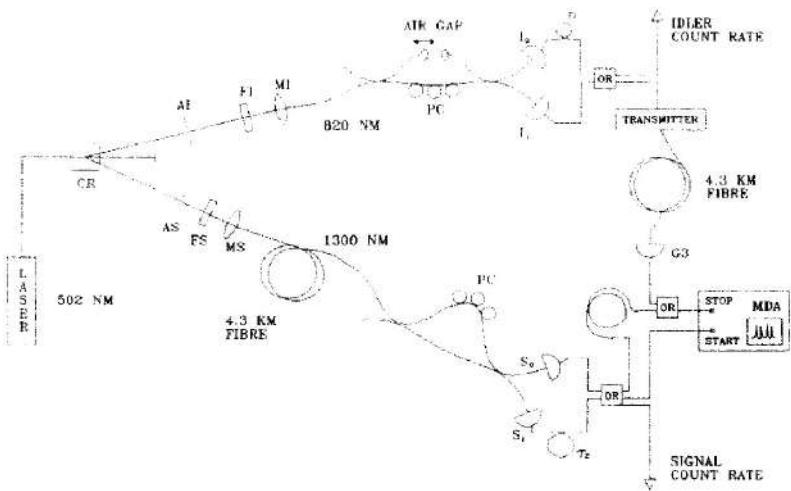
- J.G. Rarity, P.R. Tapster PRL **64**, 2495 (1990)
 Z.Y. Ou et al., PRL **65**, 321 (1990)
 P.G. Kwiat et al., PRA **41**, 2910 (1990)
 J. Brendel et al., PRL **66**, 1142 (1991)

long distances



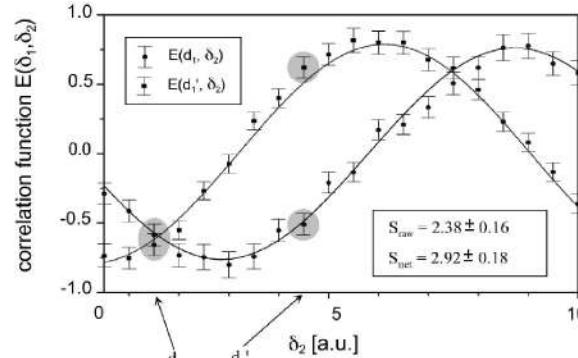
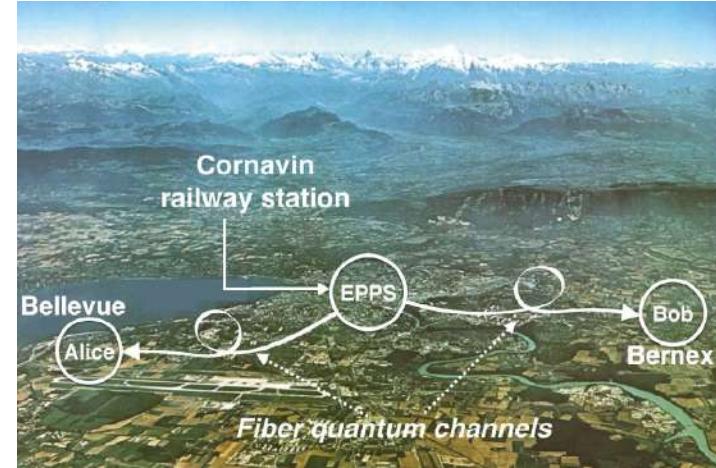
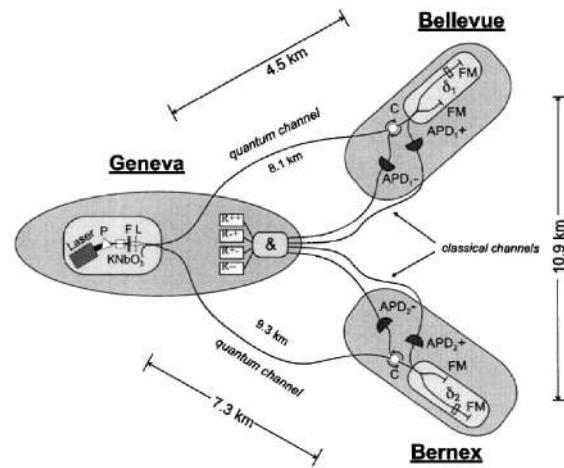
Tapster, Rarity, Owen

- dual wavelength
- 4.3 km in 1300 nm arm



Tittel, Brendel, Gisin, Zbinden

- deployed fibers, both photons 1310 nm
- 10.9 km between observers



P.R. Tapster et al., PRL 73, 1932 (1994)

W. Tittel et al., PRL 81, 3563 (1997)

closing (some) loopholes



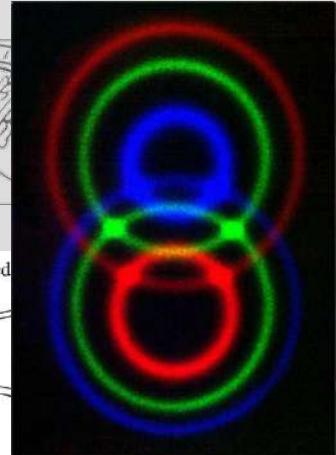
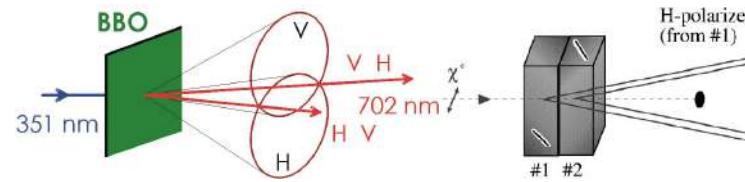
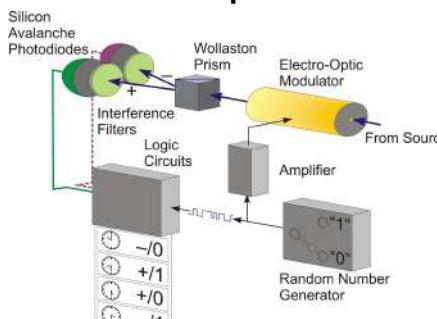
new methods:

- polarization entanglement (Kwiat)
- quantum logic gates

Weihs (Innsbruck):

locality loophole

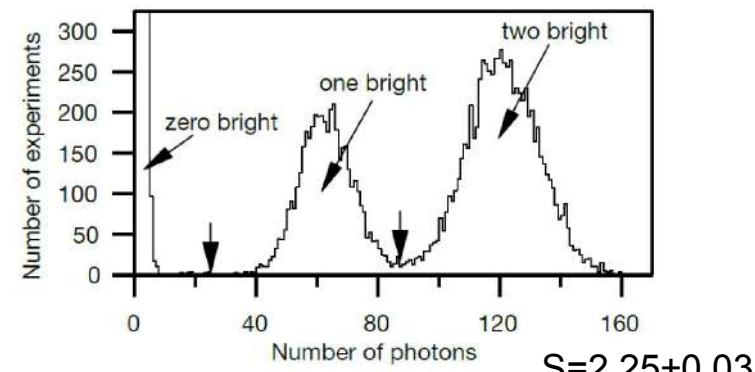
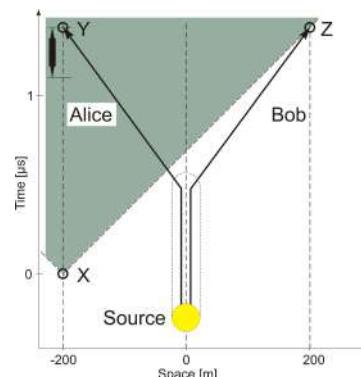
- quantum random numbers
- fast electro-optic switches
- independent data recording
- 400 m line-of-sight
- ~5% of pairs detected



Rowe (Boulder):

detection loophole

- entangled ions (!)
- using quantum logic gates
- unit detection efficiency
- ions are detected without distinguishing them



G. Weihs et al., PRL 81, 5039 (1998)

M.A. Rowe et al., Nature 409, 791 (2001)

closing detection and locality loopholes

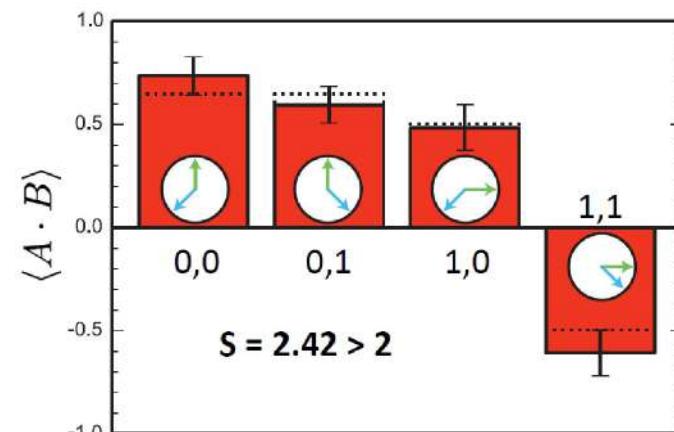
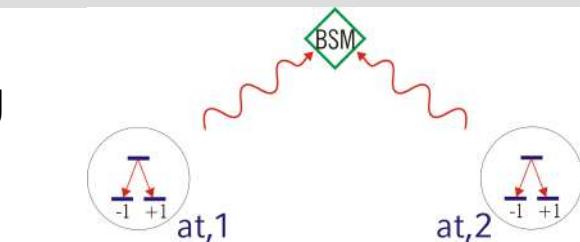
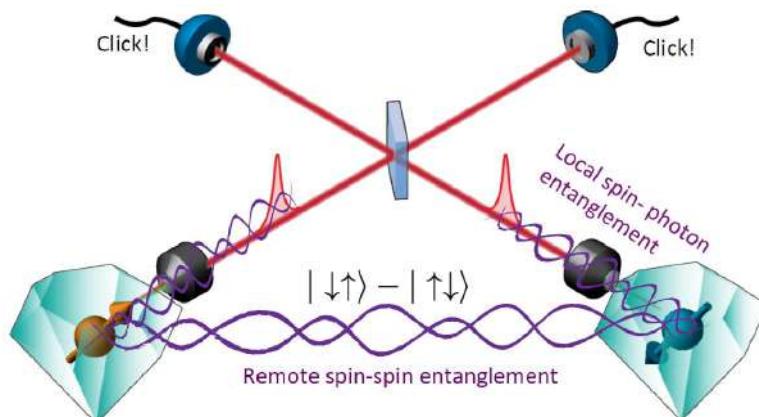
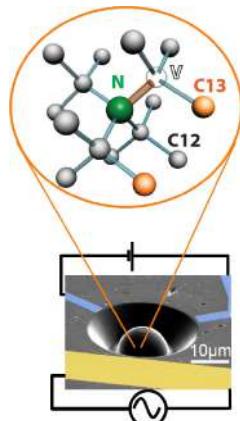


new methods:

- matter-light entanglement + entanglement swapping
- superconducting single-photon detectors

Hensen (Delft)

- NV-centers in diamond
- efficient preparation and readout



closing detection and locality loopholes



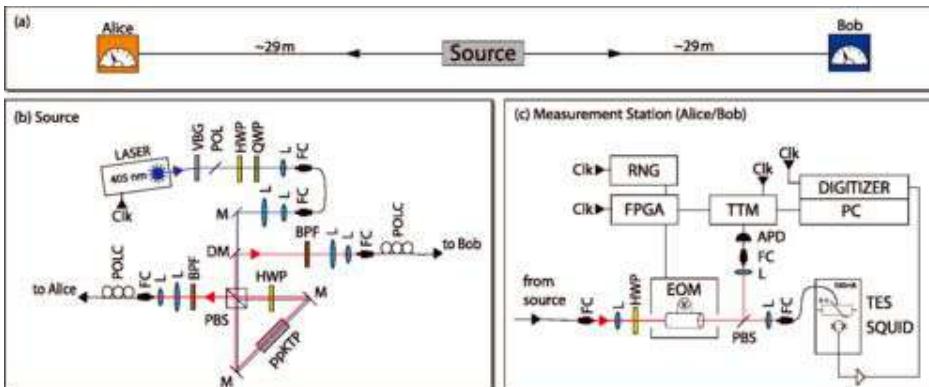
Eberhard inequality

- lower detection efficiency of 2/3 required for asymmetric entanglement

$$|\Psi\rangle = \frac{1}{\sqrt{1+r^2}} (|V\rangle_A |H\rangle_B + r |H\rangle_A |V\rangle_B)$$

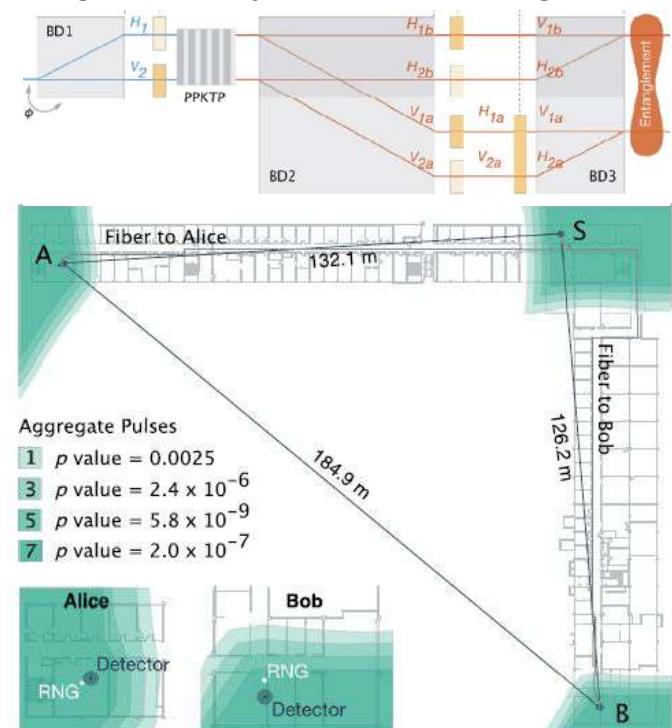
Giustina (Vienna)

- 60 m in the basement of the Hofburg



Shalm (Boulder)

- high fidelity source design



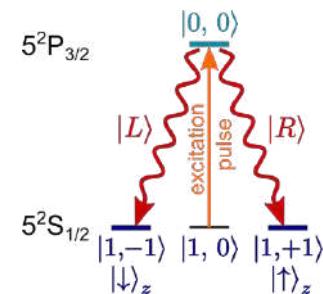
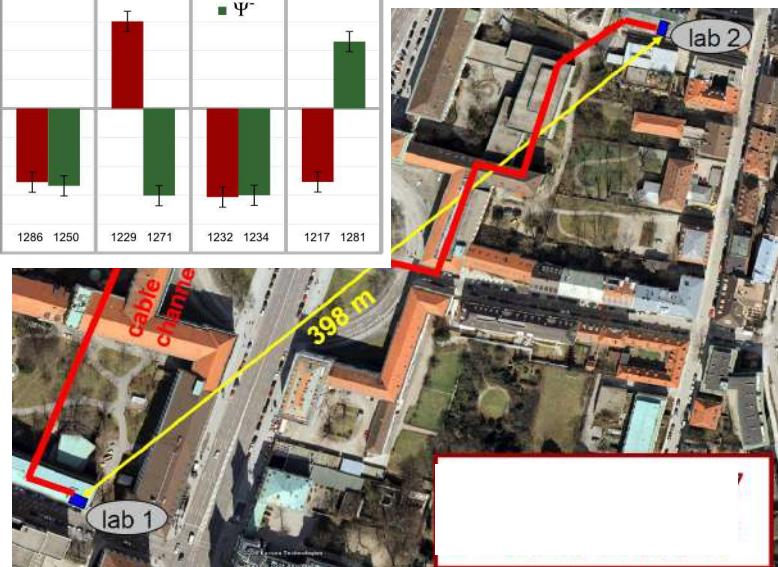
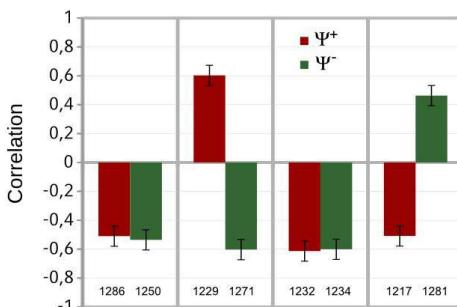
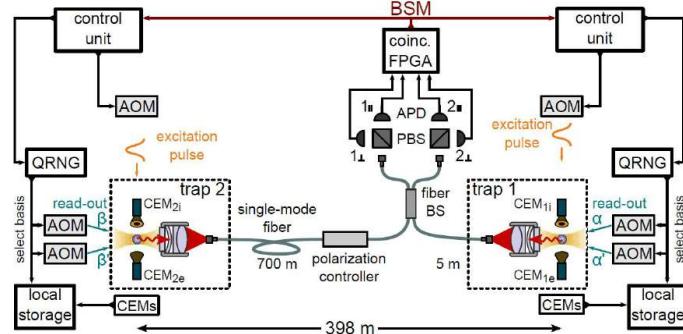
M. Giustina et al., PRL 115, 250401 (2015)
L.K. Shalm et al., PRL 115, 250402 (2015)

closing detection and locality loopholes



Rosenfeld (Munich)

- atom-atom entanglement
over 400 m, $\sim 1\mu\text{s}$ for measurement

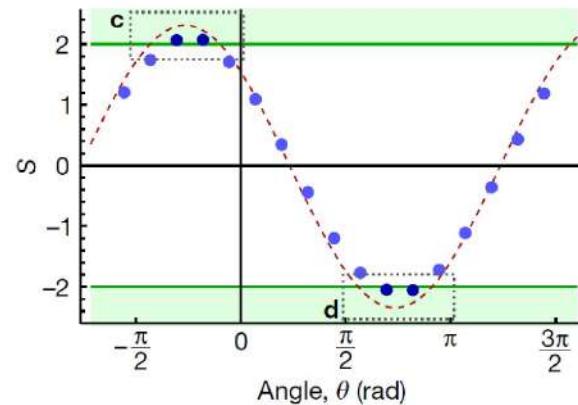


Storz (Zürich)

- superconducting qubits, 30 m
- entanglement via absorption of μ -wave photon entangled with first qubit



$$S = 2.0747 \pm 0.0033$$



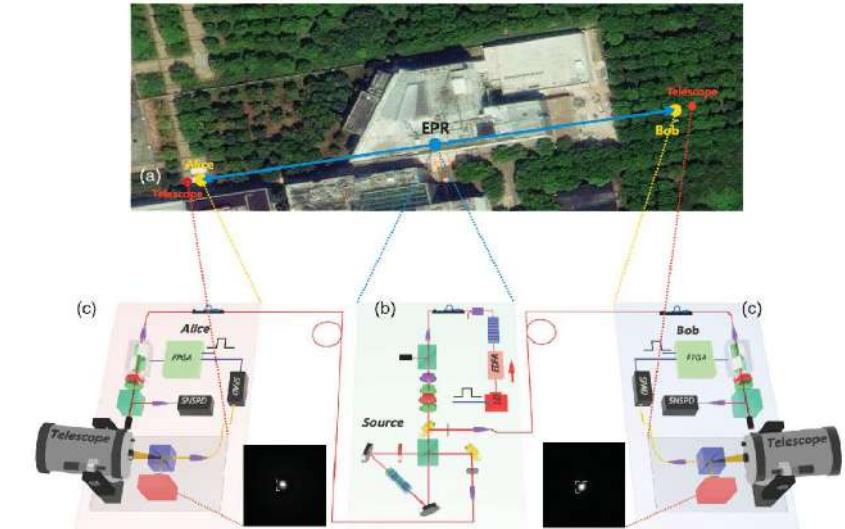
W. Rosenfeld et al., PRL 119, 010402 (2017)
S. Storz et al., Nature 617, 215 (2023)

freedom-of-choice



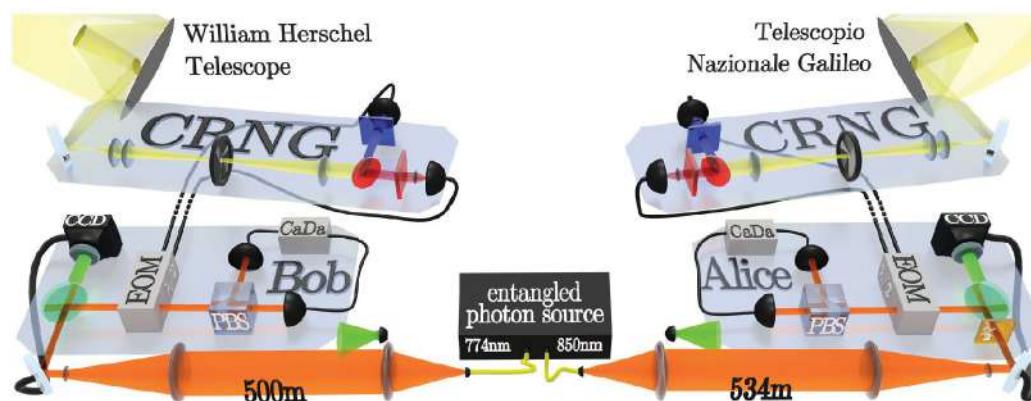
Li (Shanghai)

- 2-photon experiment closing detection and locality loophole
- random numbers according to detection of photons from stars
- $\tau_{AB} \gtrsim 100$ y



Rauch (Vienna)

- random numbers according to **colours** of photons emitted from distant quasars
- 12.2 Gyr & 7.8 Gyr
- locality loophole closed



Future ?



