

# Top quark polarization

*A probe of new physics*

*at*  
**Institut fuer Theoretische Physik und Astronomie**

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**Wuerzburg, Germany**

by

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SUSY	ED	TC	LH
Fermion mass	CP violation Fermion mass	CP violation Fermion mass Scale hierarchy	CP violation Fermion mass Scale hierarchy

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Polarization observables and decay pattern are most important features to study new particles.

# Top quark & new physics

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Top quark's coupling to the SM particles are subjected to modification due to new particles/interactions.

$$t\bar{t}\phi := g_{t\bar{t}\phi} (S_t + i P_t \gamma_5)$$

$$t\bar{t}V := g_V \left[ \gamma^\mu (f_{1L} P_L + f_{1R} P_R) + \frac{i \sigma^{\mu\nu}}{m_W} q_\nu (f_{2L} P_L + f_{2R} P_R) \right]$$

Top quark's couplings to the new particles leads to associated productions; polarization of top quark can be used to probe the new particles couplings and properties.

⇒ **Study of new physics can be done via study of top quark.**

# Top quark properties

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	Measurement	SM prediction
<b>Mass</b>	$171.4 \pm 2.1 \text{ GeV}$	-
<b>Charge</b>	Not $4/3$ (94% CL)	$2/3$
$F_0$	$0.59 \pm 0.14$	0.75
$F_+$	$< 0.10$ (95% CL)	0
<b>Spin</b>	-	$1/2$

⇒ Need to know top quark properties precisely.

We assume spin of top quark to be  $1/2$  and charge to be  $2/3$ , as in the SM, for rest of our study of new physics.

# top-quark : A looking glass

---

The mass of the top-quark is very large ( $m_t \sim 172$  GeV)

- top-mass being close to electro-weak scale, its couplings are sensitive to EWSB. Any new physics of EWSB (or mass generation) affects top-couplings with other particles.

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- the decay lepton angular distribution is insensitive to the anomalous  $tbW$  couplings, and hence a pure probe of new physics in top-production process; observed for top-pair production at  $e^+e^-$  (Rindani, Grzadkowski) as well as  $\gamma\gamma$  collider (Ohkuma, Godbole).

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We have a clean looking glass for new physics.

# Anomalous $t$ -decay

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Anomalous  $tbW$  vertex :

$$\Gamma^\mu = \frac{g}{\sqrt{2}} \left[ \gamma^\mu (f_{1L} P_L + \cancel{f_{1R}} P_R) - \frac{i\sigma^{\mu\nu}}{m_W} (p_t - p_b)_\nu (\cancel{f_{2L}} P_L + f_{2R} P_R) \right]$$

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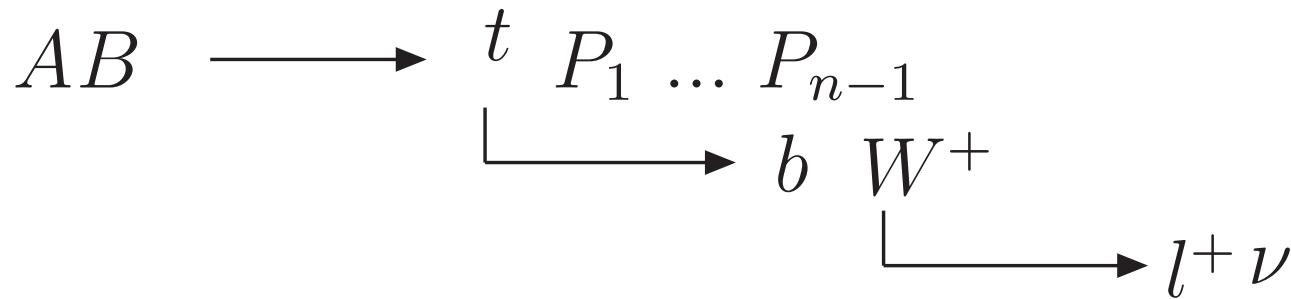
Anomalous  $tbW$  vertex :

$$\Gamma^\mu = \frac{g}{\sqrt{2}} \left[ \gamma^\mu (f_{1L} P_L + \textcolor{red}{f_{1R}} P_R) - \frac{i\sigma^{\mu\nu}}{m_W} (p_t - p_b)_\nu (\textcolor{red}{f_{2L}} P_L + f_{2R} P_R) \right]$$

- In the SM,  $f_{1L} = 1$ ,  $\textcolor{red}{f_{1R}} = 0$ ,  $f_{2L} = 0$ ,  $f_{2R} = 0$ .
- Contribution from  $\textcolor{red}{f_{1R}}$ ,  $f_{2L}$  are proportional to  $m_b$ .

# Lepton distribution

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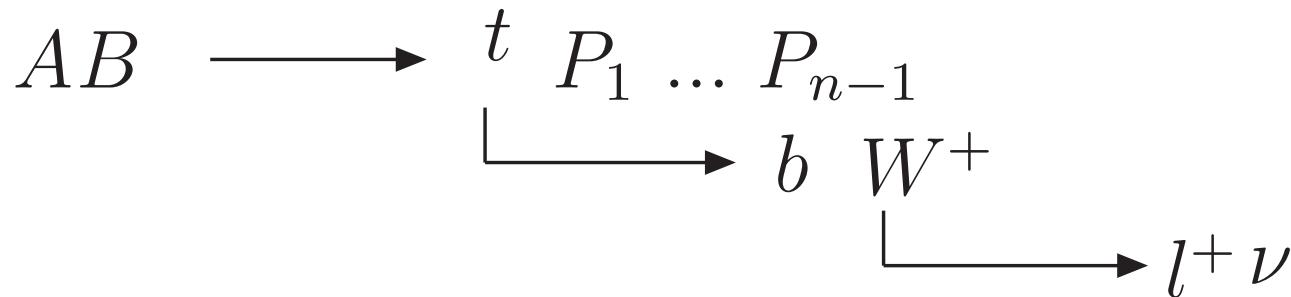


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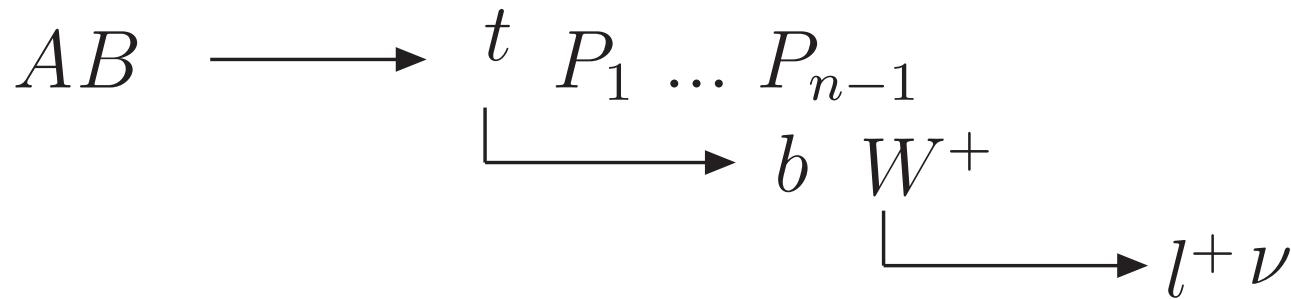


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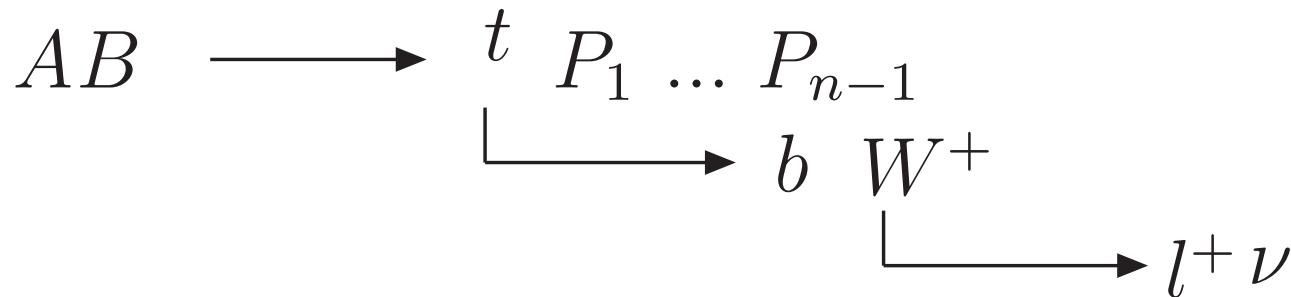


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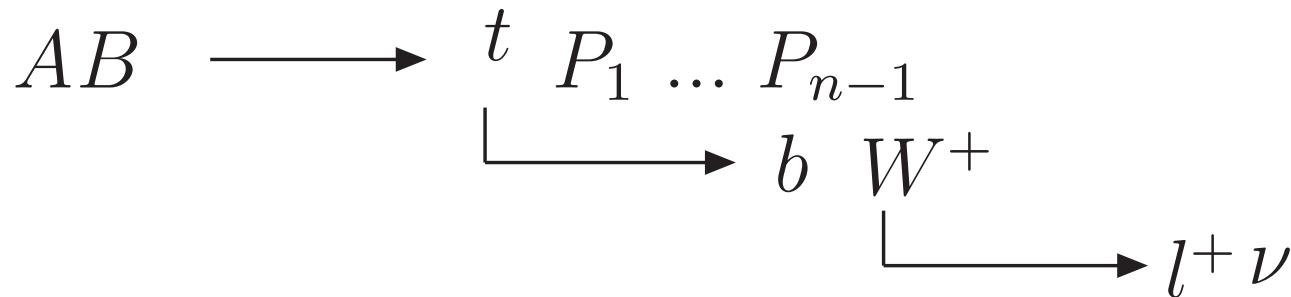


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- $b$ -quark is mass-less,
- $t \rightarrow bW(\ell\nu_\ell)$  is the only decay channel for  $t$ -quark.