Student labs

- SPDC + single photon detectors
comerzialized

alternative tests

- continous variables
- All versus Nothing – tests
GHZ, Hardy,...

network tests

- multi-party
- topology
- signaling

...



From Foundations to Quantum Networks

Wei Zhang

Tim van Leent

Florian Fertig

Robert Garthof

Yiru Zhou

Pooja Malik

Anastasia Reinl

Kai Redeker

Daniel Burchardt

Sebastian Eppelt

Norbert Ortegel

Markus Rau

Mathias Seubert

Derya Taray

René Schwonnek

Valerio Scarani

Charles C.-W. Lim



her

NV-center

B. Hensen et al., Nature, 526, 682 (2015))

Photons

M. Giustina et al., PRL 115, 250401 (2015)

K. Shalm et al., PRL 115, 250402 (2015)

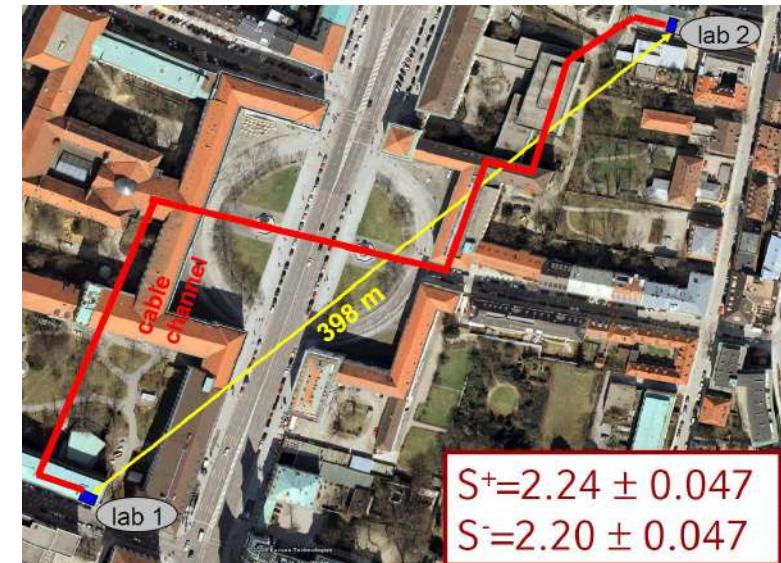
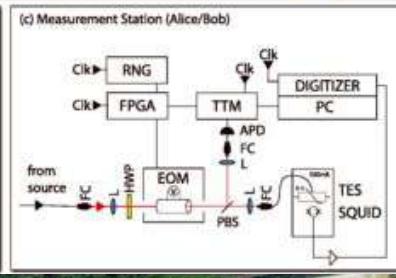
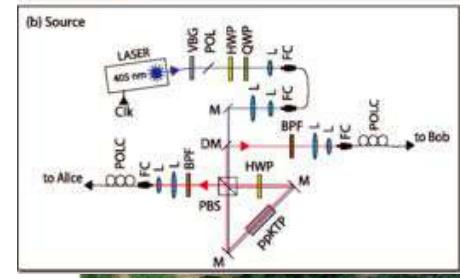
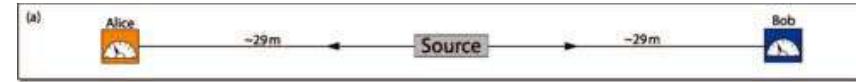
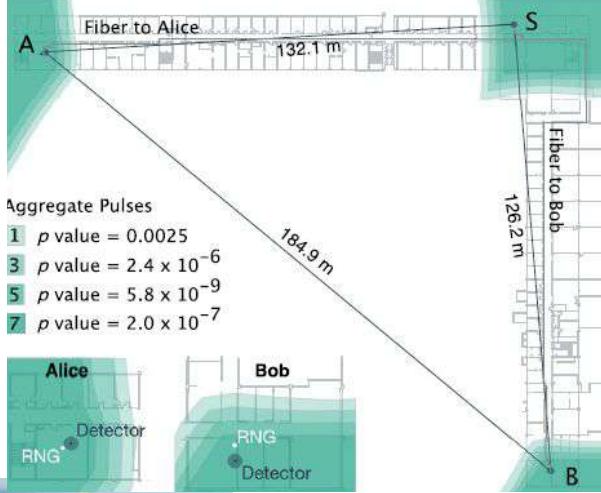
M-H Li et al., PRL 121, 080404 (2018)

sc-qubits

S. Storz et al., Nature volume 617, 265 (2023)

Rb-atoms

W. Rosenfeld et al., PRL 119, 010402 (2017)





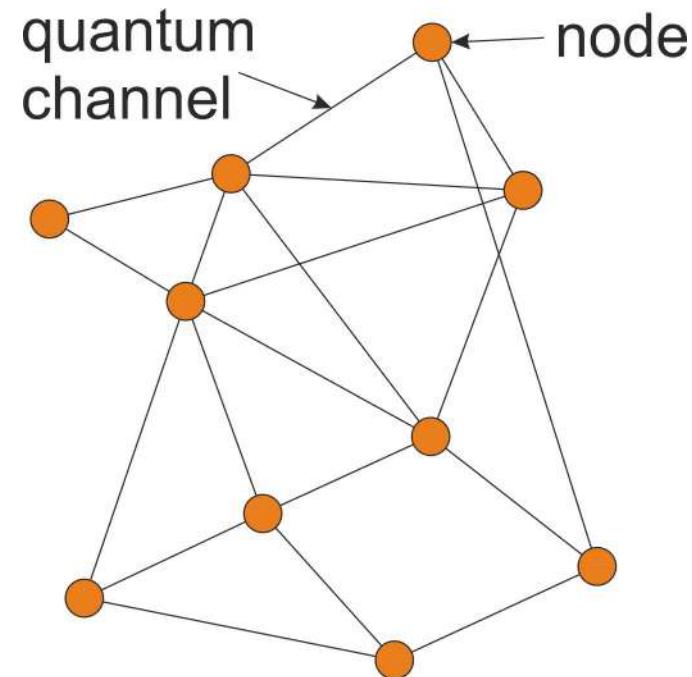
quantum networks ?

Bell-experiment

long distance

high fidelity

device independence





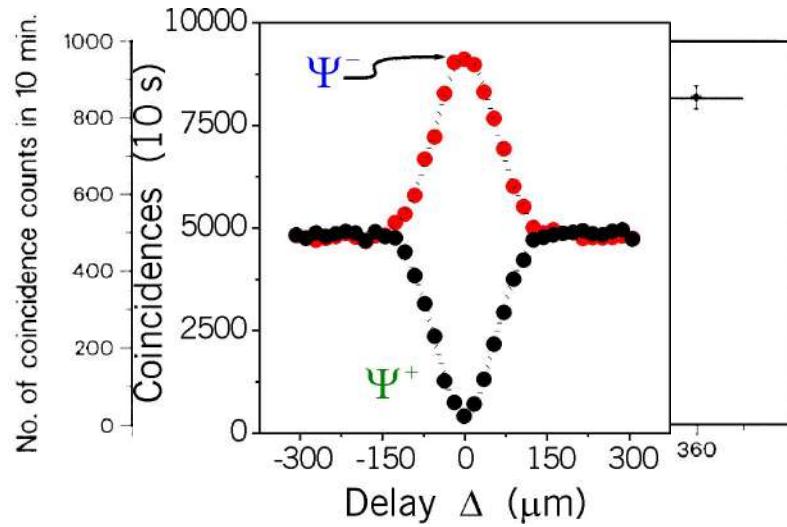
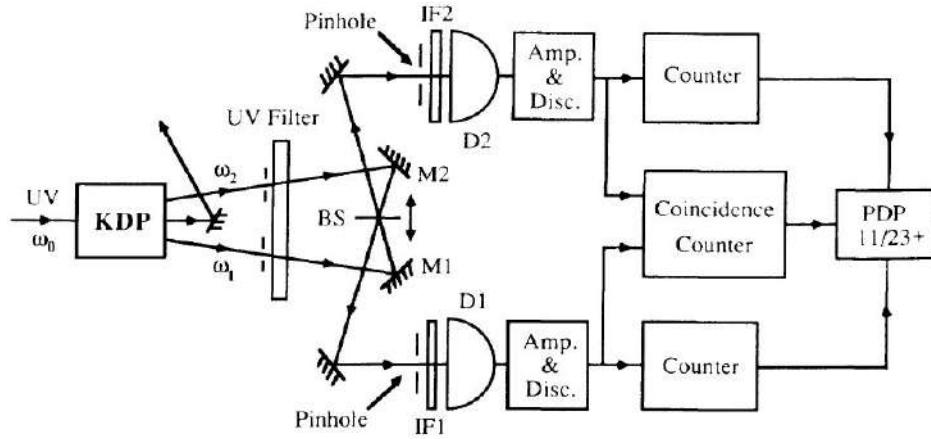
Measurement of Subpicosecond Time Intervals between Two Photons by Interference

C. K. Hong, Z. Y. Ou, and L. Mandel

Department of Physics and Astronomy, University of Rochester, Rochester, New York 14627

(Received 10 July 1987)

A fourth-order interference technique has been used to measure the time intervals between two photons, and by implication the length of the photon wave packet, produced in the process of parametric down-conversion. The width of the time-interval distribution, which is largely determined by an interference filter, is found to be about 100 fs, with an accuracy that could, in principle, be less than 1 fs.





MAY 15, 1935

PHYSICAL REVIEW

VOLUME 47

Can Quantum-Mechanical Description of Physical Reality Be Considered Complete?

A. EINSTEIN, B. PODOLSKY AND N. ROSEN, *Institute for Advanced Study, Princeton, New Jersey*

(Received March 25, 1935)

In a complete theory there is an element corresponding to each **element of reality**. A sufficient condition for the reality of a physical quantity is the possibility of predicting it with certainty, **without disturbing the system**. In quantum mechanics in the case of two physical quantities described by non-commuting operators, the knowledge of one precludes the knowledge of the other. Then either (1) the description of reality given by the wave function in

quantum mechanics is not complete or (2) these two quantities cannot have simultaneous reality. Consideration of the problem of making predictions concerning a system on the basis of measurements made on another system that had previously interacted with it leads to the result that if (1) is false then (2) is also false. One is thus led to conclude that the description of reality as given by a wave function is not complete.

Bell's theorem



MAY 15, 1935

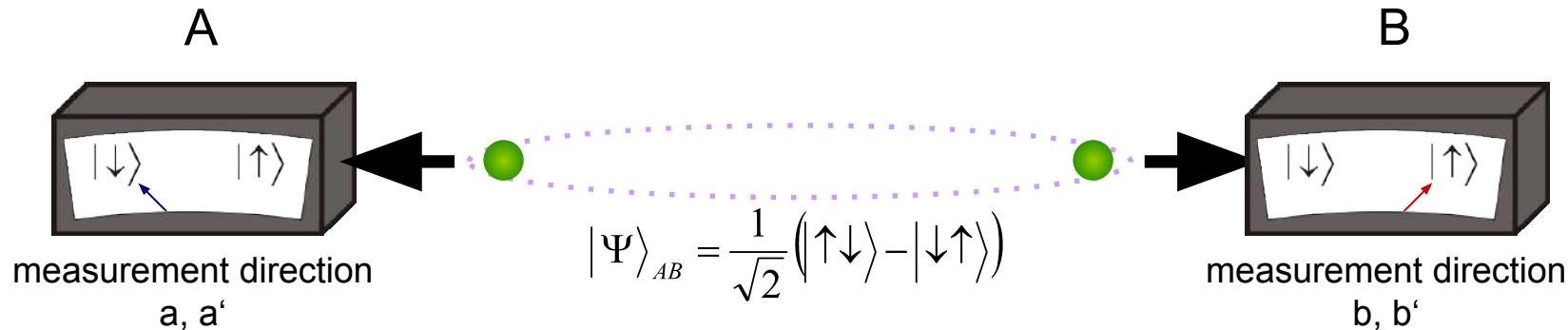
PHYSICAL REVIEW

VOLUME 47

Can Quantum-Mechanical Description of Physical Reality Be Considered Complete?

A. EINSTEIN, B. PODOLSKY AND N. ROSEN, *Institute for Advanced Study, Princeton, New Jersey*

(Received March 25, 1935)



Physics Vol. 1, No. 3, pp. 195–200, 1964

ON THE EINSTEIN PODOLSKY ROSEN PARADOX*

J. S. BELL†

Department of Physics, University of Wisconsin, Madison, Wisconsin

local realistic theories: $|\langle S \rangle| \leq 2$

QM: $S = 2\sqrt{2}$

Bell's theorem



MAY 15, 1935

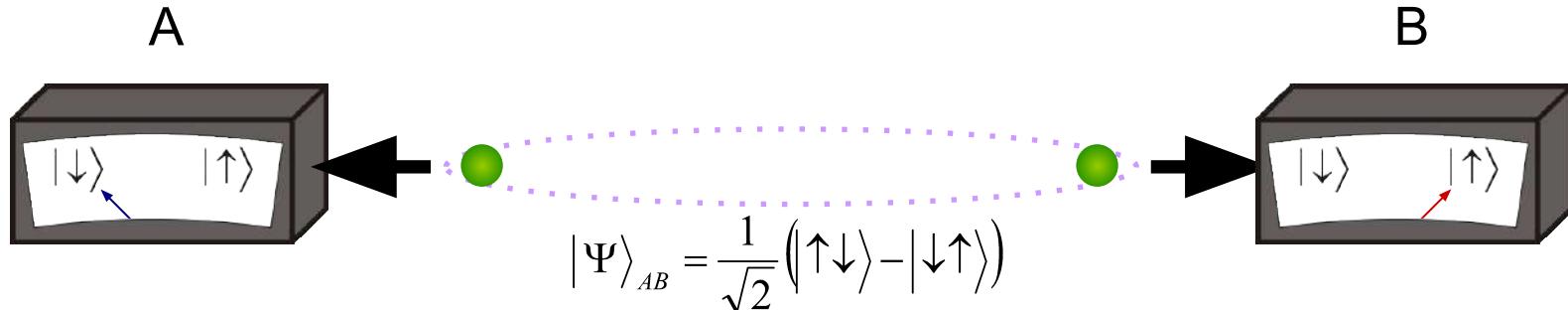
PHYSICAL REVIEW

VOLUME 47

Can Quantum-Mechanical Description of Physical Reality Be Considered Complete?

A. EINSTEIN, B. PODOLSKY AND N. ROSEN, *Institute for Advanced Study, Princeton, New Jersey*

(Received March 25, 1935)



Physics Vol. 1, No. 3, pp. 195–200, 1964

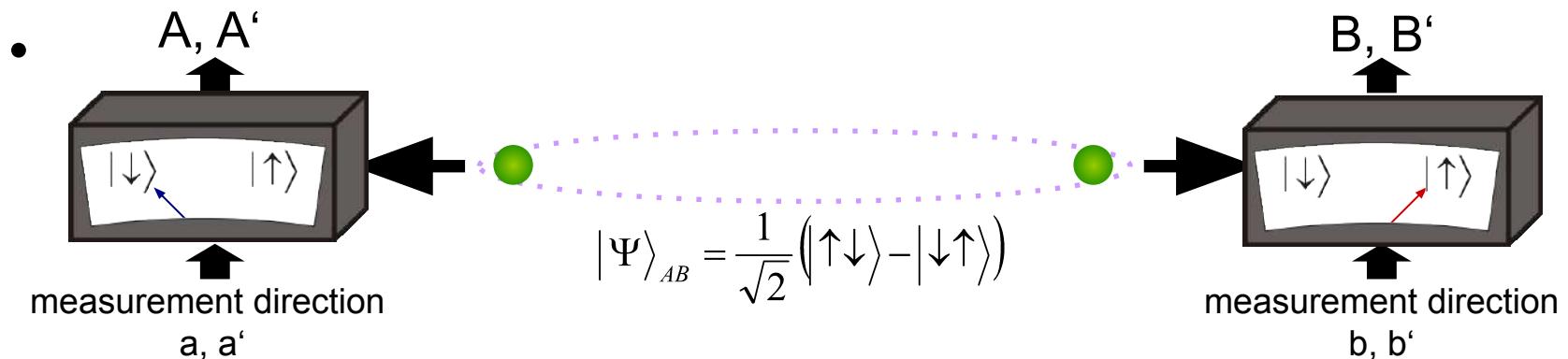
ON THE EINSTEIN PODOLSKY ROSEN PARADOX*

J. S. BELL†

Department of Physics, University of Wisconsin, Madison, Wisconsin

LHV: $S \leq 2$ QM: $S = 2\sqrt{2}$

a game



- Results $A, A', B, B' = +1$ or -1

→ evaluate expression

$$S = A * (B - B') + A' * (B + B')$$

gives in a single run:

$$S = \pm 2$$

→ average over many runs: $-2 \leq \langle S \rangle \leq +2$

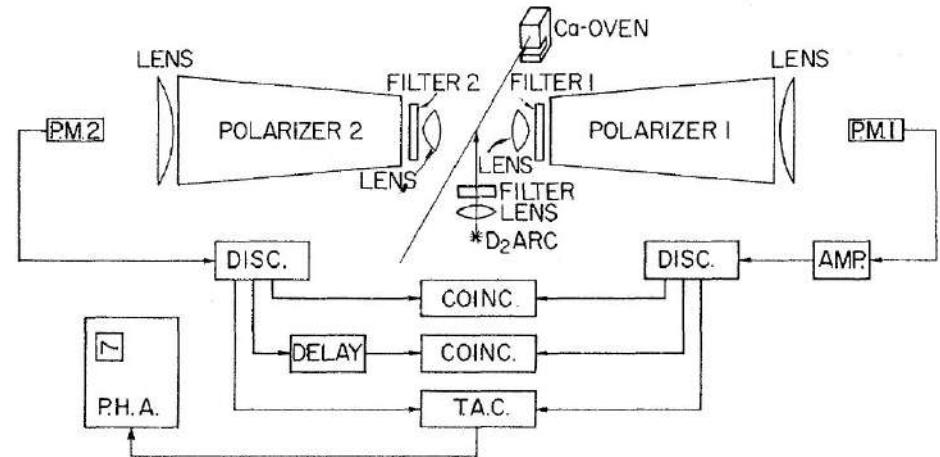
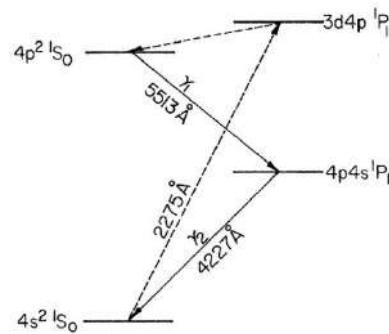
fulfilled by all local realistic theories

$QM: S = 2\sqrt{2}$

Bell tests: the starting point

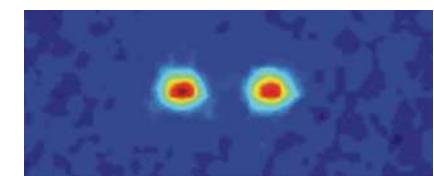


- Freedman, Clauser 1972

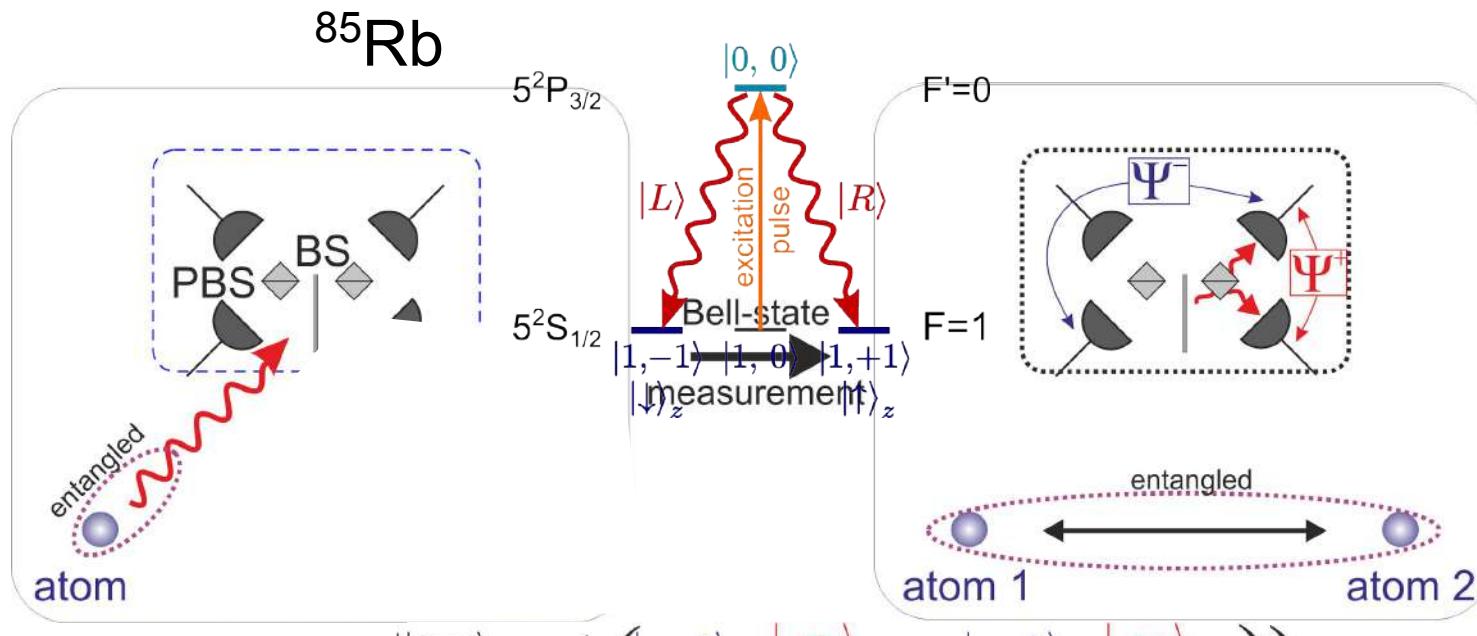


- loopholes: detection, locality

- Weihs et al. 1998:
independent observers
- Rowe et al. 2000 (Ch. Roos et al. 2004):
efficient detection of 2 entangled ions



starting point

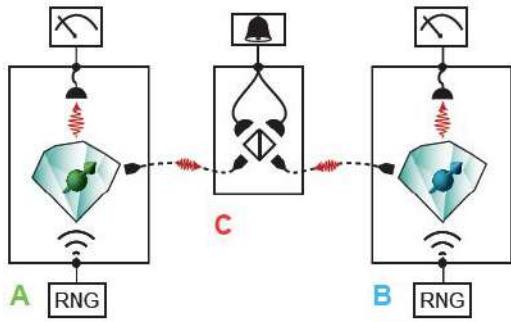


- entanglement between separated atoms
- heralded entanglement
- “event ready” Bell test
- quantum networks

other experiments

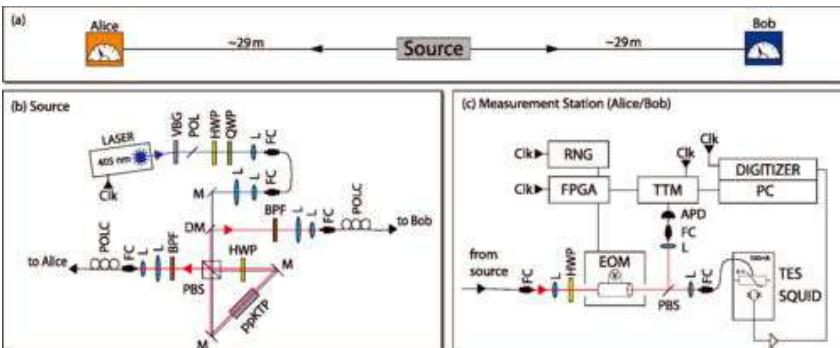


- NV-center (Delft, B. Hensen et al., Nature, **526**, 682 (2015))

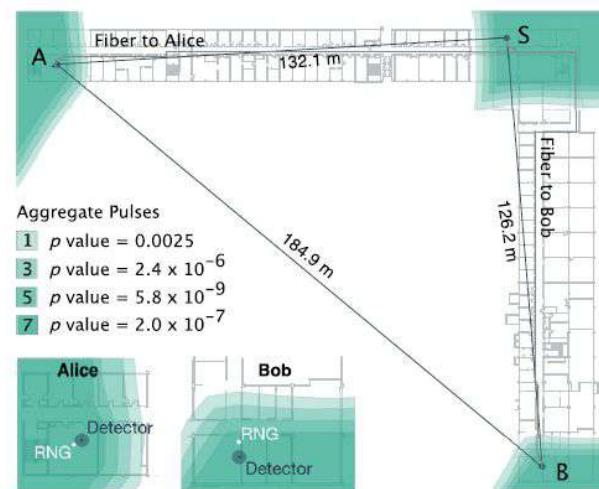


- Photons

Vienna, M. Giustina et al.,
PRL **115**, 250401 (2015)



Boulder, K. Shalm et al.,
PRL **115**,
250402
(2015)

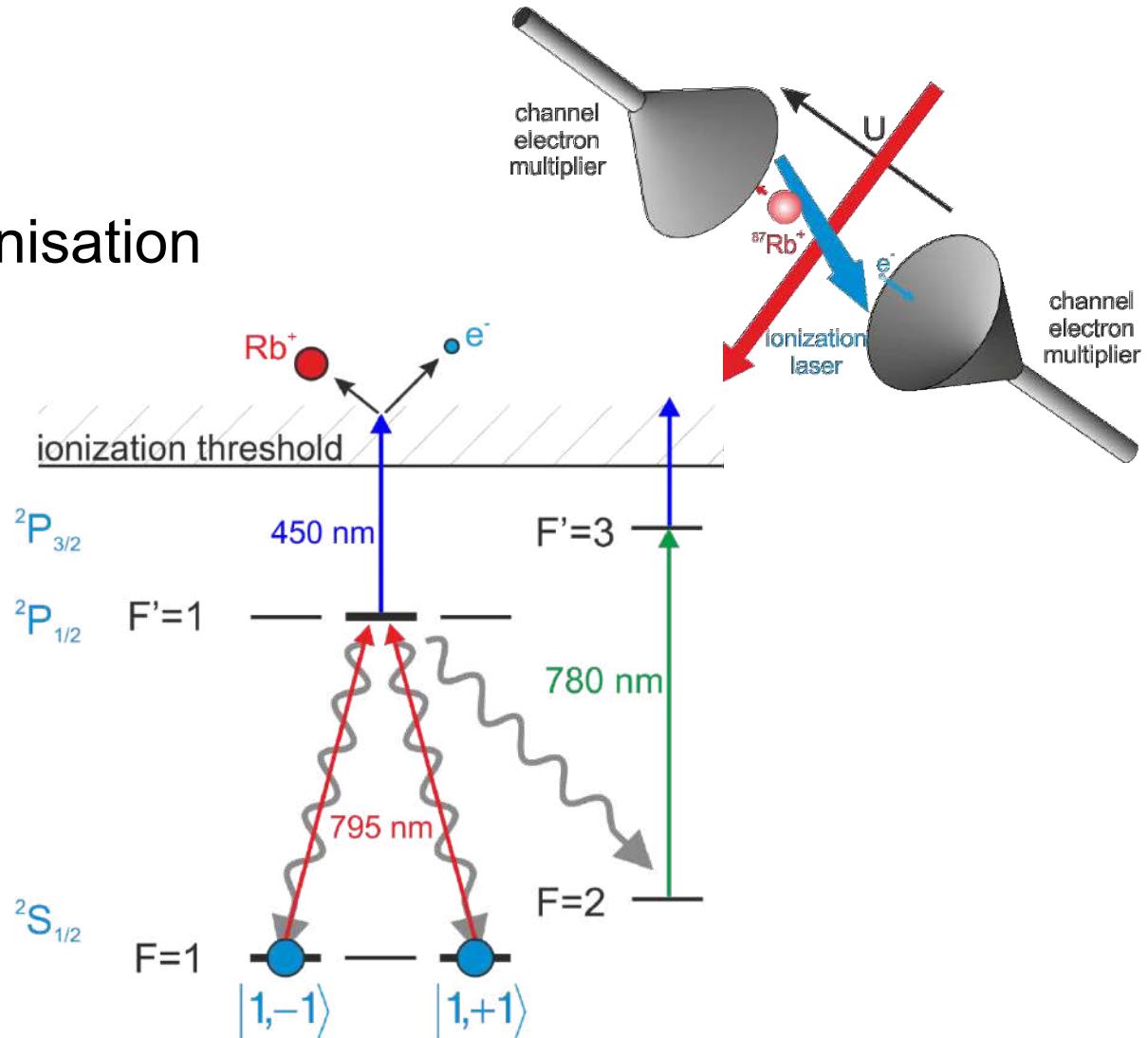


Hefei 2018

ETHZ (sc-qubits) 2023



- state selective ionisation

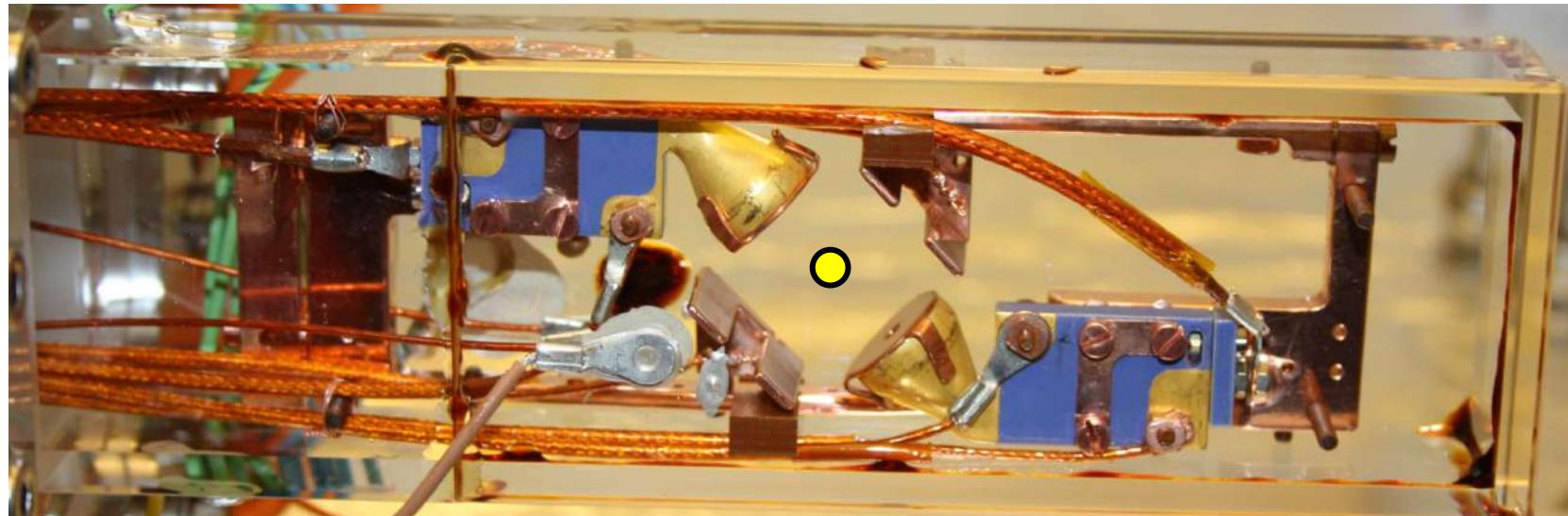
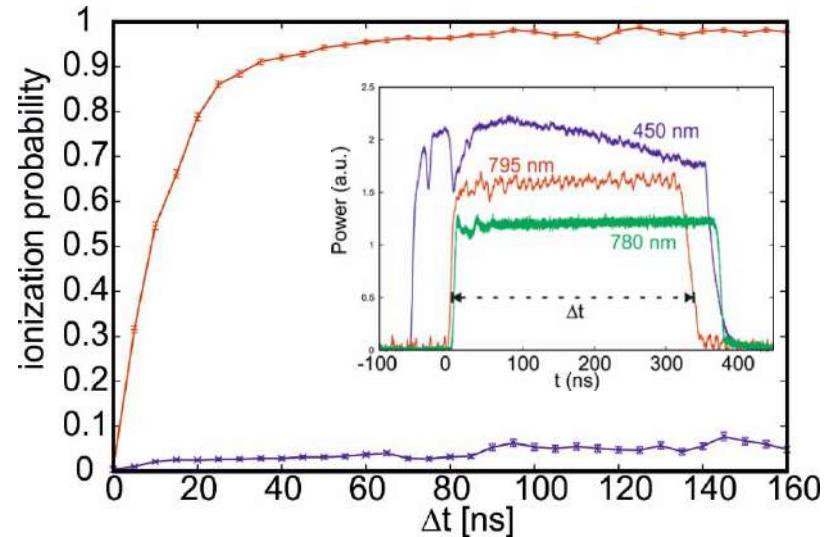


fast atomic state analysis



- ionisation

- $t = \sim 130 \text{ ns}$
- $F = 0.965$



time budget

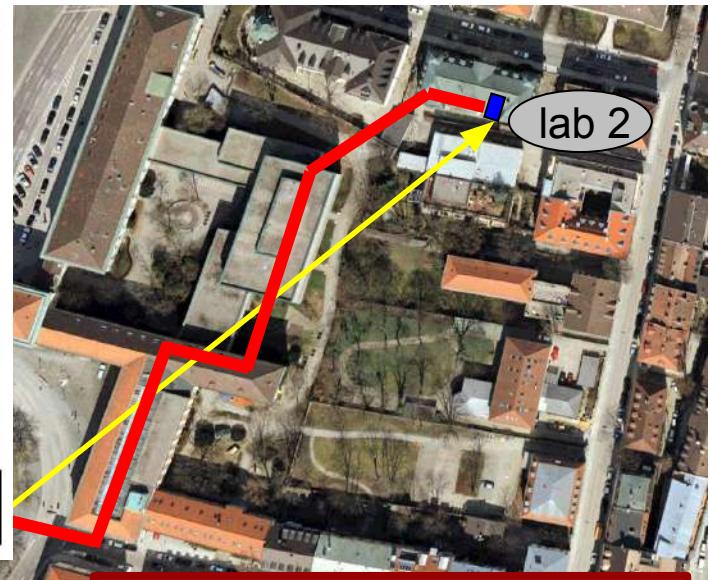
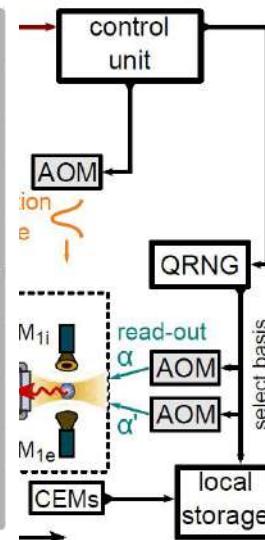
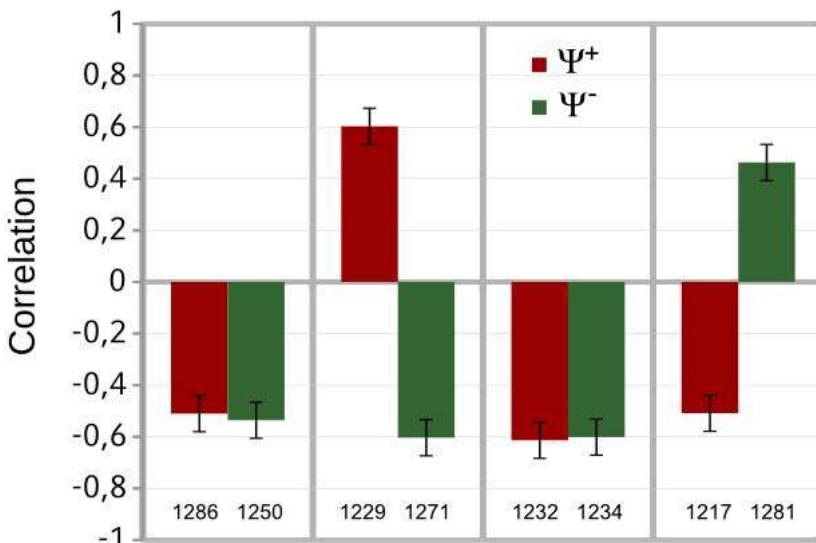