# Decay distribution

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Narrow-width approximation for  $t$ -quark  $\Rightarrow$

$$\overline{|\mathcal{M}|^2} = \frac{\pi\delta(p_t^2 - m_t^2)}{\Gamma_t m_t} \sum_{\lambda, \lambda'} \rho(\lambda, \lambda') \Gamma(\lambda, \lambda')$$

where,

$$\rho(\lambda, \lambda') = M_\rho(\lambda) M_\rho^*(\lambda') \quad \text{and} \quad \Gamma(\lambda, \lambda') = M_\Gamma(\lambda) M_\Gamma^*(\lambda').$$

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$$\begin{aligned} d\sigma &= \sum_{\lambda, \lambda'} \left[ \frac{(2\pi)^4}{2I} \rho(\lambda, \lambda') \delta^4(k_A + k_B - p_t - \sum_i^{n-1} p_i) \frac{d^3 p_t}{2E_t(2\pi)^3} \prod_i^{n-1} \frac{d^3 p_i}{2E_i(2\pi)^3} \right] \\ &\times \left[ \frac{1}{\Gamma_t} \left( \frac{(2\pi)^4}{2m_t} \Gamma(\lambda, \lambda') \delta^4(p_t - p_b - p_\nu - p_\ell) \frac{d^3 p_b}{2E_b(2\pi)^3} \frac{d^3 p_\nu}{2E_\nu(2\pi)^3} \right) \frac{d^3 p_\ell}{2E_\ell(2\pi)^3} \right]. \end{aligned}$$

# Decay distribution

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Production part ( $\phi_t = 0$ ) :

$$\int \frac{d^3 p_t}{2E_t(2\pi)^3} \prod_i^{n-1} \frac{d^3 p_i}{2E_i(2\pi)^3} \frac{(2\pi)^4}{2I} \rho(\lambda, \lambda') \delta^4 \left( k_A + k_B - p_t - \left( \sum_i^{n-1} p_i \right) \right)$$
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Decay part (in rest rest frame of  $t$ -quark) :

$$\frac{1}{\Gamma_t} \frac{(2\pi)^4}{2m_t} \int \frac{d^3 p_\ell}{2E_\ell(2\pi)^3} \frac{d^3 p_b}{2E_b(2\pi)^3} \frac{d^3 p_\nu}{2E_\nu(2\pi)^3} \Gamma(\lambda, \lambda') \delta^4(p_t - p_b - p_\nu - p_\ell)$$
$$= \frac{1}{32\Gamma_t m_t} \frac{E_\ell}{(2\pi)^4} \frac{\langle \Gamma(\lambda, \lambda') \rangle}{m_t E_\ell} dE_\ell d\Omega_\ell dp_W^2.$$

Angular brackets stands for averaging over  $\phi = (\phi_b - \phi_\ell)$ .

# Decay density matrix

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In the rest frame of  $t$ -quark, we have

$$\begin{aligned}\langle \Gamma(\pm, \pm) \rangle &= g^4 m_t E_\ell^0 |\Delta_W(p_W^2)|^2 (1 \pm \cos \theta_l) \times F(E_\ell^0), \\ \langle \Gamma(\pm, \mp) \rangle &= g^4 m_t E_\ell^0 |\Delta_W(p_W^2)|^2 (\sin \theta_l e^{\pm i\phi_l}) \times F(E_\ell^0).\end{aligned}$$

where  $\Delta_W(p_W^2) = \frac{1}{p_W^2 - m_W^2 + i\Gamma_W m_W}$

$$\begin{aligned}F(E_\ell^0) &= \left[ (m_t^2 - m_b^2 - 2p_t \cdot p_l) \left( |f_{1L}|^2 + \Re(f_{1L} f_{2R}^*) \frac{m_t}{m_W} \frac{p_W^2}{p_t \cdot p_l} \right) \right. \\ &\quad \left. - 2\Re(f_{1L} f_{2L}^*) \frac{m_b}{m_W} p_W^2 - \Re(f_{1L} f_{1R}^*) \frac{m_b m_t}{p_t \cdot p_l} p_W^2 \right]\end{aligned}$$

In general,

$$\langle \Gamma(\lambda, \lambda') \rangle = (m_t E_\ell^0) |\Delta(p_W^2)|^2 g^4 A(\lambda, \lambda') F(E_\ell^0)$$

# Angular distribution of lepton

---

Combining production and decay part, we have

$$\begin{aligned} d\sigma &= \frac{1}{32 \Gamma_t m_t (2\pi)^4} \left[ \sum_{\lambda, \lambda'} d\sigma_{2 \rightarrow n}(\lambda, \lambda') \times g^4 A^{c.m.}(\lambda, \lambda') \right] \\ &\times dE_t d\cos\theta_t d\cos\theta_\ell d\phi_\ell \\ &\times E_\ell F(E_\ell) |\Delta(p_W^2)|^2 dE_\ell dp_W^2 \end{aligned}$$

and

$$\Gamma_t \propto \int E_\ell F(E_\ell) |\Delta(p_W^2)|^2 dE_\ell dp_W^2$$

Contribution from anomalous  $tbW$  couplings cancels between numerator and denominator, if  $t \rightarrow bW$  is the only decay channel.

**⇒ Lepton angular distribution is independent of anomalous  $tbW$  interactions.**

# Energy distribution of lepton

---

The  $E_\ell$  distribution (in the lab frame) depends both on

- anomalous  $t b W$  couplings  $\Rightarrow$  **new physics in  $t$ -decay**
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The  $E_\ell^0$  distribution (in the top-rest-frame) depends only on the possible **new physics in  $t$ -decay**.

$$\frac{d\sigma}{dE_\ell^0} \propto \int E_l^0 F(E_l^0) |\Delta(p_W^2)|^2 dp_W^2$$

**Independent of production mechanism of  $t$ -quark !!**

# Polarization of $t$ -quark

---

Polarized cross-sections :

$$\int \frac{d^3 p_t}{2E_t(2\pi)^3} \left( \prod_{i=1}^{n-1} \frac{d^3 p_i}{2E_i(2\pi)^3} \right) \frac{(2\pi)^4}{2I} \rho(\lambda, \lambda') \delta^4 \left( k_A + k_B - p_t - \left( \sum_{i=1}^{n-1} p_i \right) \right) = \sigma(\lambda, \lambda').$$

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Polarization density matrix :

$$P_t = \frac{1}{2} \begin{pmatrix} 1 + \eta_3 & \eta_1 - i\eta_2 \\ \eta_1 + i\eta_2 & 1 - \eta_3 \end{pmatrix}, \quad \begin{aligned} \eta_3 &= (\sigma(+,+) - \sigma(-,-)) / \sigma_{tot} \\ \eta_1 &= (\sigma(+,-) + \sigma(-,+)) / \sigma_{tot} \\ i \eta_2 &= (\sigma(+,-) - \sigma(-,+)) / \sigma_{tot} \end{aligned}$$

# Polarization of $t$ -quark

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Polarization through leptonic decay of  $t$ -quark :

$$\frac{\eta_3}{2} = \frac{\sigma(p_\ell \cdot s_3 < 0) - \sigma(p_\ell \cdot s_3 > 0)}{\sigma(p_\ell \cdot s_3 < 0) + \sigma(p_\ell \cdot s_3 > 0)}$$

$$\frac{\eta_2}{2} = \frac{\sigma(p_\ell \cdot s_2 < 0) - \sigma(p_\ell \cdot s_2 > 0)}{\sigma(p_\ell \cdot s_2 < 0) + \sigma(p_\ell \cdot s_2 > 0)}$$

$$\frac{\eta_1}{2} = \frac{\sigma(p_\ell \cdot s_1 < 0) - \sigma(p_\ell \cdot s_1 > 0)}{\sigma(p_\ell \cdot s_1 < 0) + \sigma(p_\ell \cdot s_1 > 0)}$$

$$s_i \cdot s_j = -\delta_{ij} \quad p_t \cdot s_i = 0$$

For  $p_t^\mu = E_t(1, \beta_t \sin \theta_t, 0, \beta_t \cos \theta_t)$ , we have

$$s_1^\mu = (0, -\cos \theta_t, 0, \sin \theta_t), \quad s_2^\mu = (0, 0, 1, 0), \quad s_3^\mu = E_t(\beta_t, \sin \theta_t, 0, \cos \theta_t)/m_t.$$

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Angular distribution in lab frame can be used as a qualitative measure of the  $t$ -polarization.

# Polarization through angular distribution

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For demonstration, we chose  $\gamma\gamma \rightarrow t\bar{t}$  process with/without Higgs exchange contribution.

$$m_\phi = 500 \text{ GeV}; \Gamma_\phi = 2.5 \text{ GeV},$$

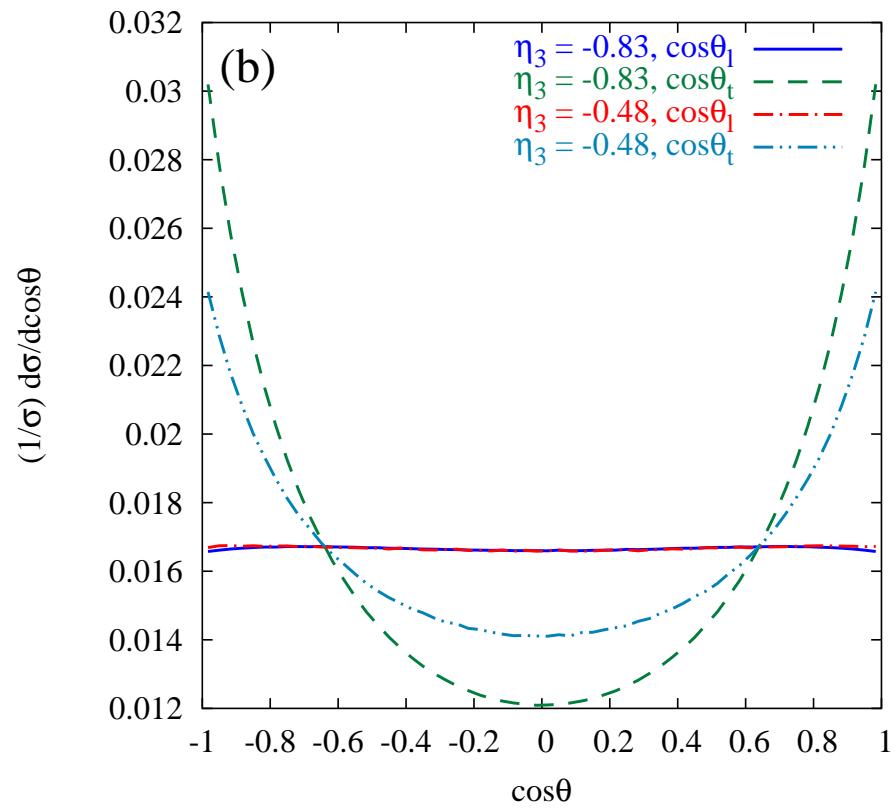
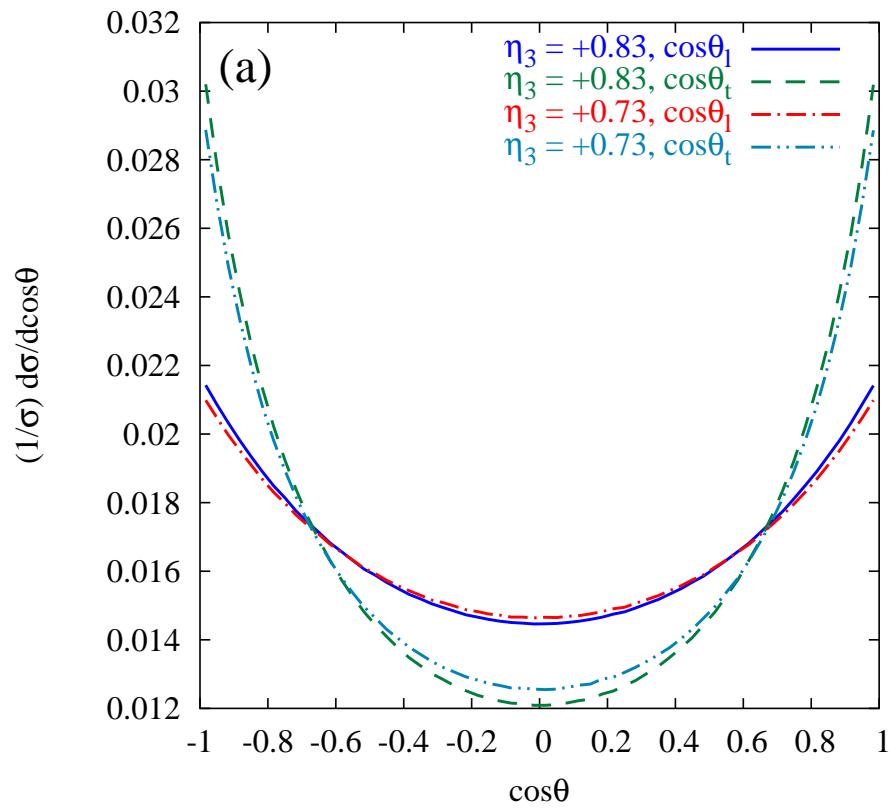
$$S_t = 0.2, P_t = 0.4, S_\gamma = 4.0 + i 0.5 \text{ and } P_\gamma = 1.25 + i 2.0.$$

**Polarized ideal photon spectrum is used.**

**Assumptions :**

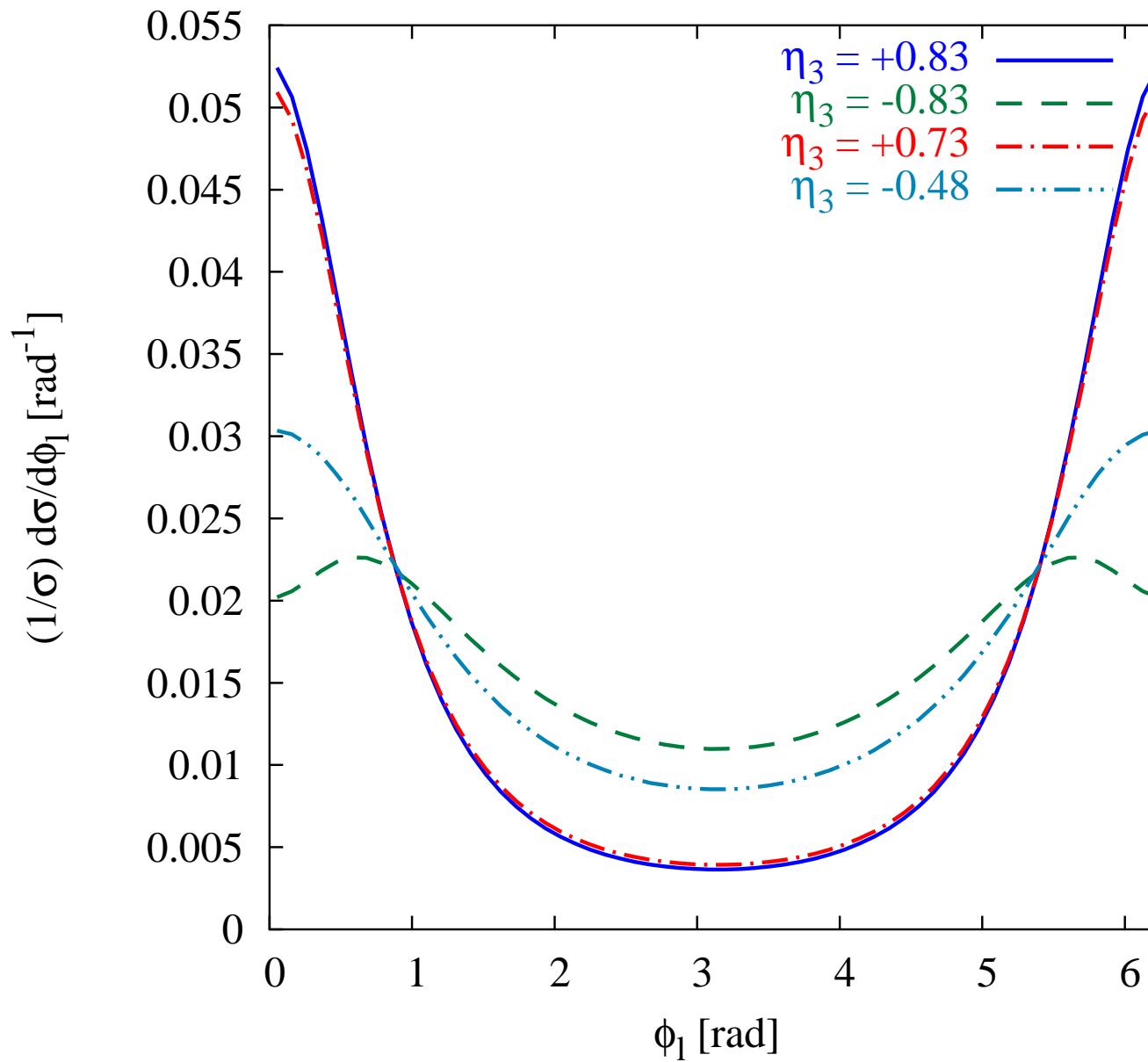
- $t$ -quark is on-shell
- anomalous  $tbW$  couplings are small
- $W$ -boson is on-shell
- $b$ -quark is mass-less and
- $t \rightarrow bW$  is the only decay channel for  $t$ -decay