- random number via photon count
- trigger from Bell state measurement
- selection of meas with fast AOMs
- state selective io
- time of flight of ic fragments to det
- buildup of avalar electron multiplie
- detection logic o



$t < 1 \mu\text{s}$

atom – atom entanglement



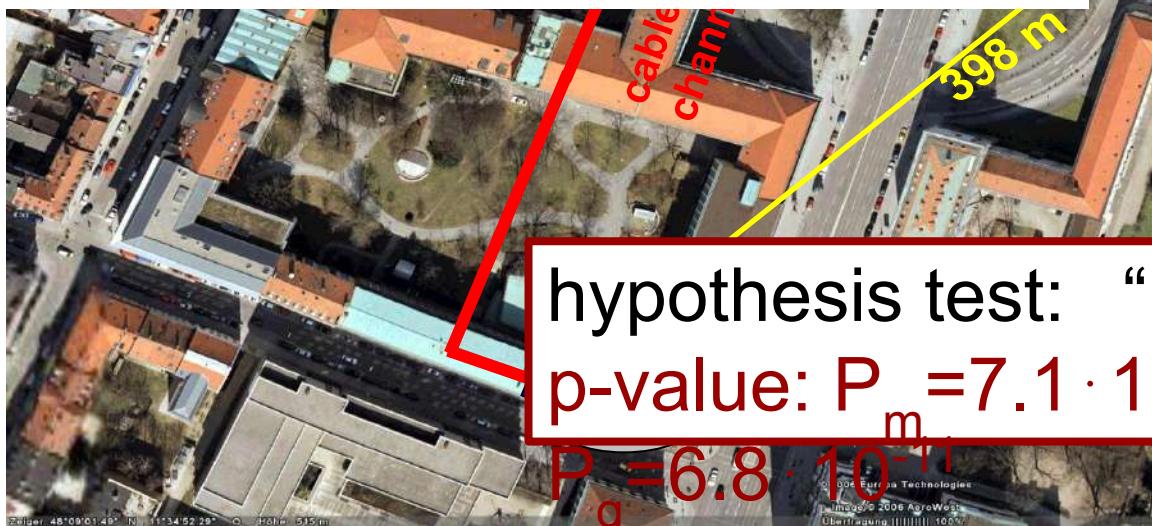
$$S^+ = 2.24 \pm 0.047$$

$$S^- = 2.20 \pm 0.047$$

hypothesis test: “LHV correct”

p-value: $P_m = 7.1 \cdot 10^{-10}$ /

$P_g = 6.8 \cdot 10^{-11}$



what is it good for?



Physics Vol. 1, No. 3, pp. 195–200, 1964

ON THE EINSTEIN PODOLSKY ROSEN PARADOX*

J. S. BELL[†]

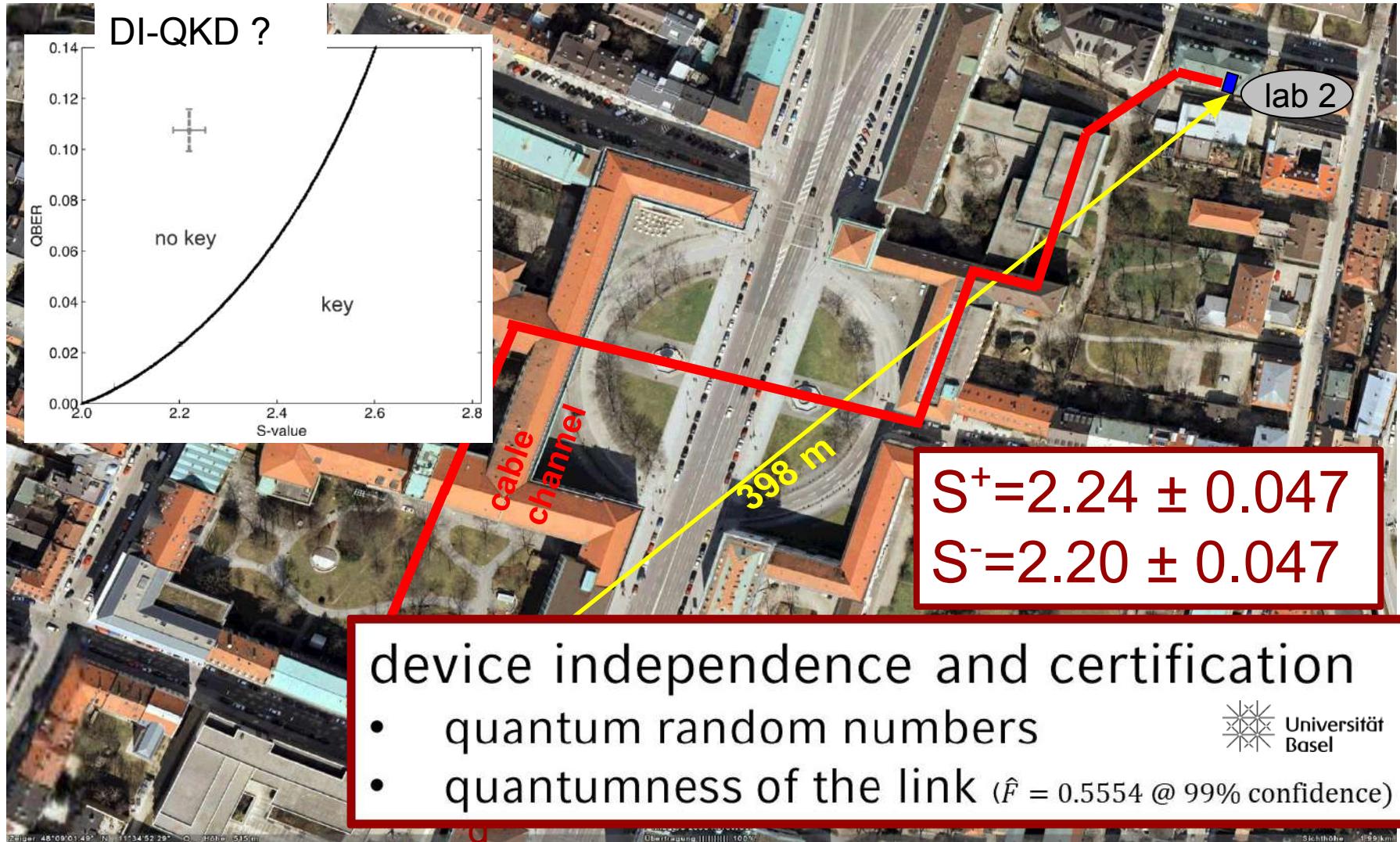
Department of Physics, University of Wisconsin, Madison, Wisconsin

test, whether Nature can be described by
a local, realistic theory

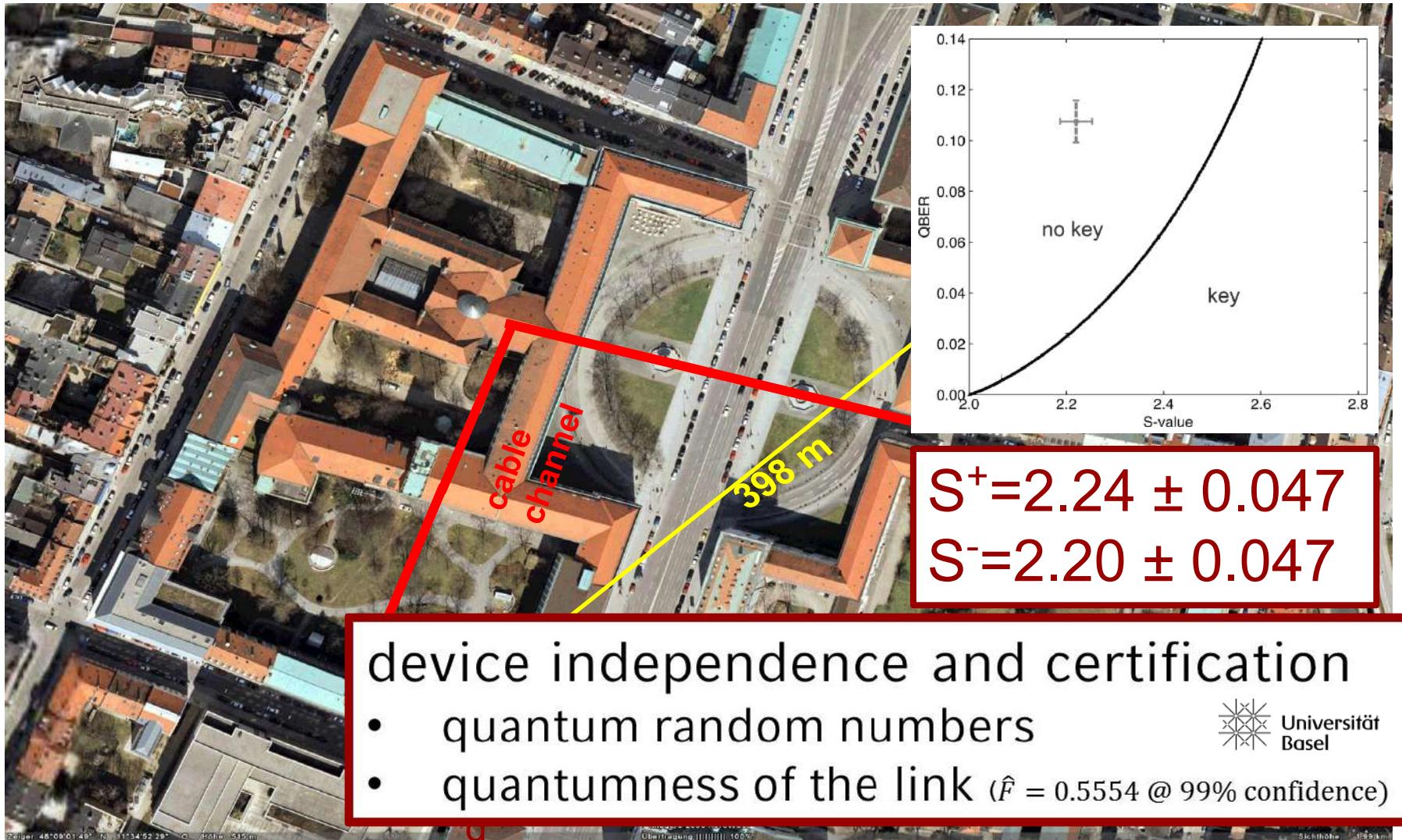
↔

test, whether knowledge about measurement results is
available locally

- entanglement based QKD
- quantum origin, fewer security assumptions
- NO trust or knowledge about the devices required



atom – atom entanglement

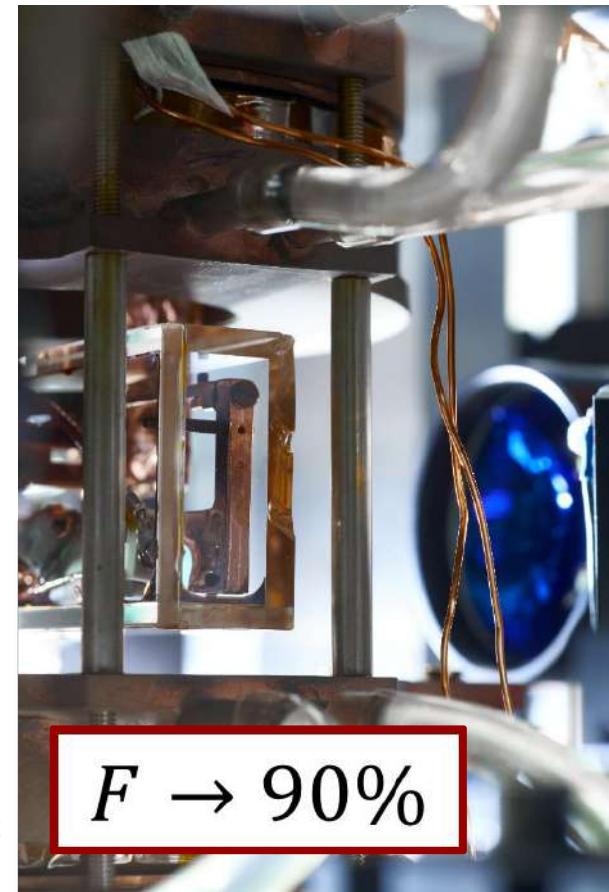
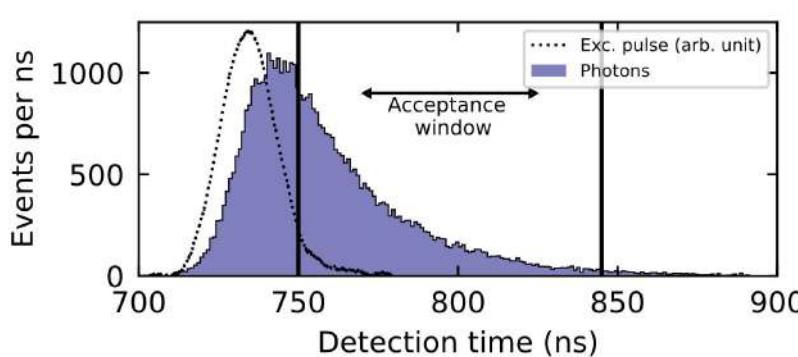
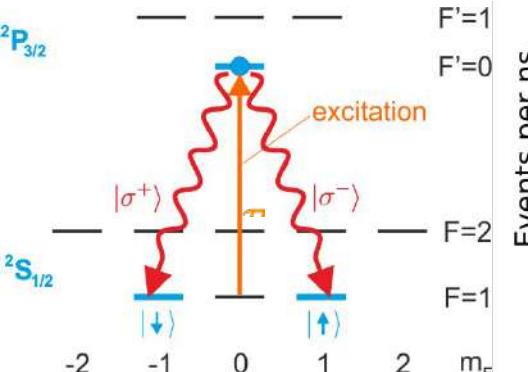


improvements



• experiment:

- new high-NA objectives:
 - better beam definition: less heating when atoms move
 - higher collection efficiency: higher rate
- magnetic fields
 - guiding field
 - lower trapping potential
- time selection
 - improve visibility of BSM

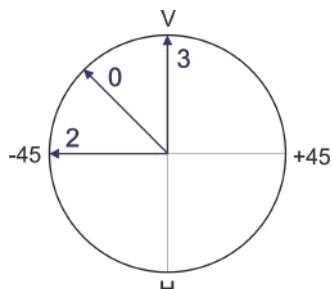


$F \rightarrow 90\%$

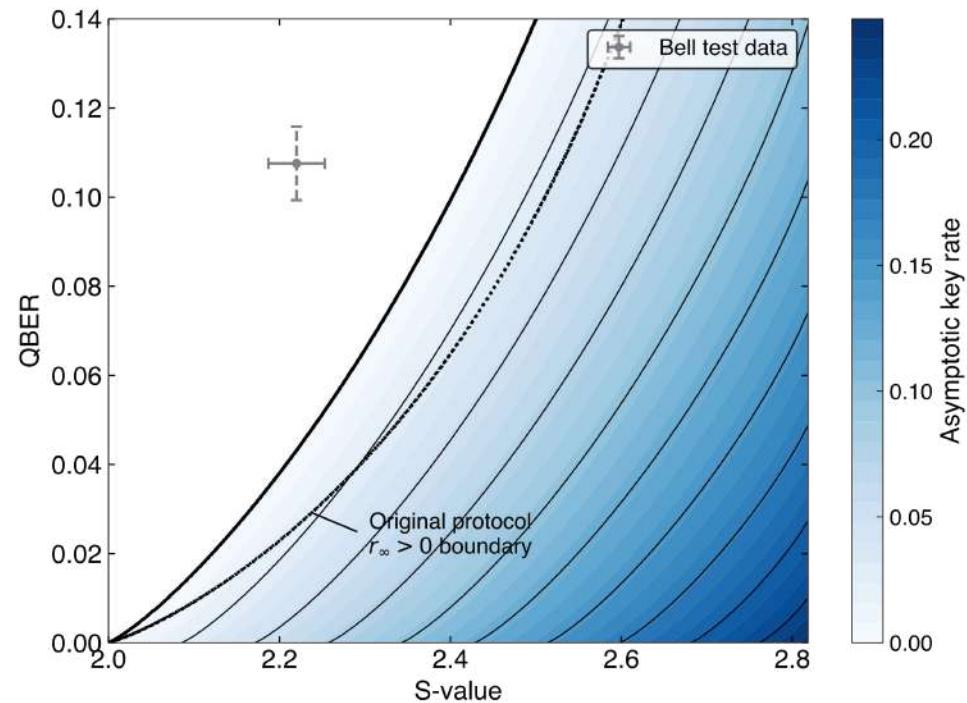
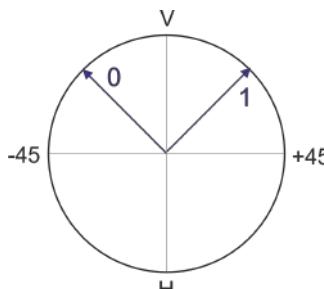


- noise tolerant protocol
 - two bases for key generation and QBER determination
- Bell test:
 - Alice $X=\{2, 3\}$
& Bob $Y=\{0, 1\}$
- Key exchange (Q):
 - Alice $X=\{0, 1\}$
& Bob $Y=\{0, 1\}$

Settings Alice (X)