# Polarization through angular distribution

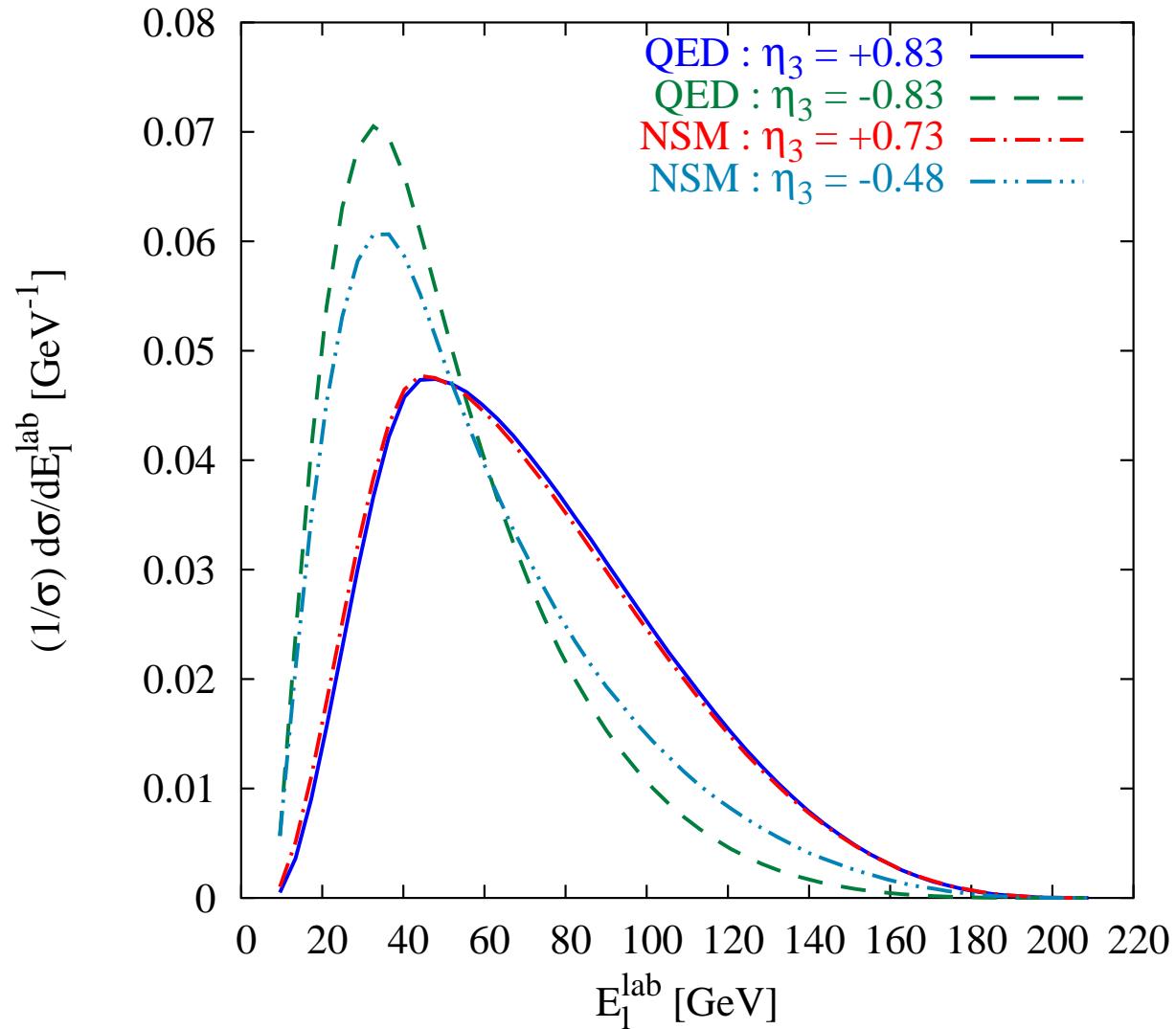


$$\eta_1 = 0 \text{ and } \eta_2 = 0$$

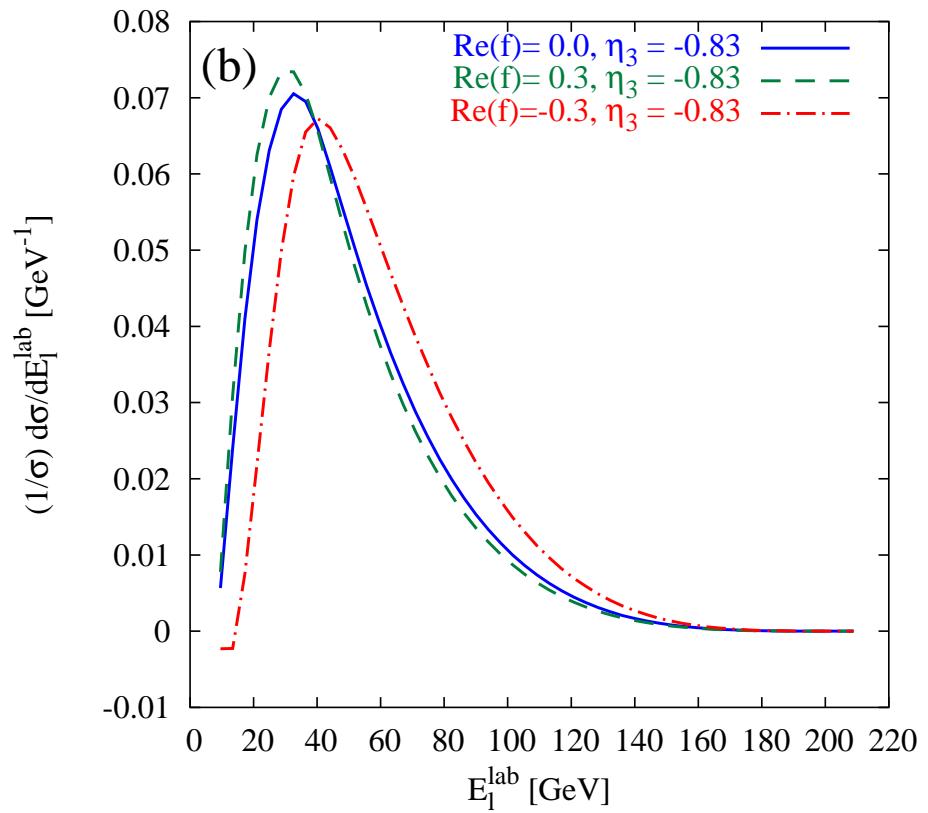
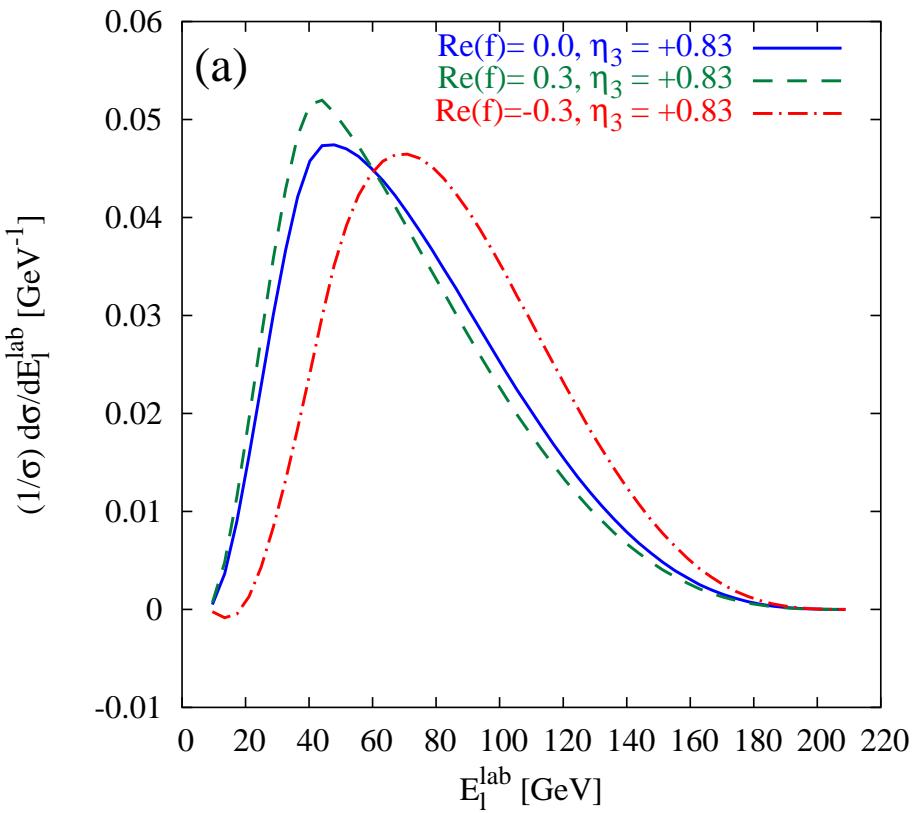
# Polarization through angular distribution



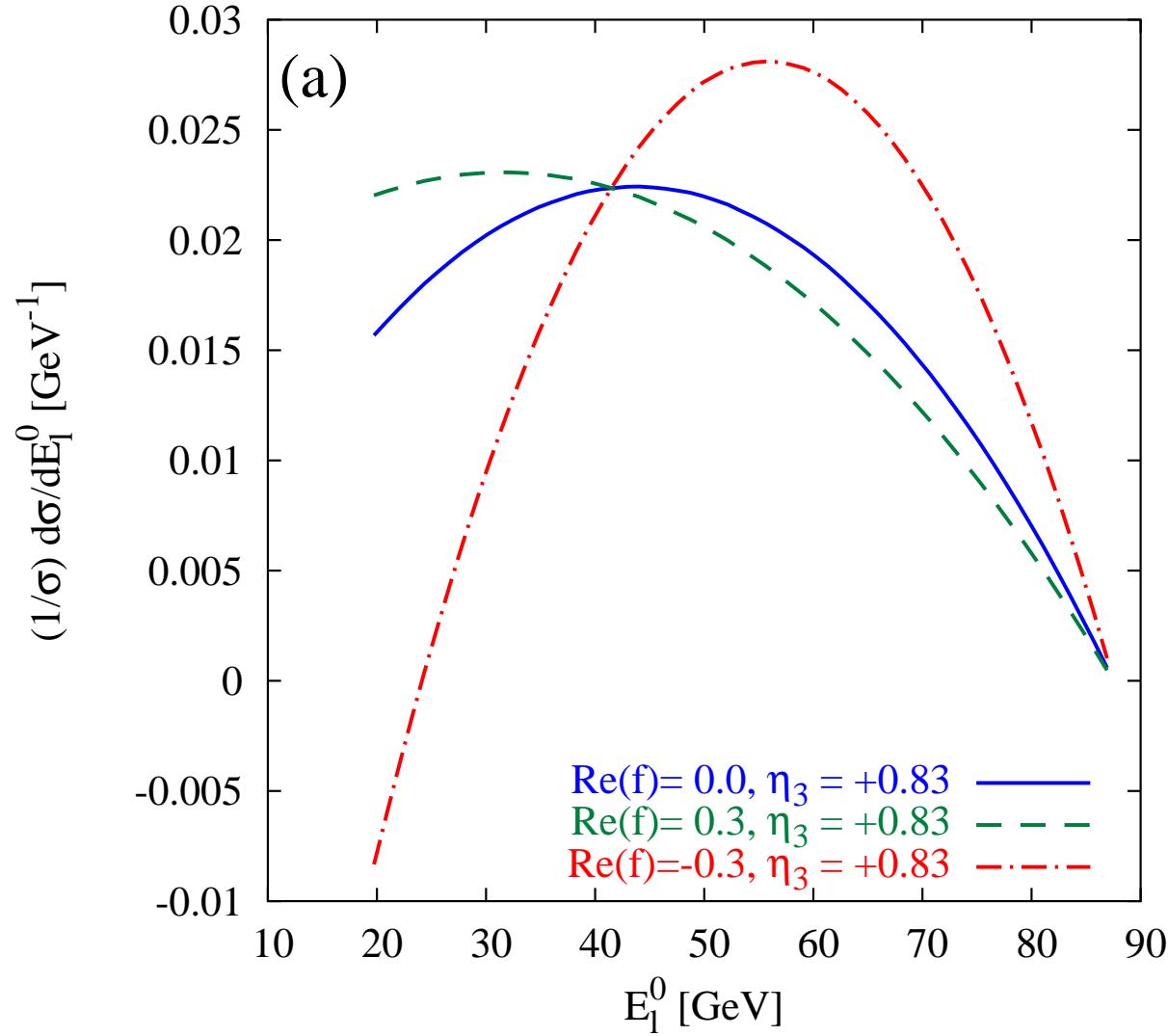
# Energy distribution



# Energy distribution



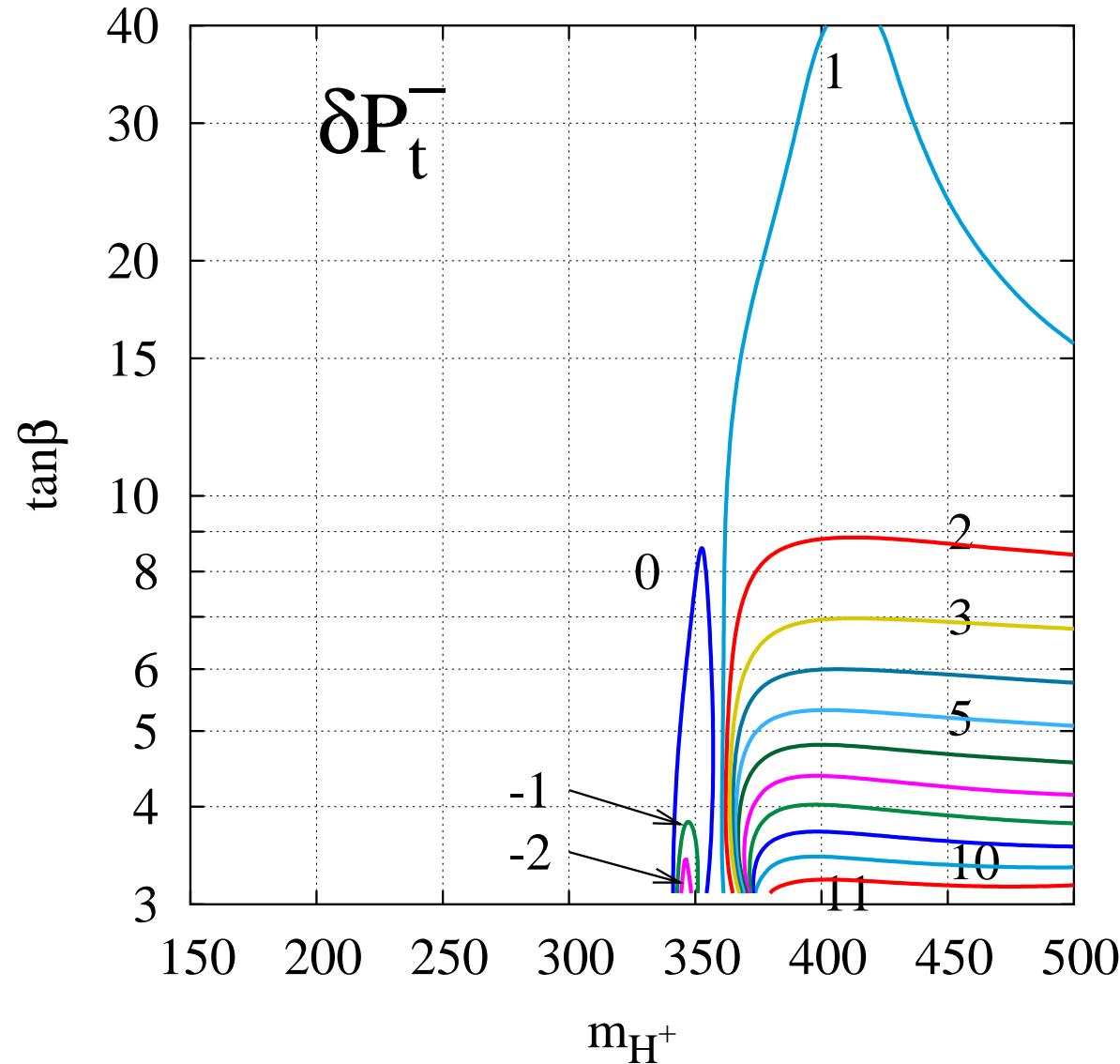
# Energy distribution



## CPX scenario

MSSM parameters	Values
$\tan \beta$	3 - 40 (used for scan)
$m_{H^+}$	150-500 GeV (used for scan)
$\mu$	2 TeV, $\Phi_\mu = 0$
$M_1, M_2$	200 GeV, $\Phi_{1,2} = 0$
$M_3$	1 TeV, $\Phi_3 = 90^\circ$
$m_{\tilde{q}, \tilde{l}}$	500 GeV
$A_{t,b}$	1 TeV, $\Phi_{t,b} = 90^\circ$
$A_\tau$	500 GeV, $\Phi_\tau = 90^\circ$

# SUSY Higgs: $\gamma\gamma \rightarrow t\bar{t}$



# Flat extra-dimensions: $pp \rightarrow t\bar{t}$

---

In the models of flat extra-dimensions, there is a KK-tower of excitations corresponding to each SM gauge bosons and fermions.