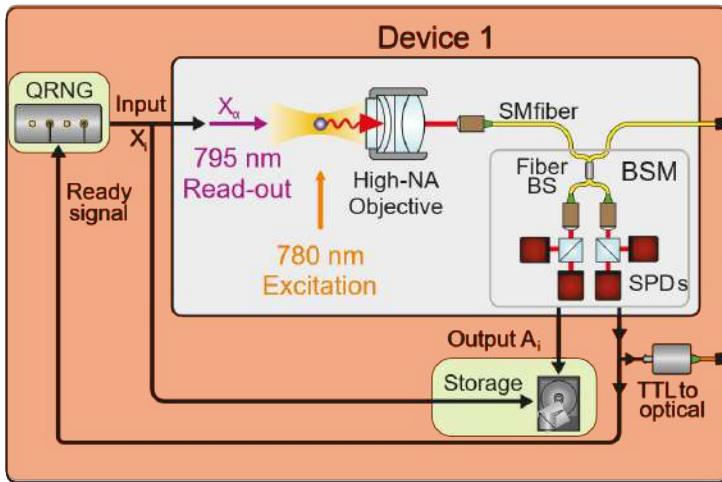


Settings Bob (Y)

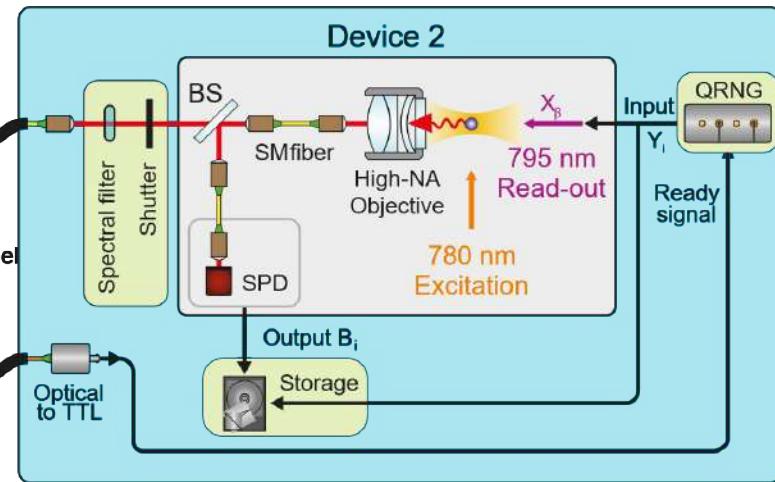




Alice (Lab 1)



Bob (Lab 2)



Alice's and Bob's equipment:

1. Single-atom trap
2. Bell-state measurement
3. QRNG
4. Trusted storage

- For Alice:

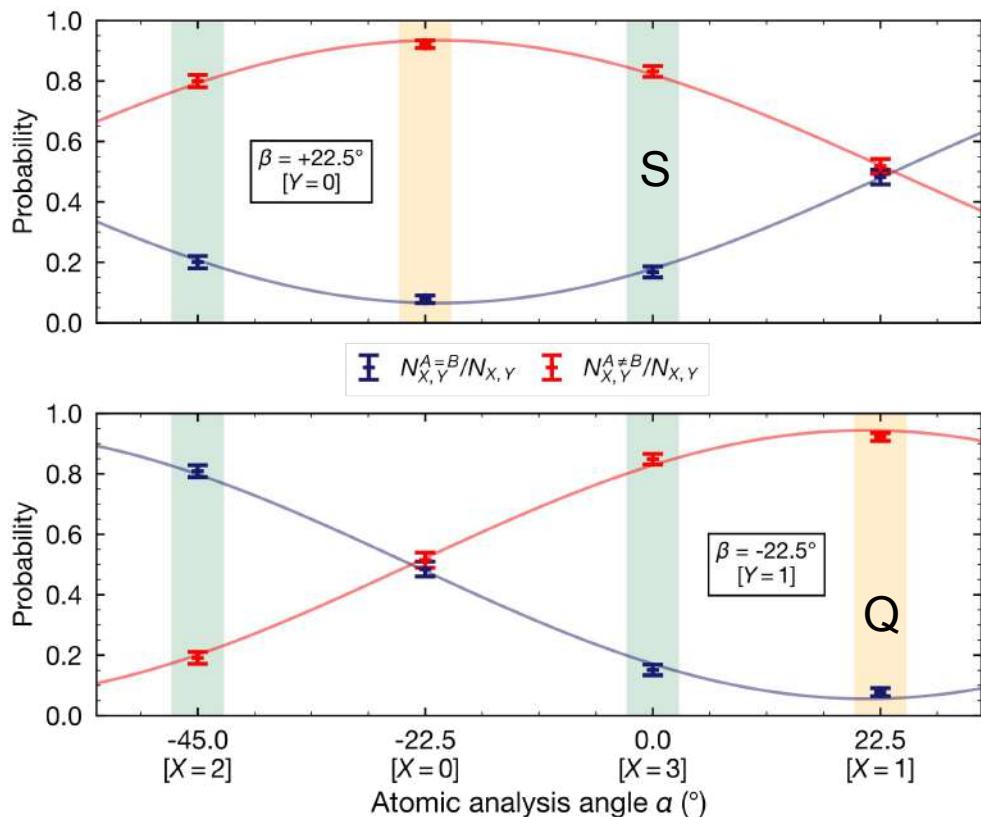
- BSM detectors used for fluorescence detection

- For Bob:

- Extra SPD installed for fluo. Detection
- Spectral filter and shutter to shield readout result and setting



$$|\Psi^+ \rangle = \frac{1}{\sqrt{2}}(|\uparrow\rangle|\downarrow\rangle + |\downarrow\rangle|\uparrow\rangle)$$



Number of rounds:

- N=3342 in 75 hours

Visibility fits:

- 0.869(25) & 0.888(45)

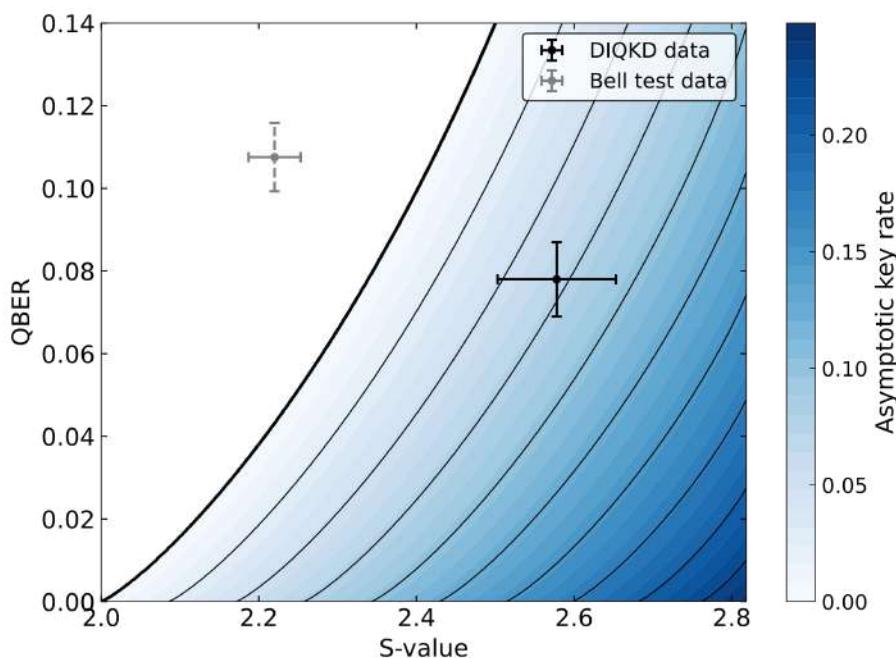
Fidelity:

- $\geq 0.892(12)$



performance

- asymptotic limit



Measurement outcome:

- $S = 2.578(75)$
- $Q_1 = 0.078(13)$
- $Q_2 = 0.078(13)$

Asymptotic key rate:

- $R=0.07$
per entanglement event
- $R>0$ with >99% confidence
(assuming Beta distributed errors)

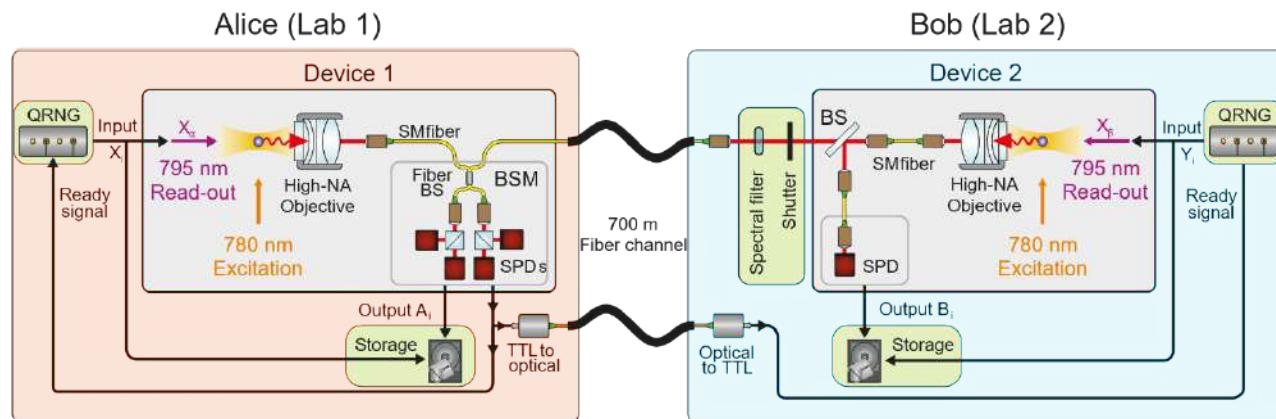
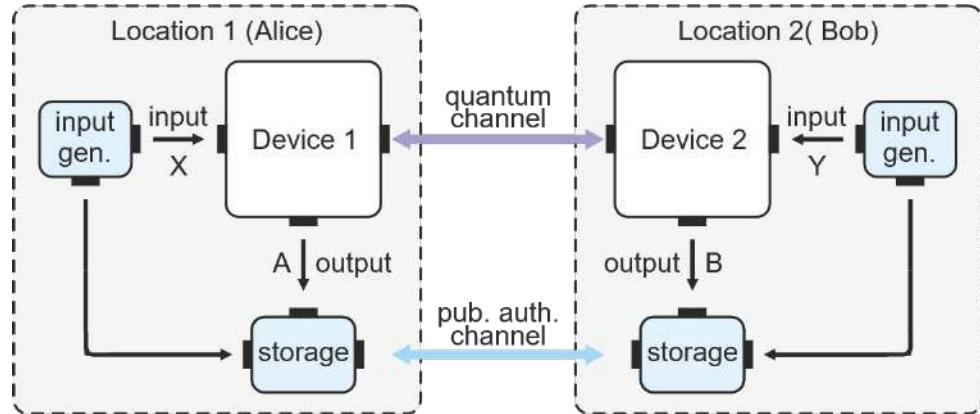
also at University of Oxford and USTC Hefei

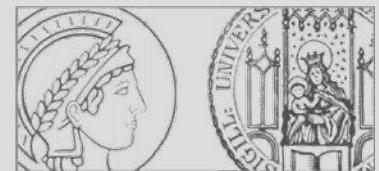
W. Zhang, et al., Nature **607**, 687 (2022)

DI-QKD



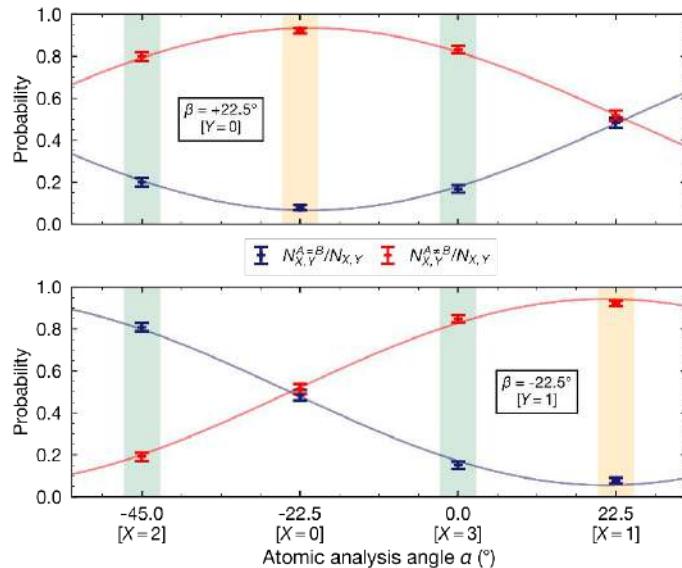
- device-independent
- QKD systems could be
 - uncharacterized
 - manipulated by producer
- Bell test: violation secrecy
 - efficient detection, no unauthorized communication



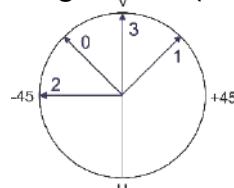


▪ More robust against noise with BB84 like settings

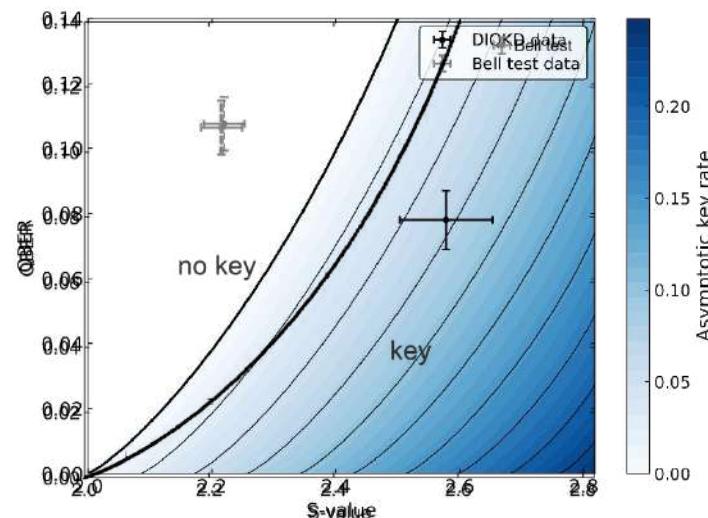
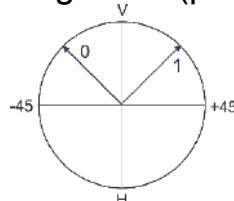
Schwonnek, et al., Nat Commun 12, 2880 (2021)



Settings Alice (α or X)



Settings Bob (β or Y)



Number of rounds:

- $N=3342$ in 75 hours

Visibility:

$>0.869(25)$

key (asymptotic limit):

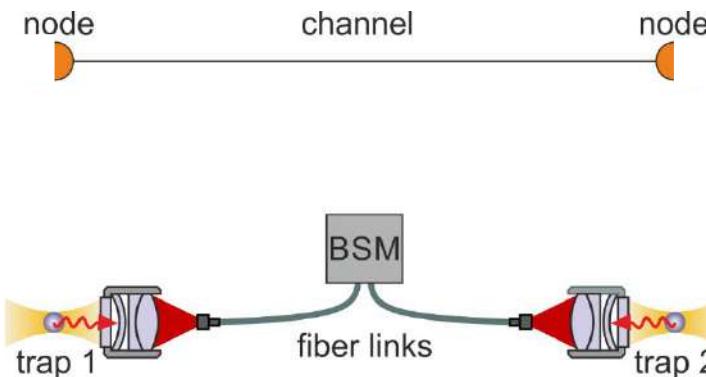
0.07 / 0.25 per event

also at University of Oxford and USTC Hefei

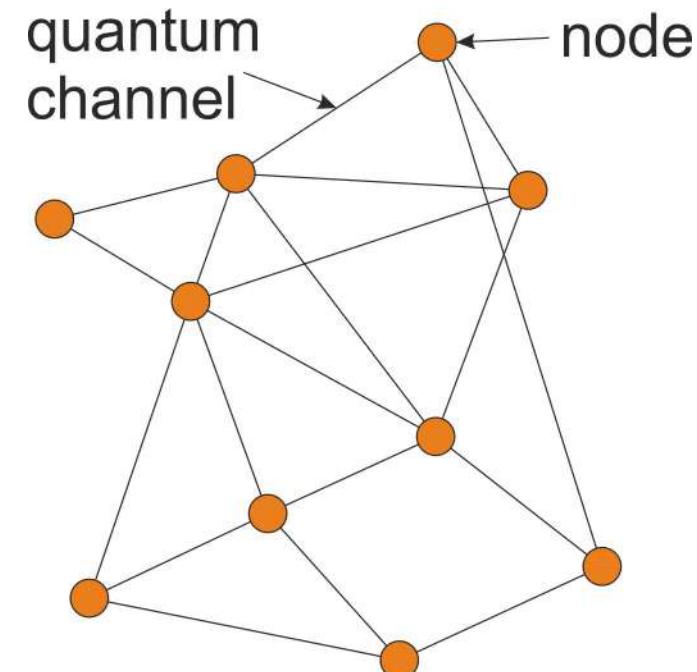
W. Zhang, et al., Nature 607, 687 (2022)



- a quantum link



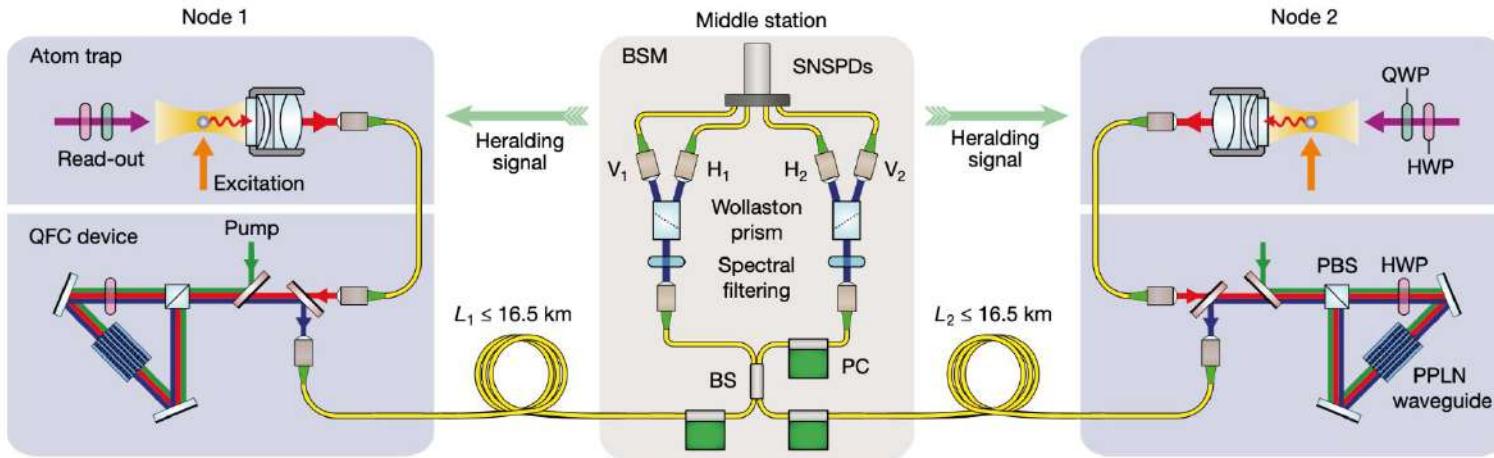
- local quantum system + photonic interface
- NV-centers
- quantum dots
- ensembles of colour centers or atoms ...
- Rb-Atoms