Signal channel in  $pp$  collision:

$$q\bar{q} \rightarrow V \rightarrow t\bar{t}$$

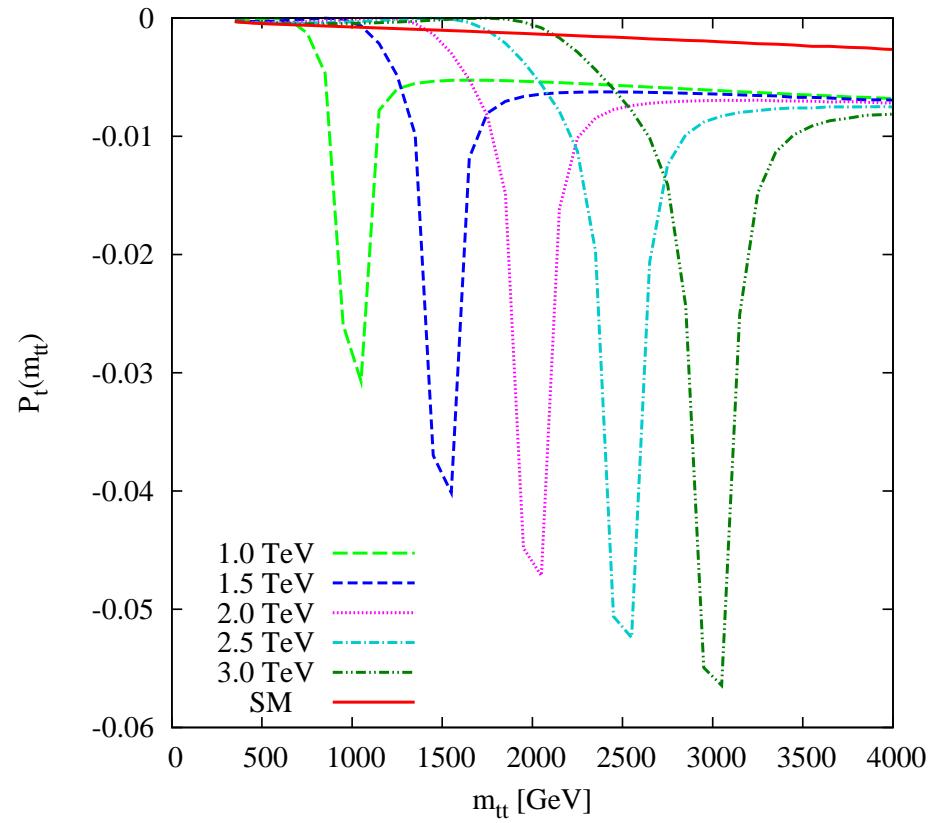
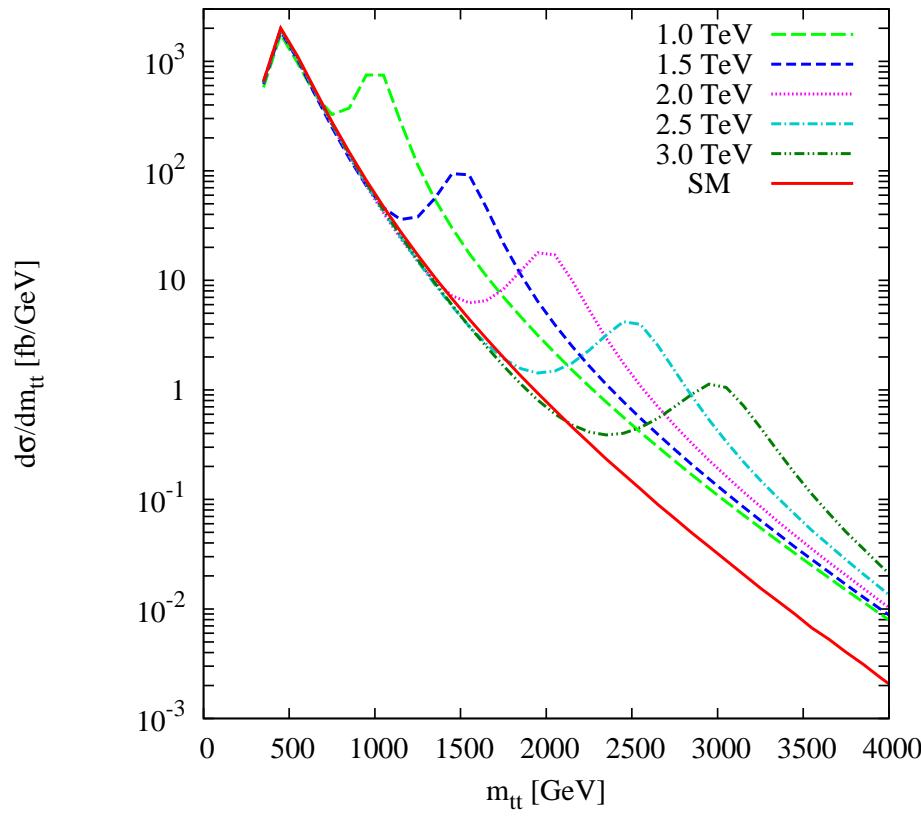
$$V \equiv \gamma, Z, g, \gamma^{(1)}, Z^{(1)}, g^{(1)}$$

The pure SM background:

$$gg \rightarrow V \rightarrow t\bar{t}$$

All KK-excitations contribute to a resonance in  $m_{t\bar{t}}$  distribution. The presence of  $Z$  and  $Z^{(1)}$  is responsible for finite polarization of top quark.

# Flat extra-dimensions: $pp \rightarrow t\bar{t}$



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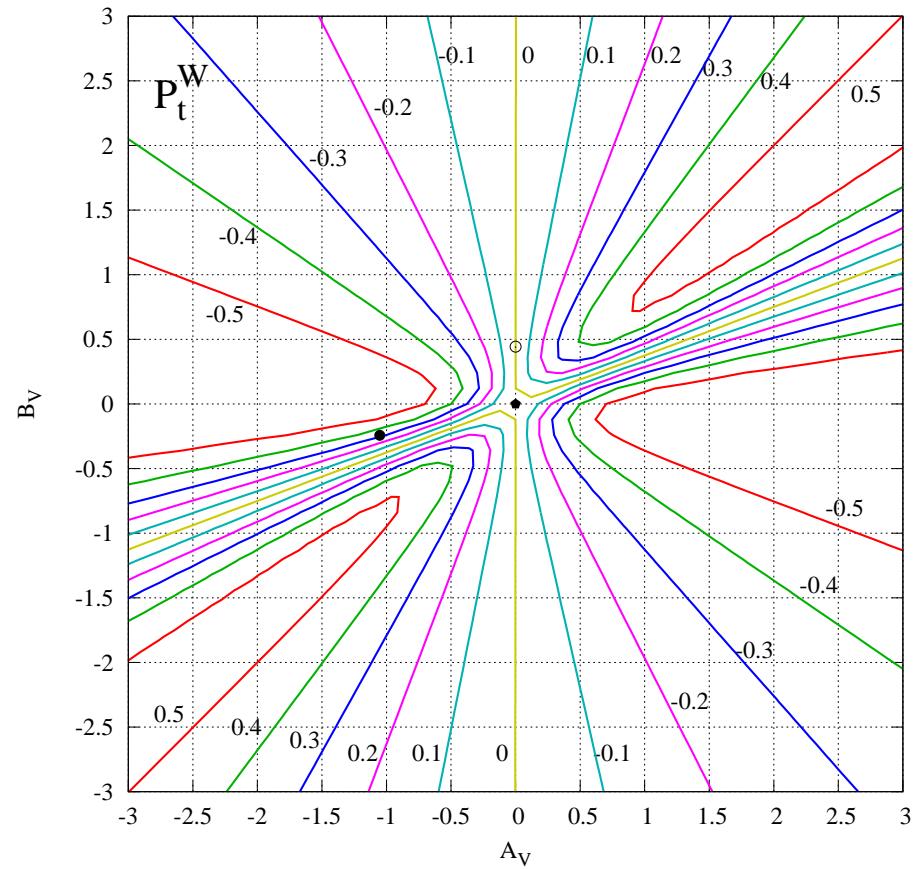
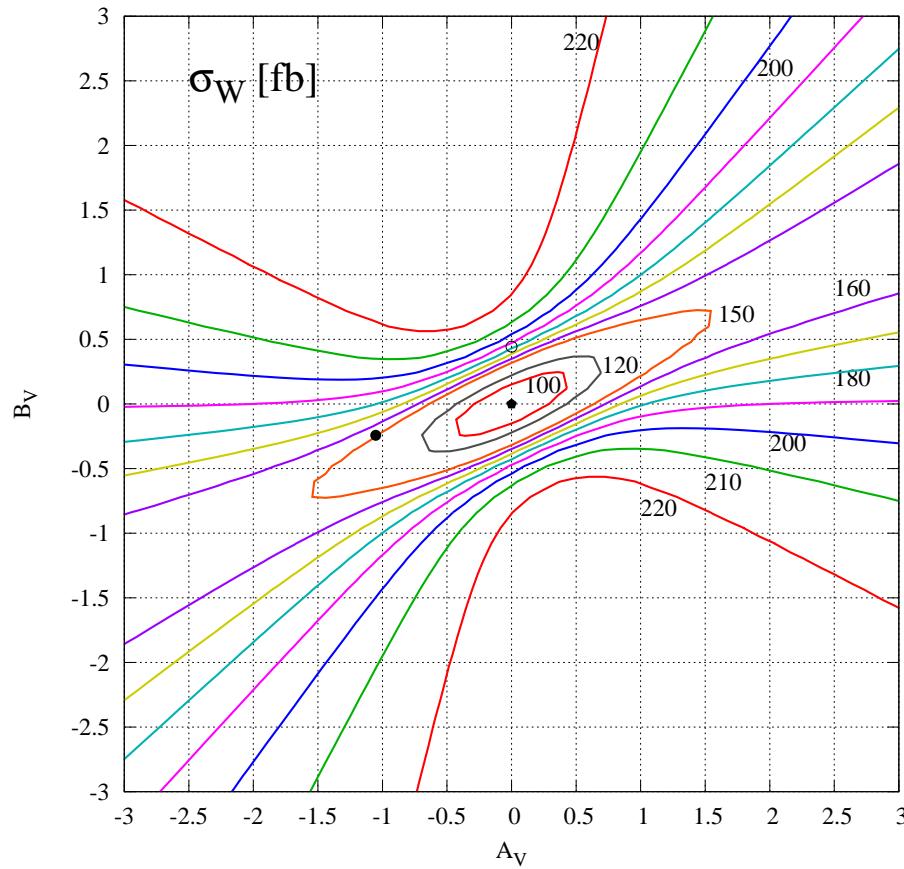
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For  $M_{KK} = 2$  TeV, and  $|m_{t\bar{t}} - M_{KK}| < 50$  GeV.

	$\sigma(pp \rightarrow t\bar{t})$ (fb)	$P_t$
$SM$	77.9	$-1.33 \times 10^{-3}$
$SM + \gamma^{(1)}$	185	$-2.55 \times 10^{-4}$
$SM + Z^{(1)}$	150	$-3.26 \times 10^{-1}$
$SM + g^{(1)}$	1700	$-6.13 \times 10^{-5}$
$SM + V_{KK}$	1900	$-5.87 \times 10^{-2}$

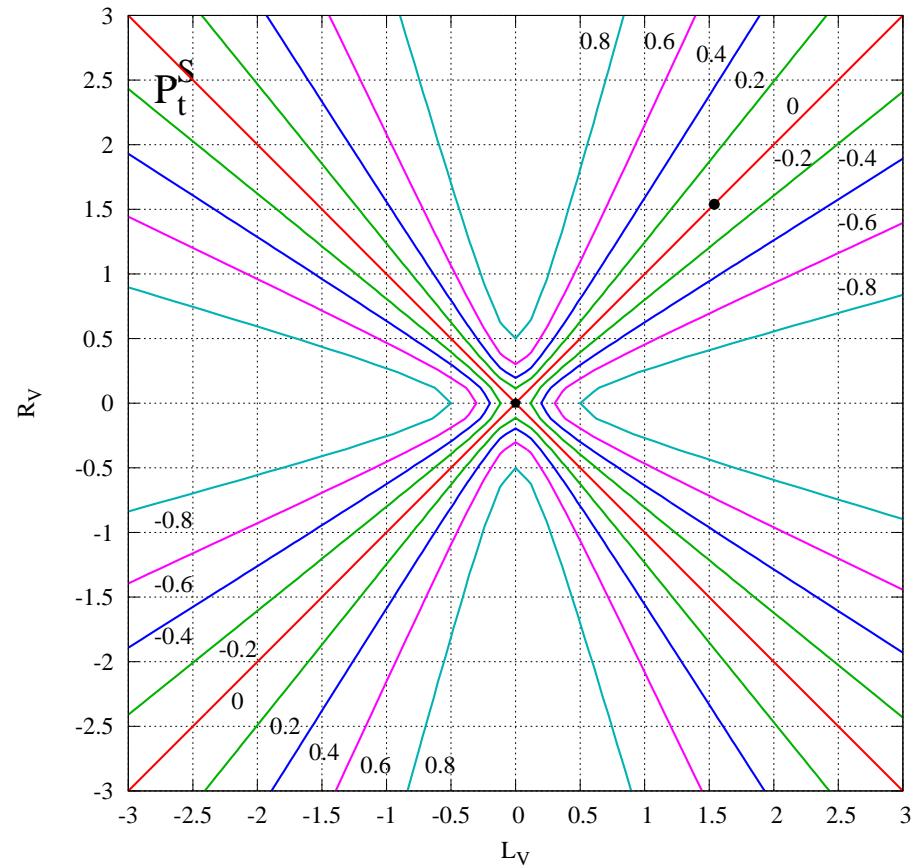
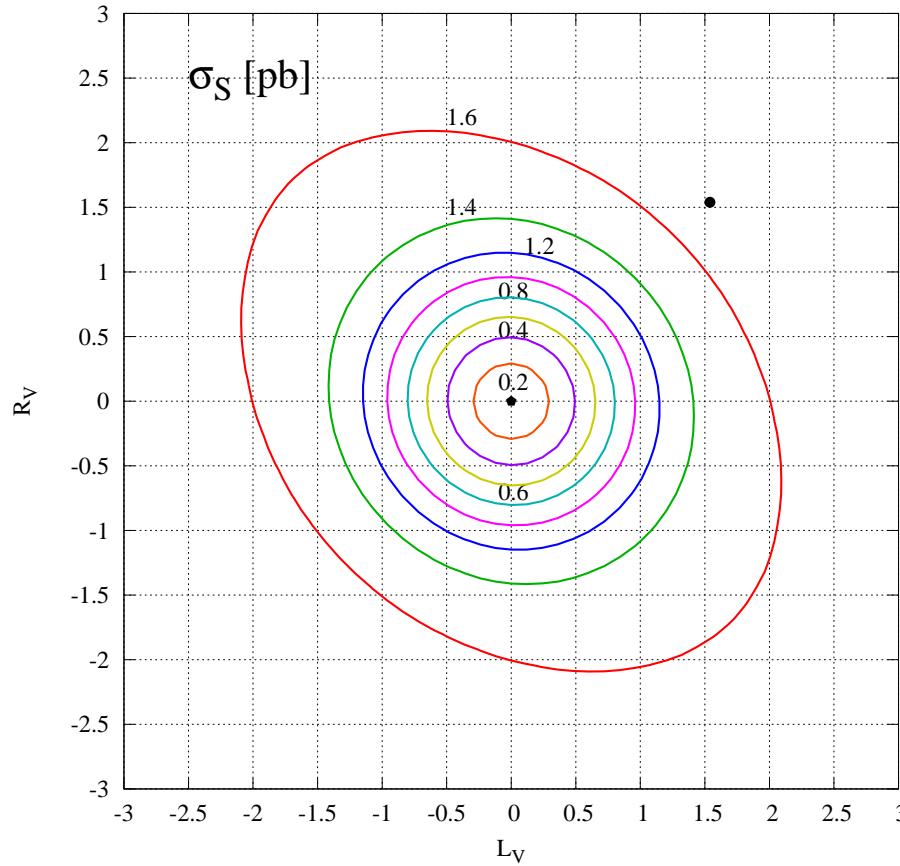
# ED: Weak resonance model

$$f_i \bar{f}_i V := A_V T_3^{f_i} + B_V Q^{f_i} ; \quad i = L, R$$



# ED: Strong resonance model

$$f\bar{f}V := R_V P_R + L_V P_L$$



# Wrapped extra dimensions

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In universal wrapped extra dimension model, with fermion localization in the fifth dimensions, one has differing couplings of  $V_{KK}$

For electro weak boson:

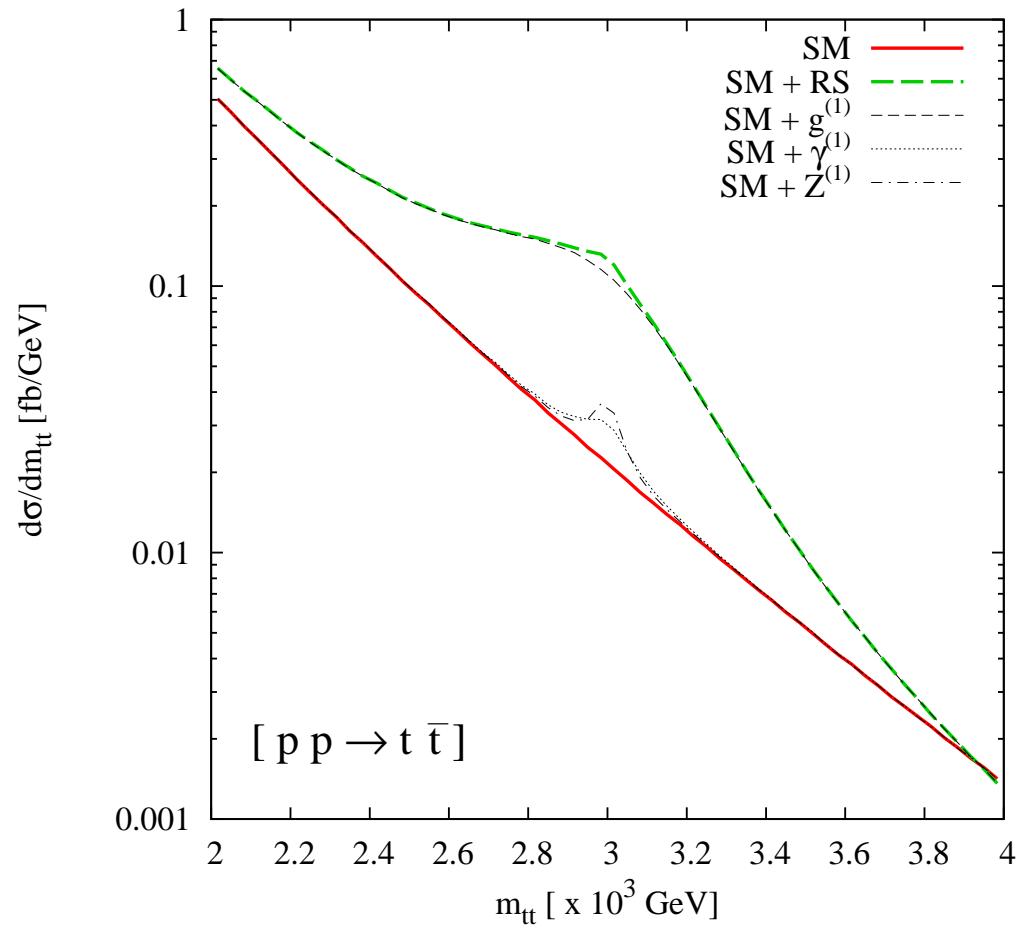
$$f_i \bar{f}_i V := (A_V T_3^{f_i} + B_V Q^{f_i}) Q_V(f_i) ; i = L, R$$

For strong boson:

$$f \bar{f} V := Q_V(f_R) R_V P_R + Q_V(f_L) L_V P_L$$

- can explain fermion mass hierarchy,
- can explain  $A_{FB}^b$  anomaly through  $Z - Z'^{(1)}$  mixing,
- can be probed at LHC upto  $M_{KK} = 3$  TeV through polarization.

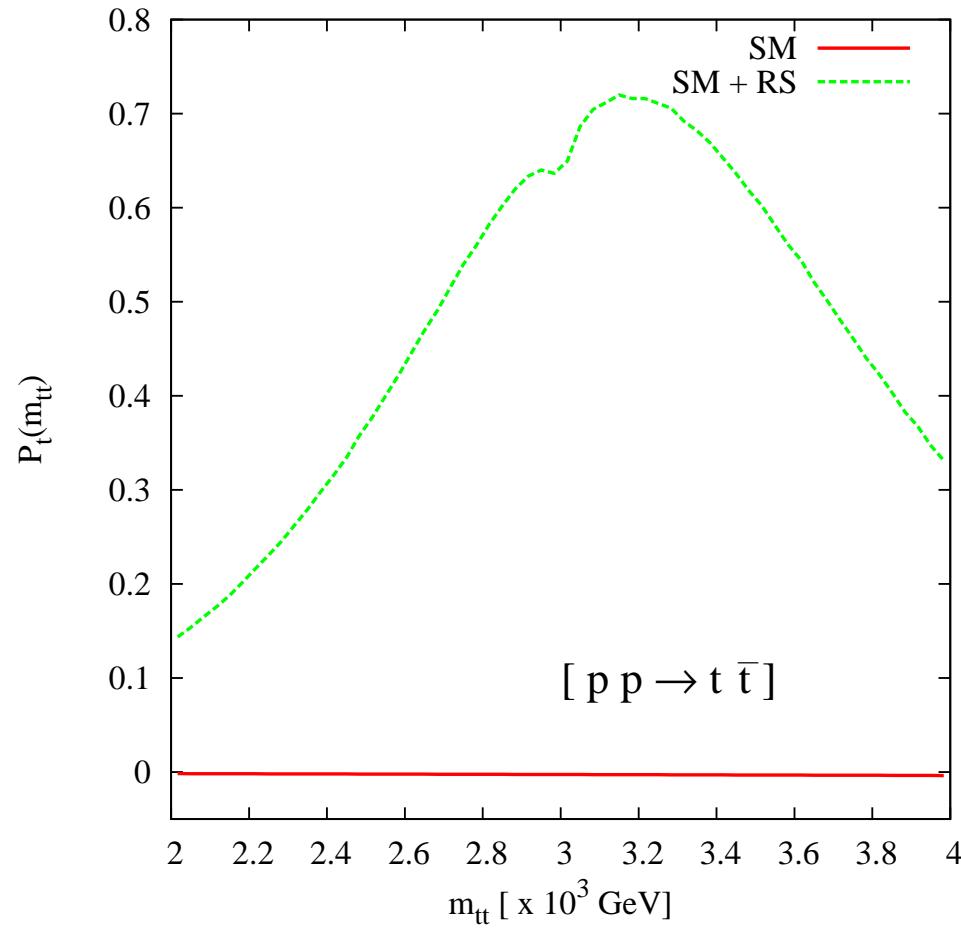
# Wrapped extra dimensions



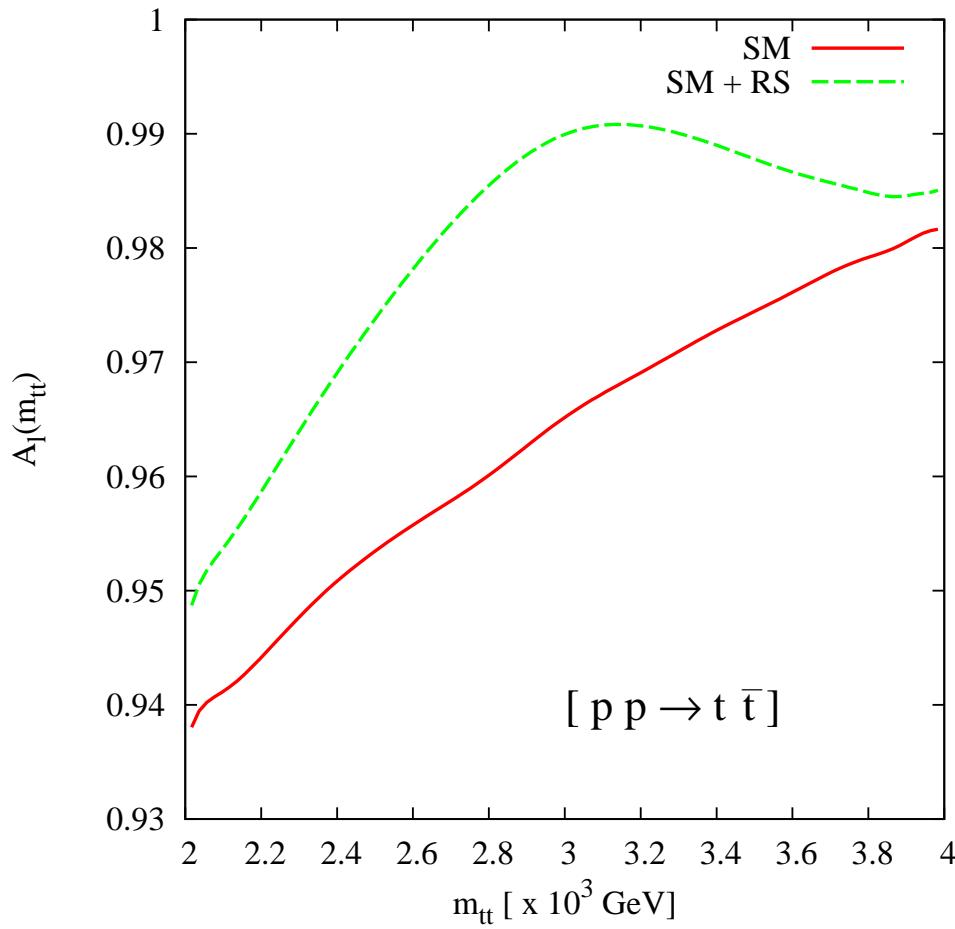
$$\Gamma_{g^{(1)}} = 627 \text{ GeV}, \Gamma_{Z^{(1)}} = 75 \text{ GeV}, \Gamma_{\gamma^{(1)}} = 137 \text{ GeV}.$$

# Wrapped extra dimensions

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# Wrapped extra dimensions



$$A_l = (\sigma(\cos \phi_l > 0) - \sigma(\cos \phi_l < 0)) / \sigma_{tot}$$

# Conclusions

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- Angular distribution of decay lepton in the lab-frame is a good qualitative probe of  $t$ -polarization; quantitatively better for negative polarizations.
- Top quark polarization can be probed at various colliders and it can be instrumental in discovering and characterising new physics.

# Ongoing projects

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- Spin/polarization measurement of new particles in their cascade decay. Look at azimuthal distributions in the lab frame.
- Likelihood mapping of SUSY parameters space using MCMC.

## Contact :

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