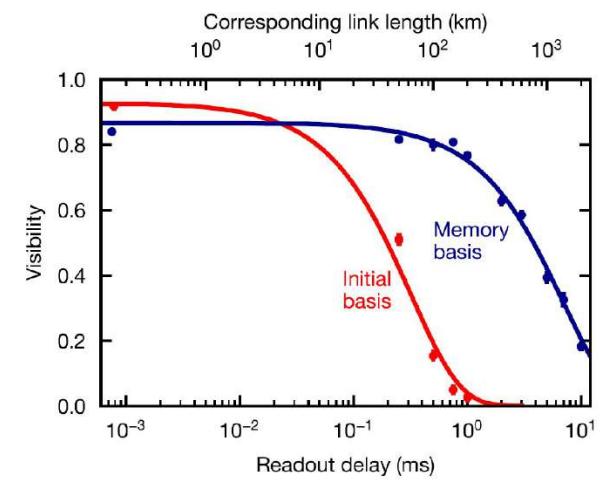
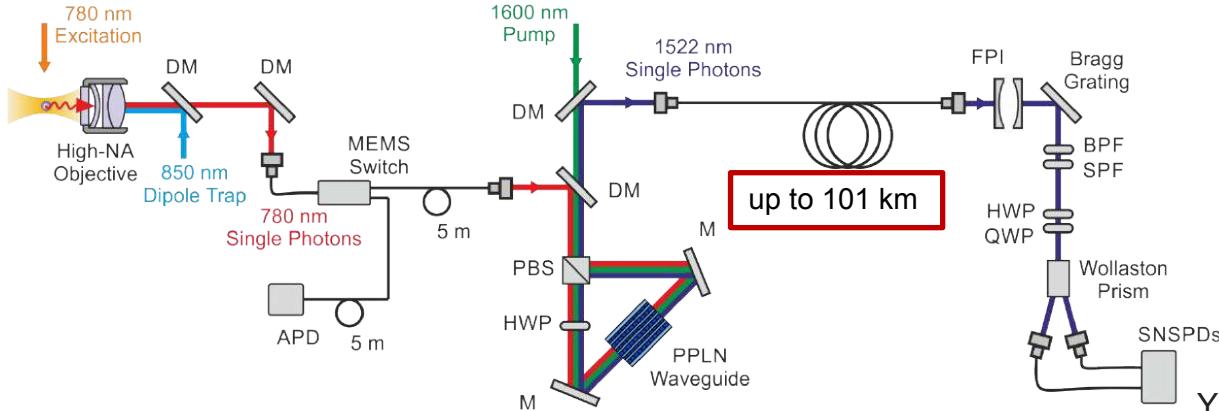
long-distance entanglement distribution



33 km glas fiber between nodes



101 km atom-photon entanglement

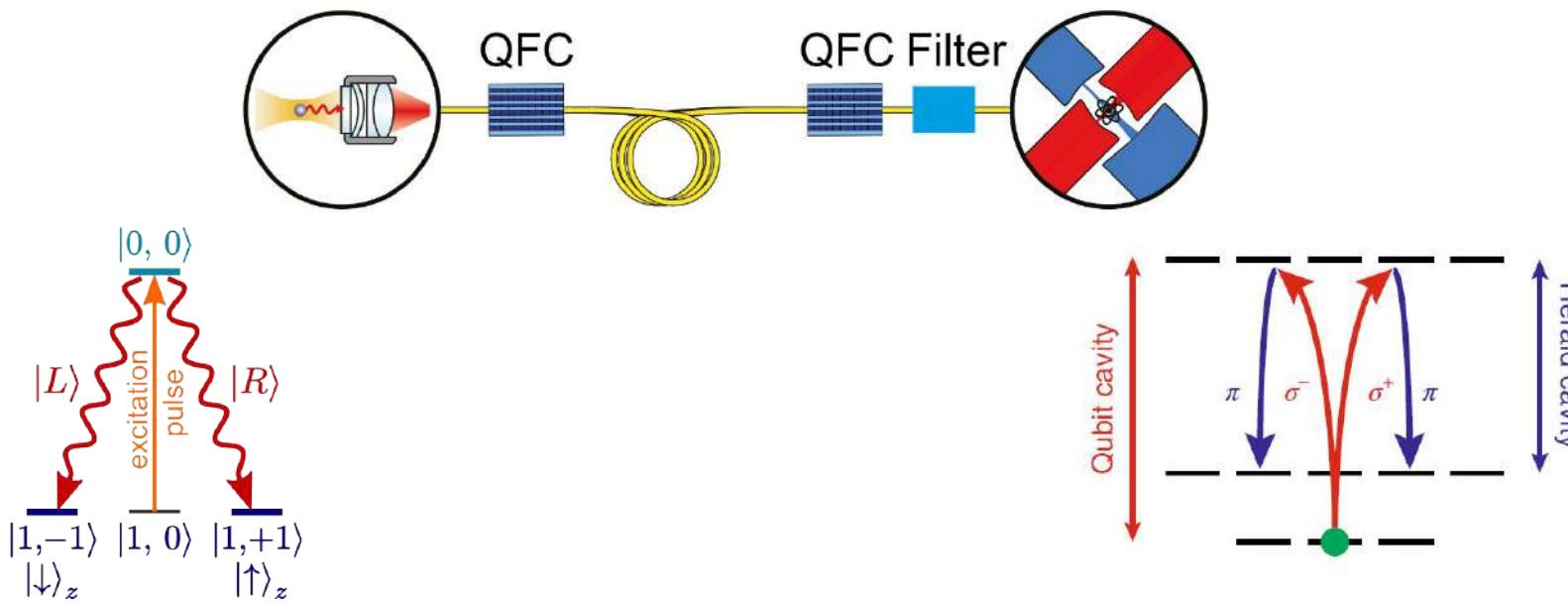


LMU-MPQ entanglement distribution



MAX-PLANCK-INSTITUT
FÜR QUANTENOPTIK

Tobias Frank
Gianvito
Chiarella
Maya Büki
Marvin Scholz
Pau Farrera
Gerhard Rempe



quantum networks?

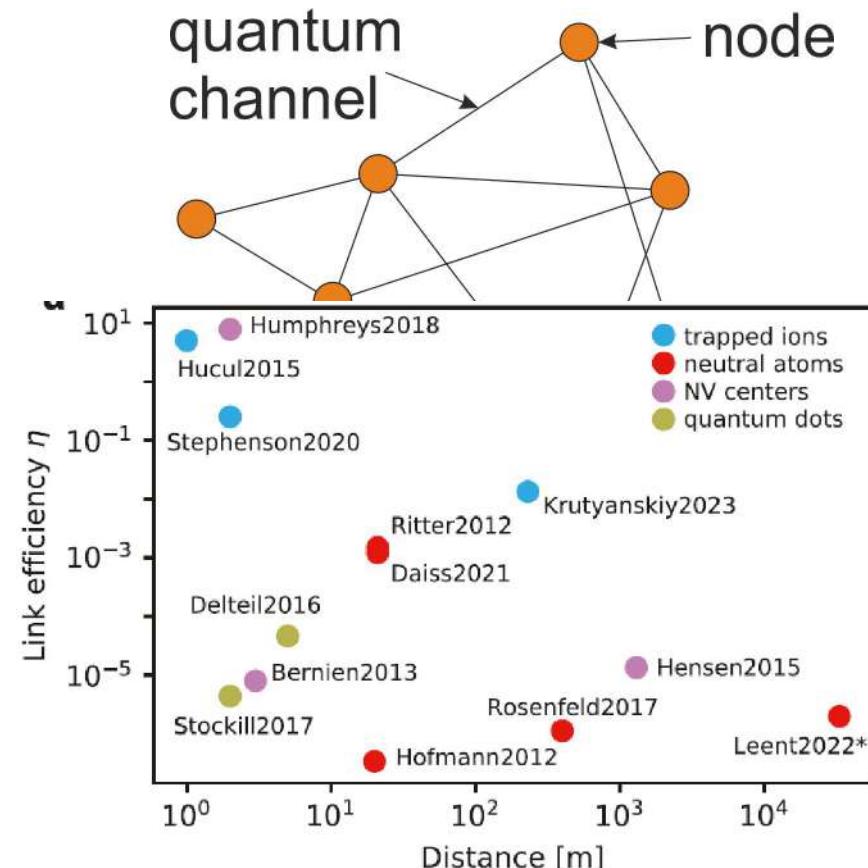


- quantum channel:
efficient distribution quantum repeater functionality

- quantum memory
- quantum logic operation
for entanglement purification
and Bell-state measurement

- quantum node:
 - provide entanglement at all times
 - one link:
link efficiency

$$\eta = \frac{\gamma_{ent}}{\gamma_{dec}} > 1$$

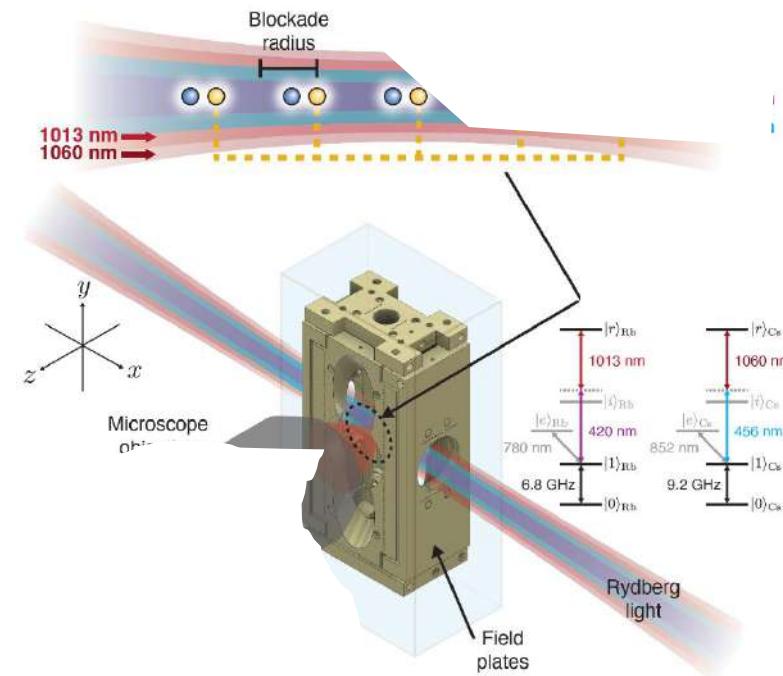
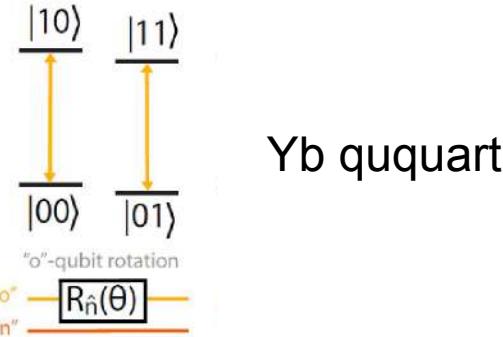


quantum networks?



$$\eta = \frac{\gamma_{ent}}{\gamma_{dec}} > 1$$

- quantum memories
 - quantum error correction
- neutral atom implementations:



Z. Jia et al., arXiv:2402.13134

S. Anand et al., arXiv:2401.10325

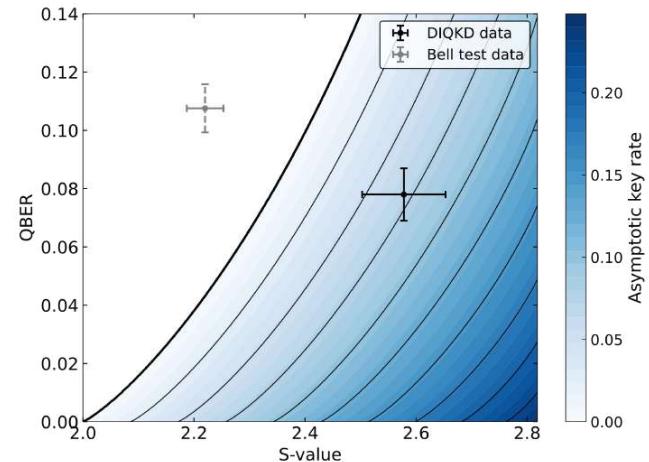
S.G. Menon et al., Nature Comm. **15**, 6156 (2024)

D. Bluvstein et al., Nature **626**, 58 (2024)

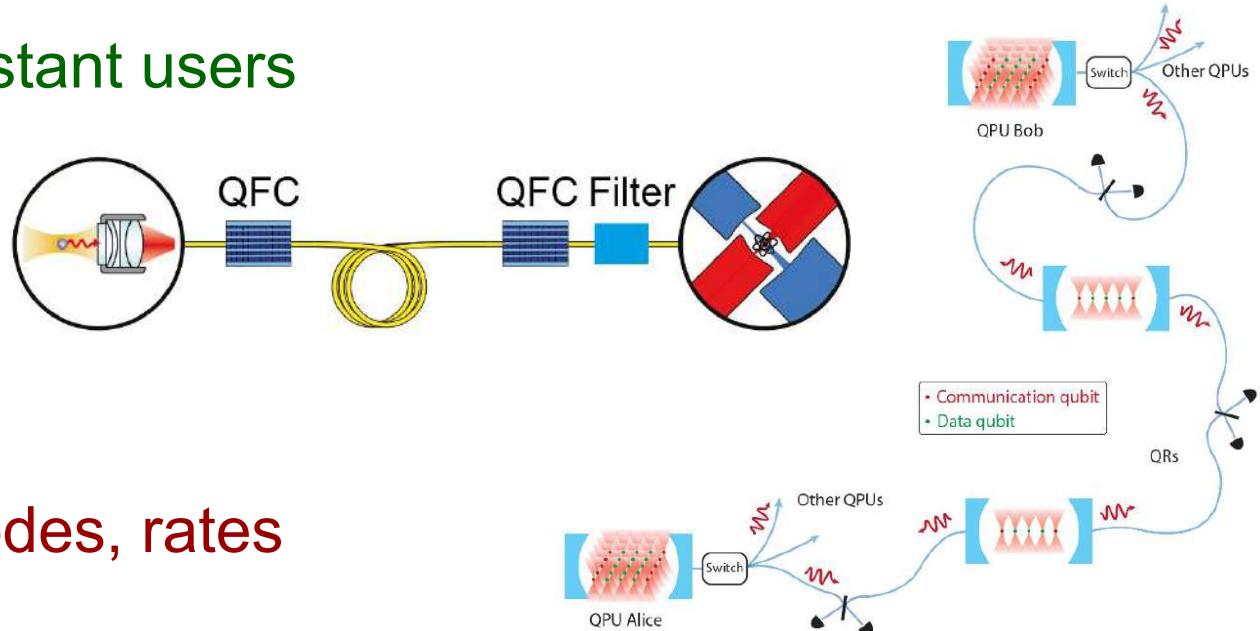
Summary



- Atom-Atom-Entanglement
 - atom-photon entanglement + entanglement swapping
- loophole free Bell-test



- DIQKD between distant users
- longer distances
- LMU-MPQ link



- quantum networks:
 - memory, local nodes, rates

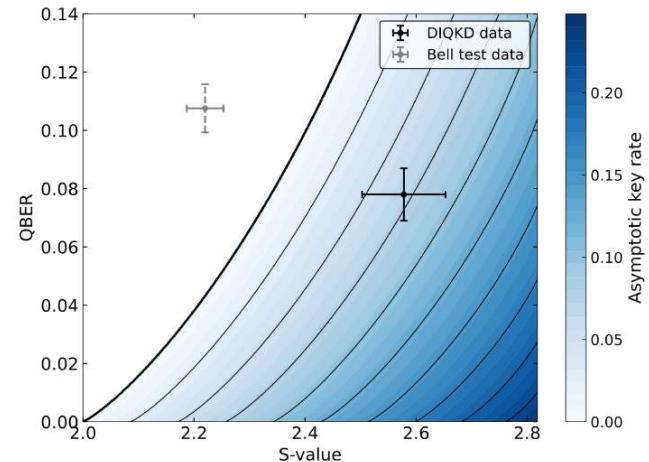
xop



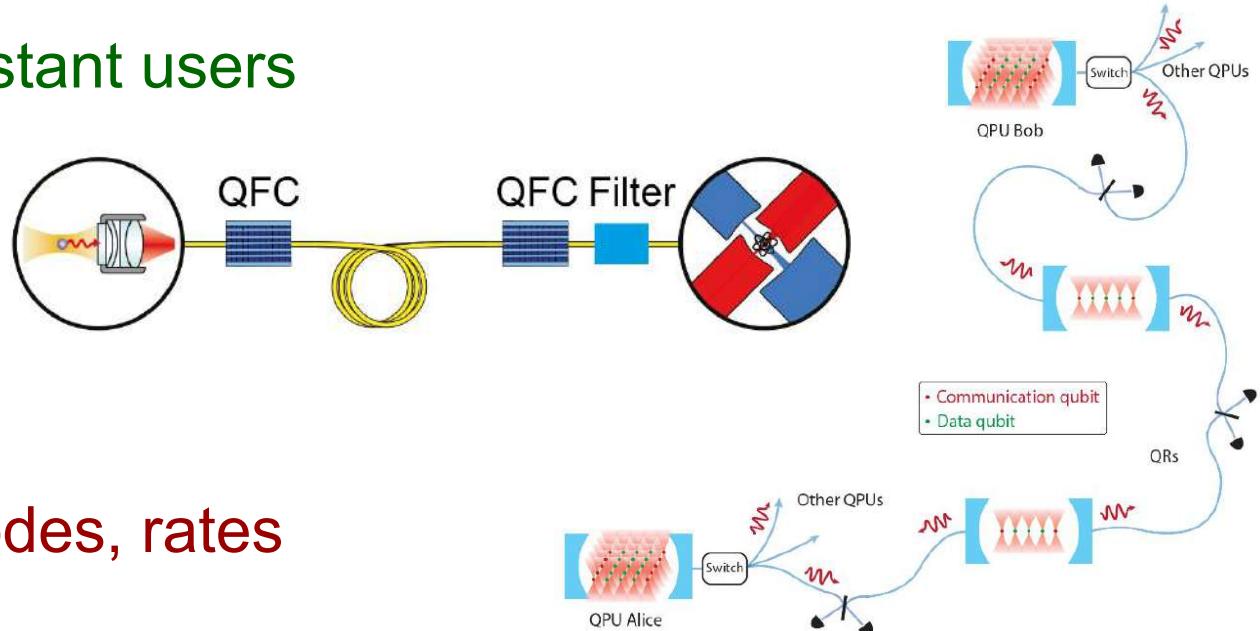
Summary



- Atom-Atom-Entanglement
 - atom-photon entanglement + entanglement swapping
- loophole free Bell-test



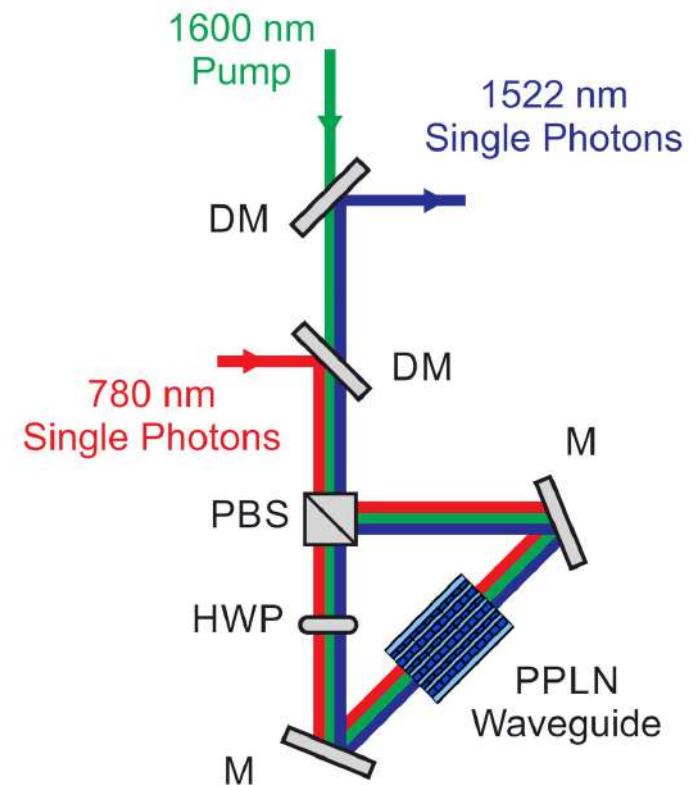
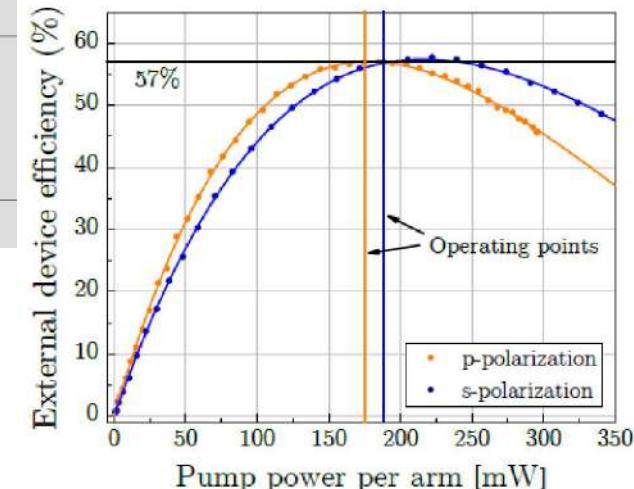
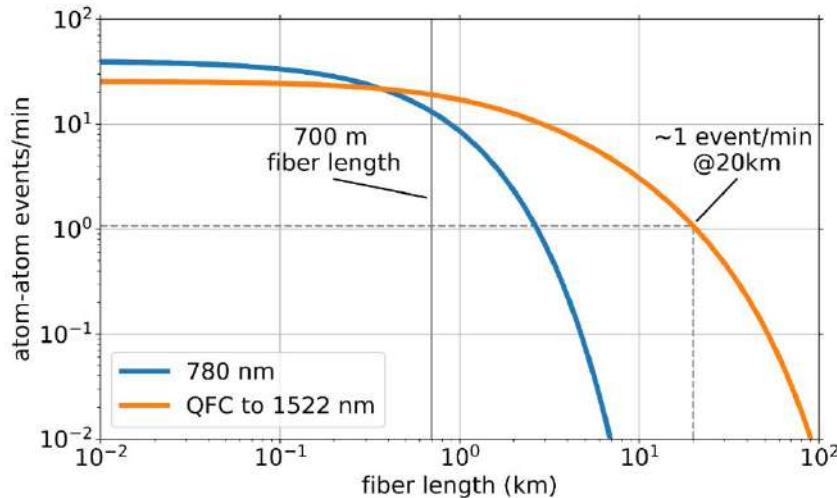
- DIQKD between distant users
- longer distances
- LMU-MPQ link



- quantum networks:
 - memory, local nodes, rates

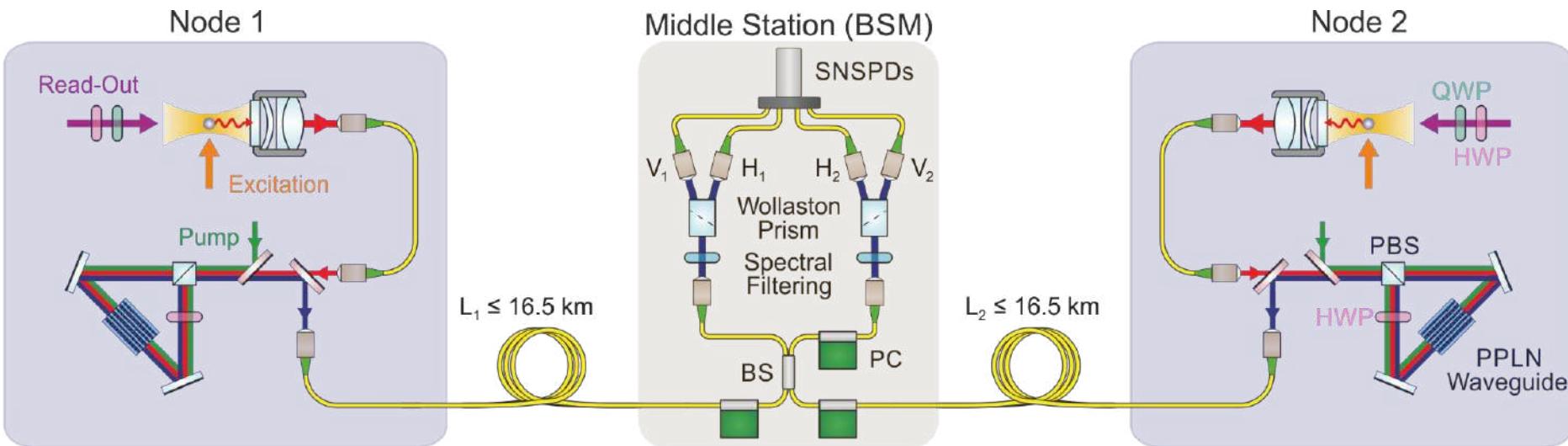
long distances

- efficient optical coupling
- long coherence times
vector light shift → lower temp, standing wave
magnetic field → new encoding
- absorption in fiber
→ quantum frequency conversion





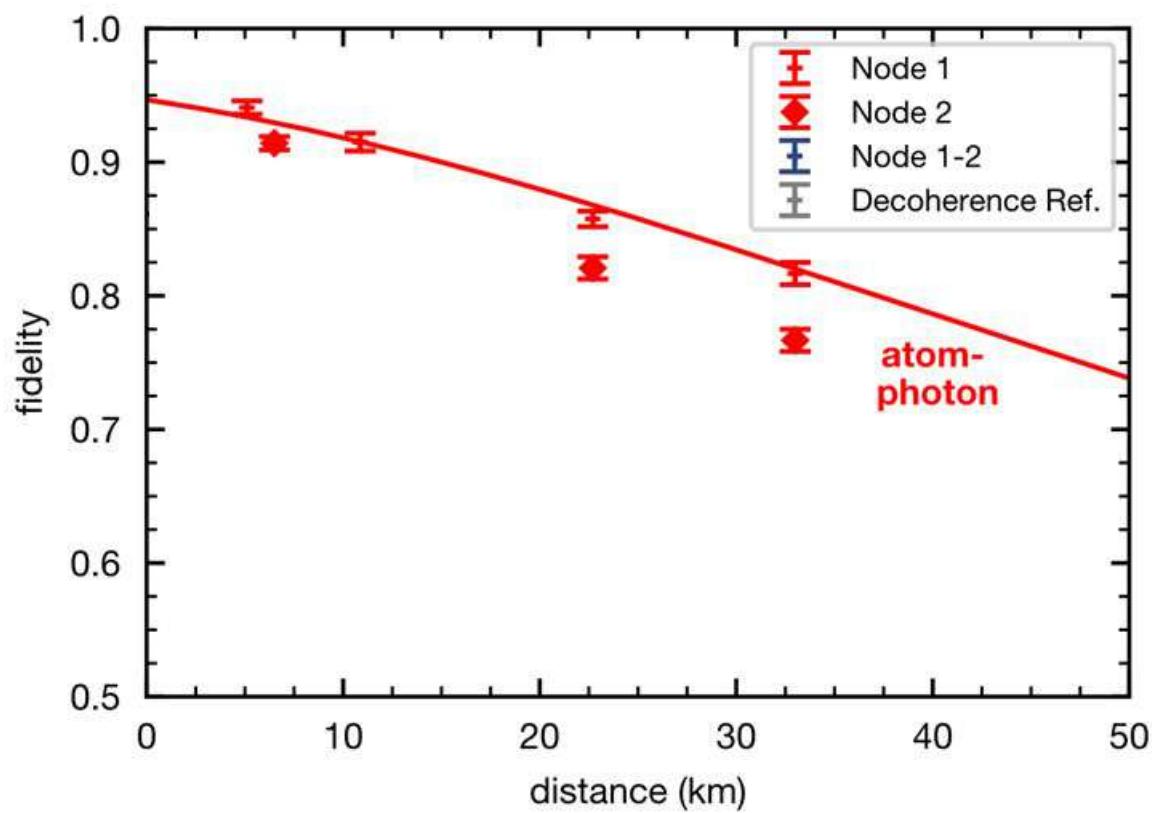
- two conversion units + BSM at telecom wavelengths



- Physical separation between nodes equals 400 m
- Different symmetric fiber configurations: $L = 6, 11, 23$, and 33 km
- Implement delay for communication of the heralding signal
 - decoherence for long times + Raman noise from converter



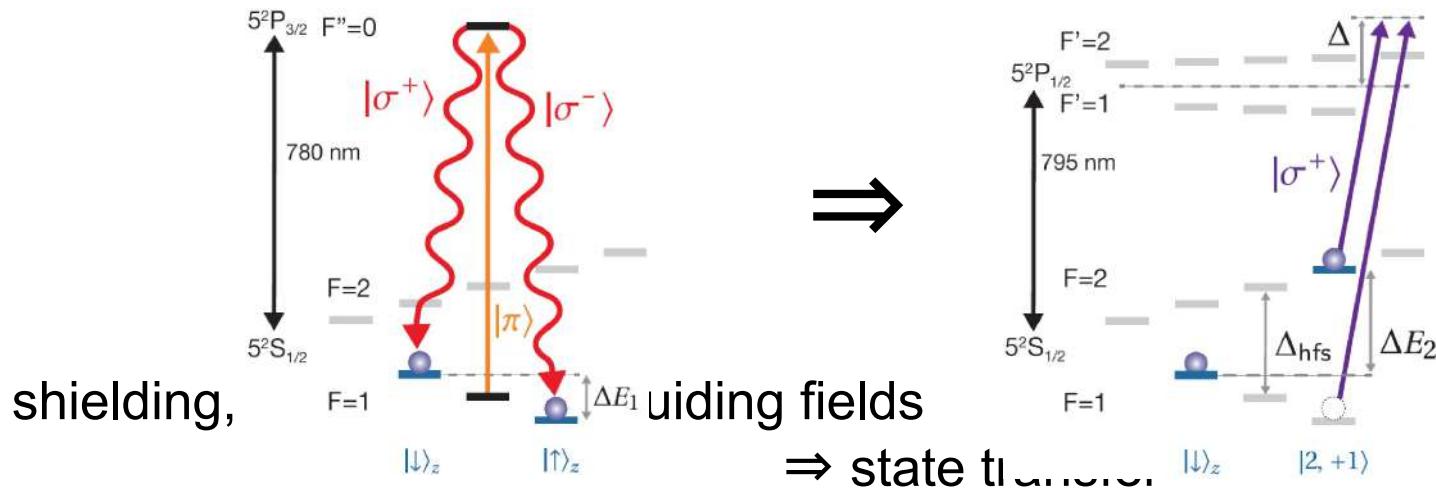
- atom-atom entanglement over up to 30 km



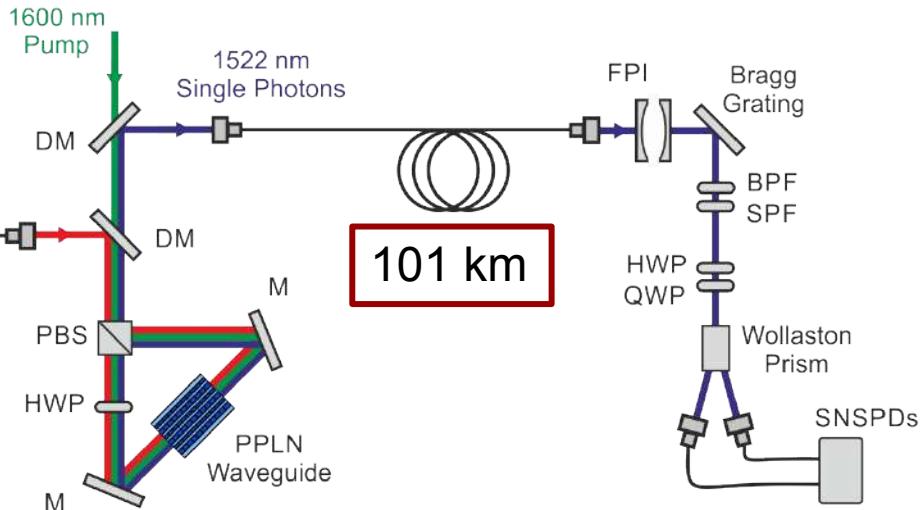
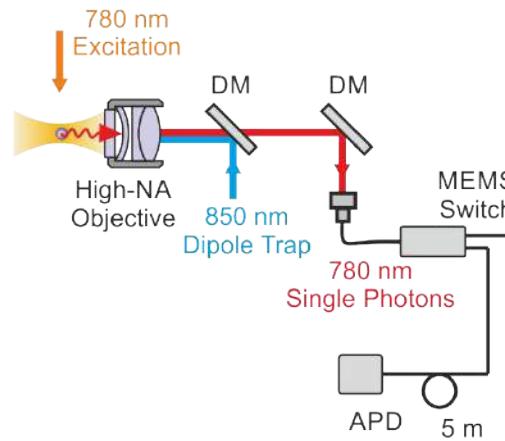
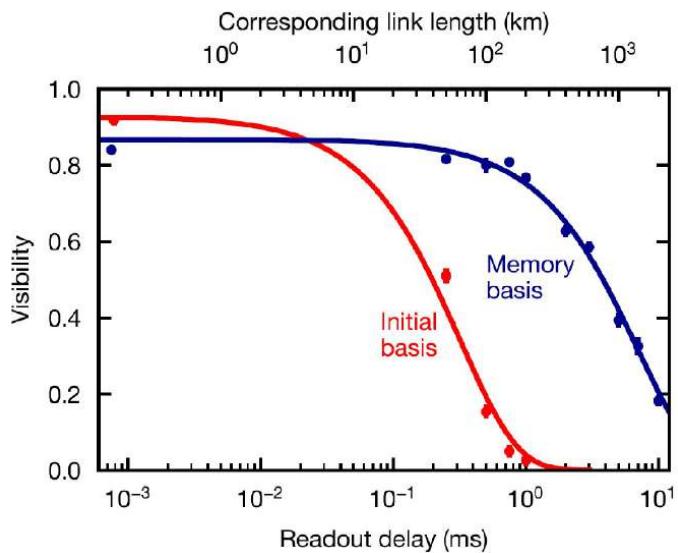
decoherence ? dephasing !



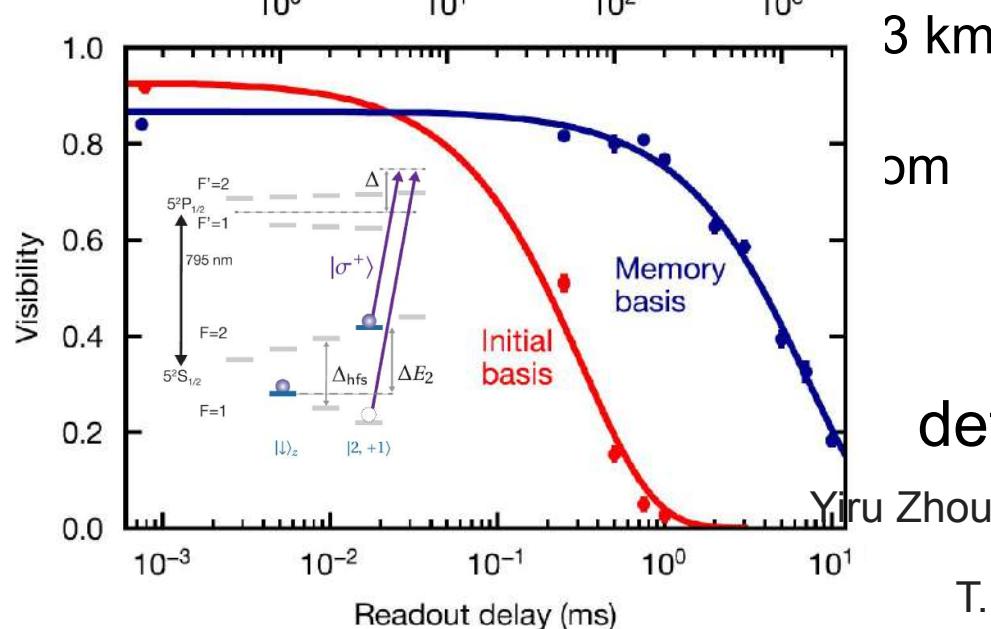
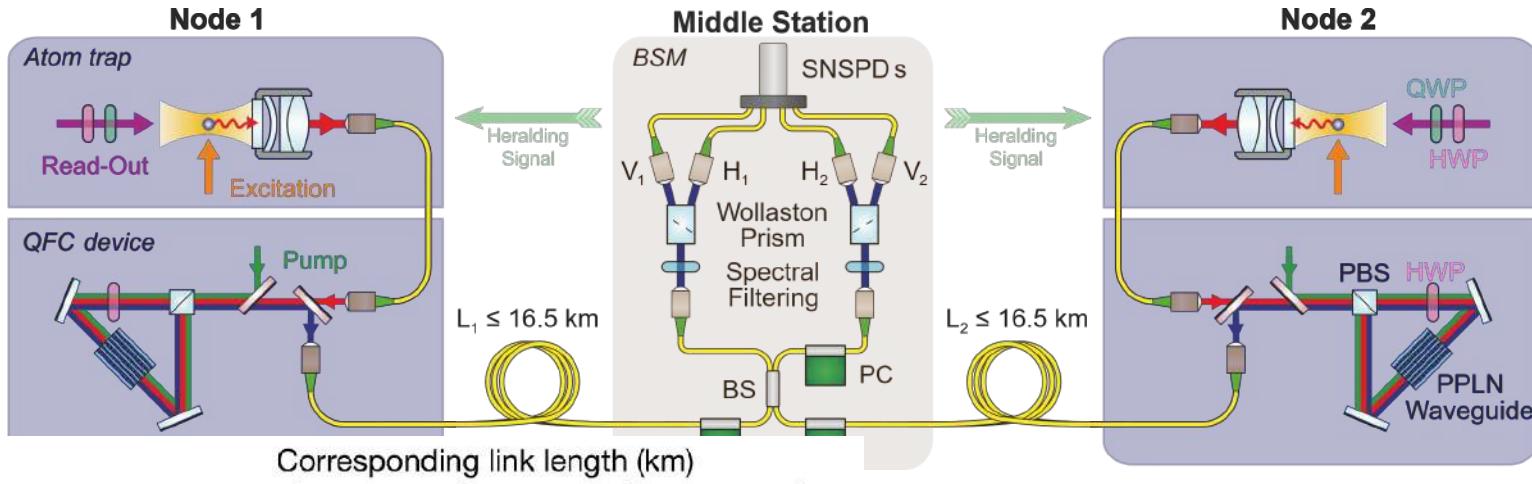
magnetic fields: subway,..., strongly focused light



EXPERIMENTS ON BELL'S THEOREM



long(er) distances



quantum networks?

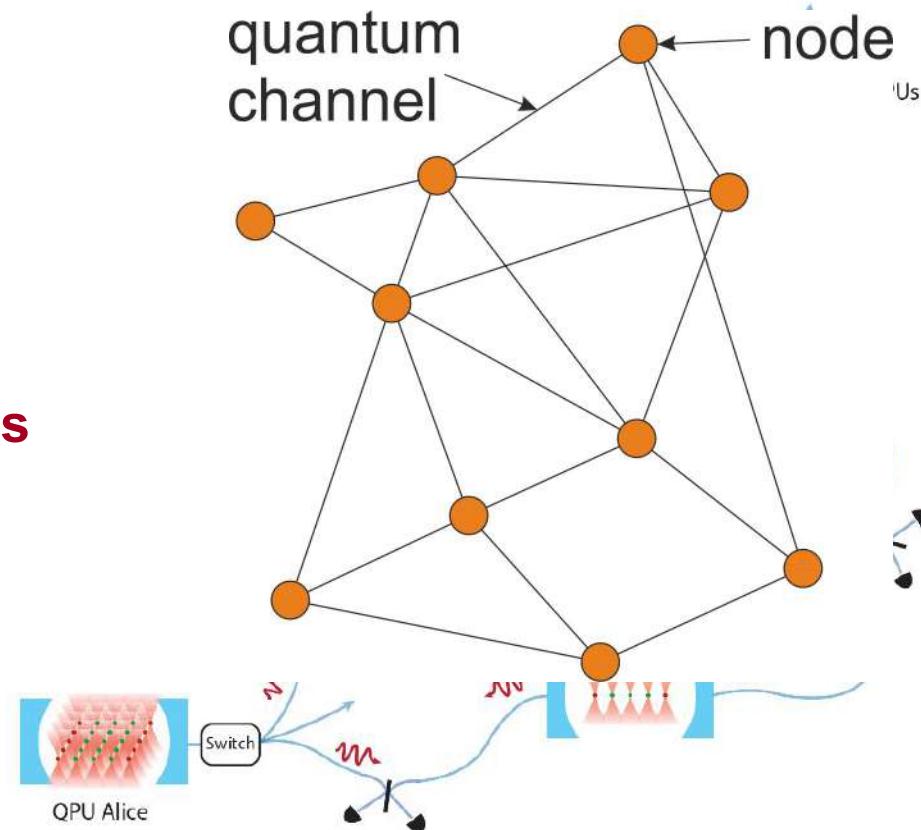


- quantum channel:
efficient quantum repeater functionality

- quantum memory
- quantum logic operation
for entanglement purification
and Bell-state measurement

- quantum node:
 - **provide entanglement at all times**
 - one link:
link efficiency

$$\eta = \frac{\gamma_{ent}}{\gamma_{dec}} > 1$$

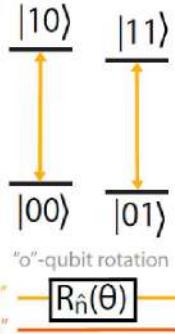


quantum networks?



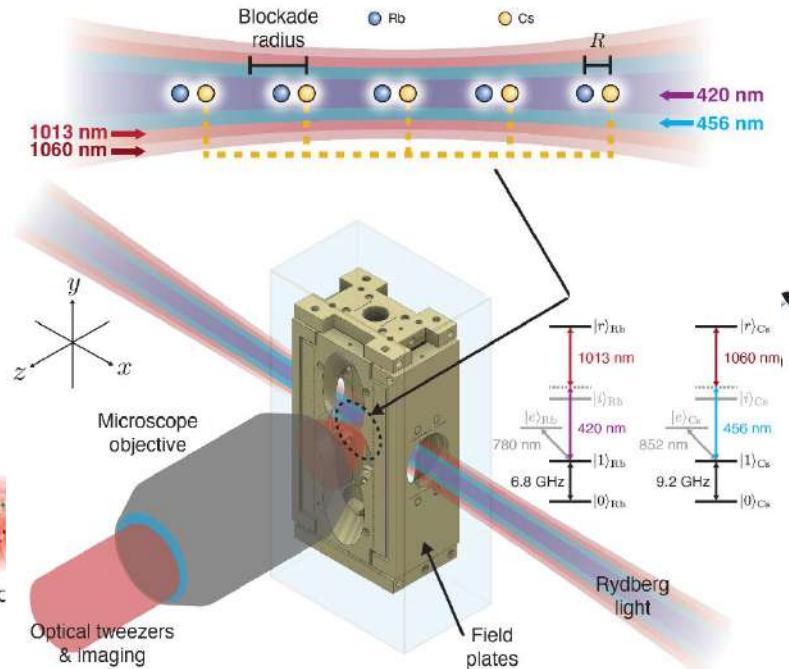
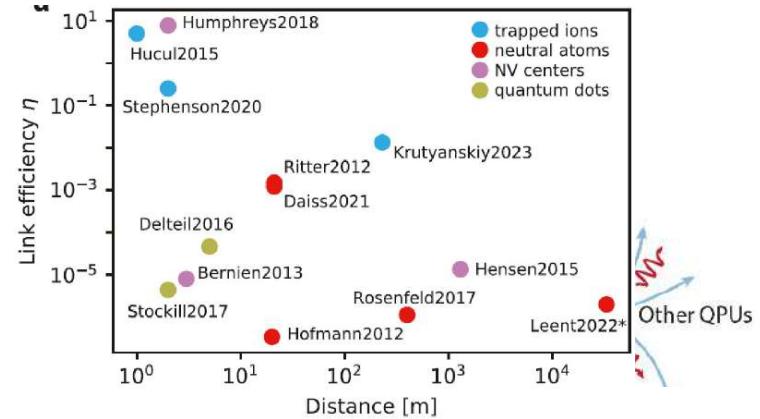
$$\eta = \frac{\gamma_{ent}}{\gamma_{dec}} > 1$$

- quantum memories
 - quantum error correction
- neutral atom implementations:



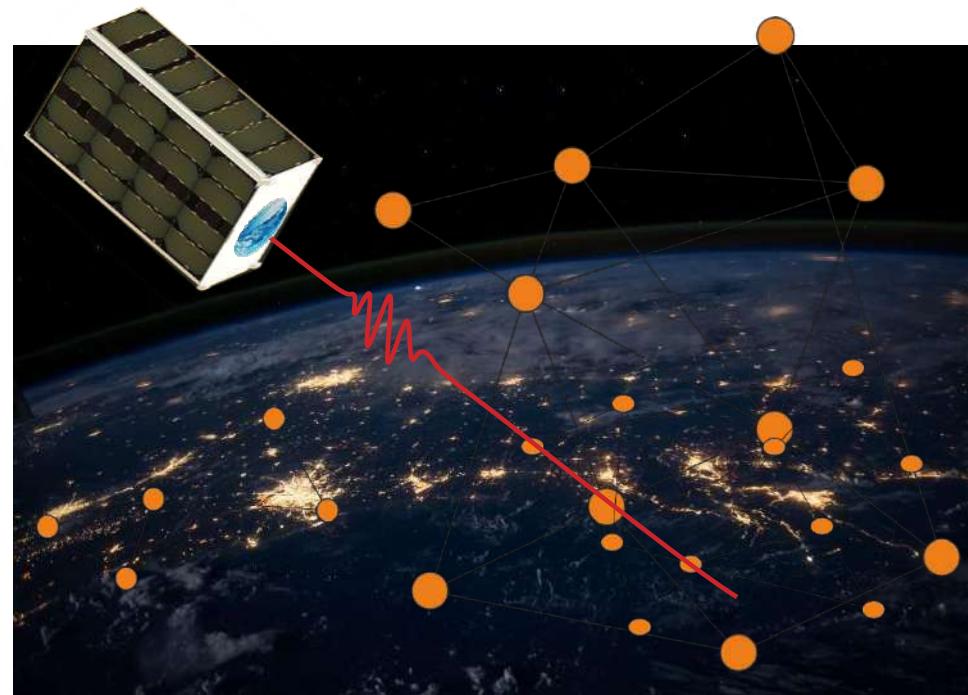
Yb ququart

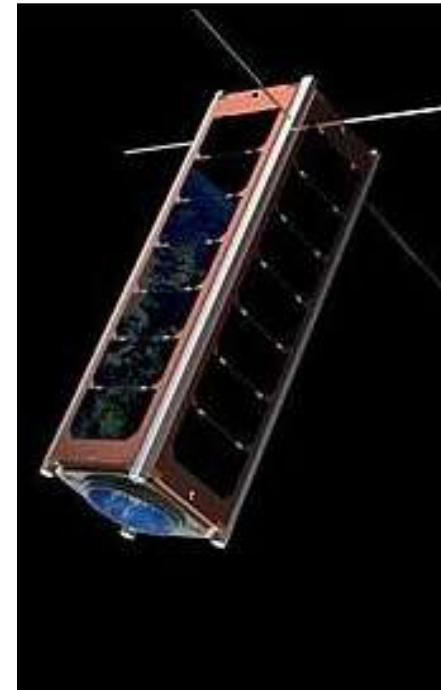
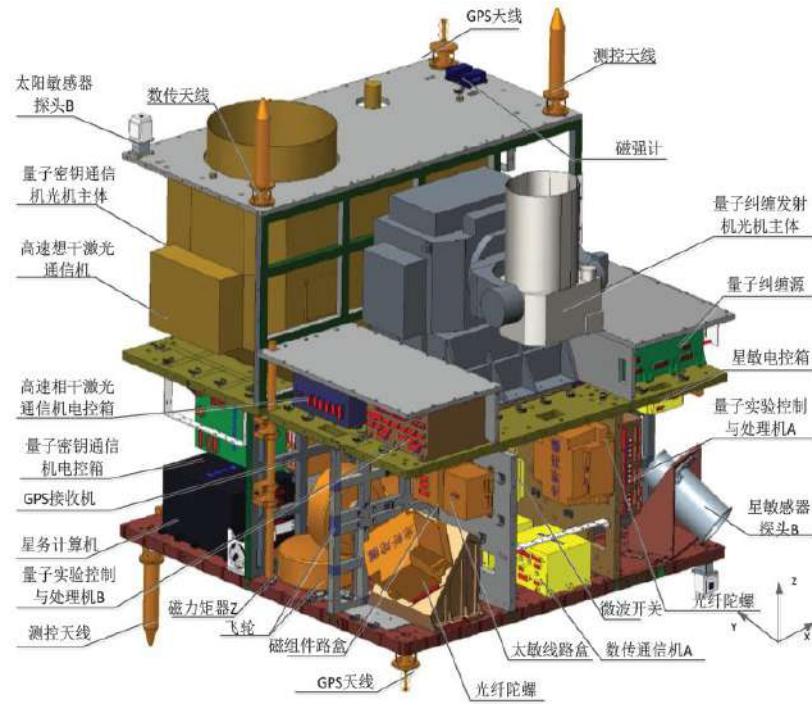
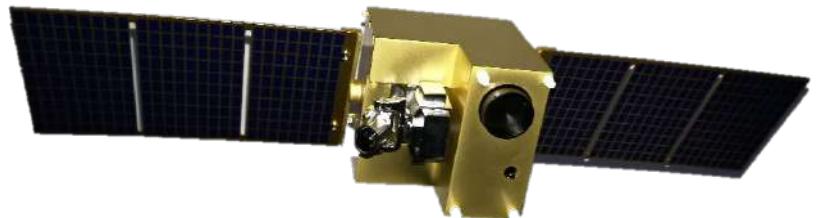
- Z. Jia et al., arXiv:2402.13134
 S. Anand et al., arXiv:2401.10325
 S.G. Menon et al., Nature Comm. **15**, 6156 (2024)
 D. Bluvstein et al., Nature **626**, 58 (2024)





- Fundamental elements of Quantum Physics
 - secure communication
 - towards quantum networks
- Loophole-free Bell test
DI-QKD



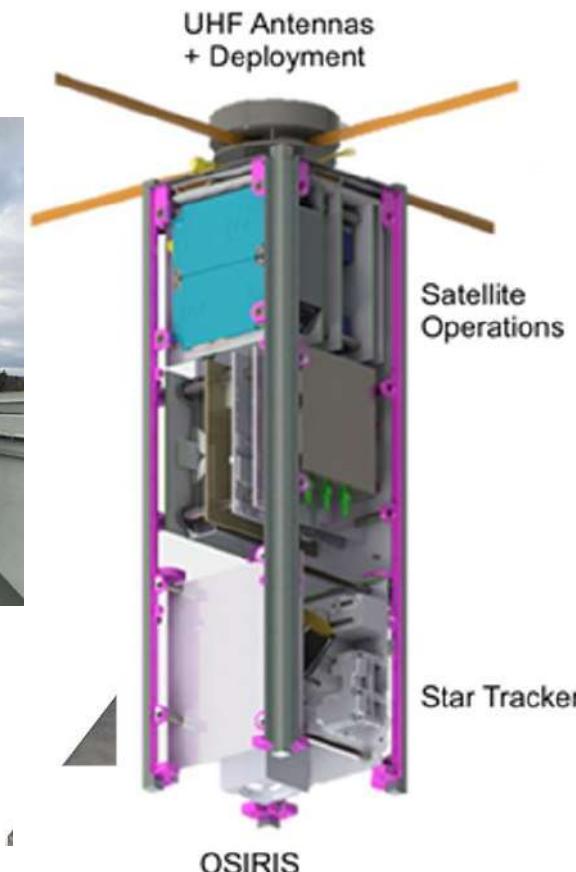
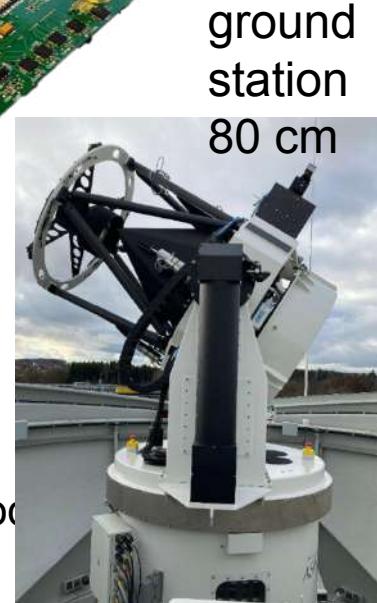
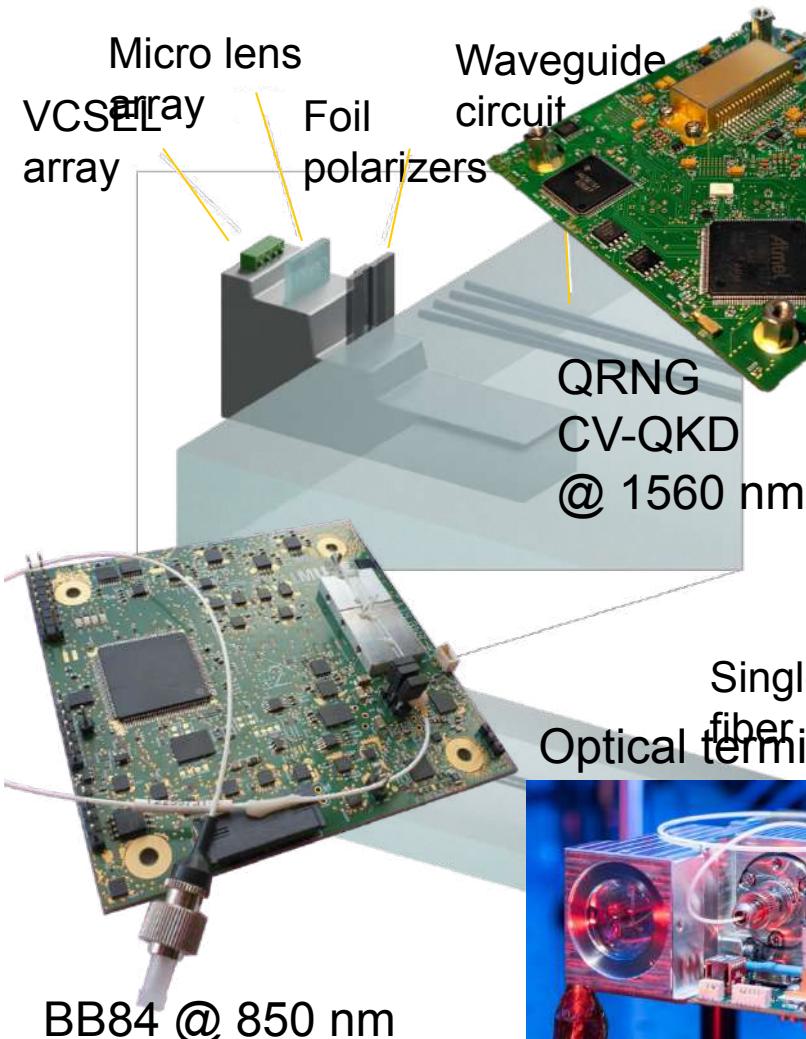


SWaP : size, weight, and power

QKD on cubesats?



2017 – 2021



MAX PLANCK INSTITUTE
for the science of light



ZENTRUM
FÜR
TELEMATIK E.V.



Communication
s
and Navigation



